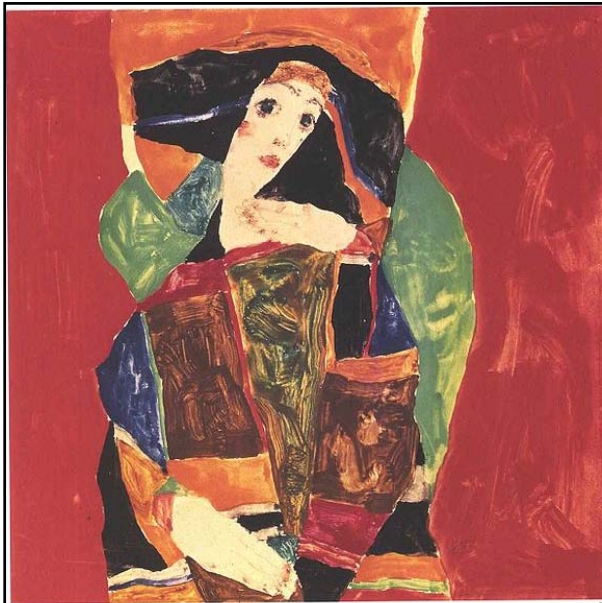




Outline

- Cause-specific survival models in the setting of competing risks
- Data augmentation method
 - Preparation of data
 - Estimate of survival regression models on expanded data
- Covariate-adjusted cumulative incidence: `stcompadj`
- Comparing covariate-adjusted cumulative incidence obtained by two approaches: Cox model (`-stcompadj-`) vs. Fine and Gray method (`-stcrreg-` post-estimation)



**Cause-specific survival models
in the setting of competing risks**

**Common survival
study**

Vs.

Competing risks survival study

Common survival study measures the time from a starting point to an endpoint defined by the occurrence of one type of event.

In the competing risks situation more than one type of event may occur. Often, one type of event is singled out as the event of interest, the other types as competing events. The remarkable feature of this situation is that the occurrence of one type of event either precludes or fundamentally alters the probability of occurrence of the others⁽¹⁾.

Hazard - Probability of Occurrence

The hazard is the fundamental measure of the occurrence of the event and we can investigate the role of various factors in modifying the hazard by using appropriate regression models

In the competing risks situation we can still compute the cause-specific hazard for the event of interest and for the competing event. The “latent failure times” mathematical approach demonstrates that the cause-specific hazard is an estimable function also in a competing risks situation and, thus, we can model it⁽²⁾.

5

Hazard - Probability of Occurrence

The probability that the event occurs before time t can be derived from the hazard through an equation. So, the hazard completely describes this probability distribution. Higher the hazard, higher the probability that the event occurs before t and vice versa.

In a competing risks situation, the probability that the main event occurs before time t (Cumulative Incidence) depends on both the hazard of the main event and the hazard of the competing event. Thus, there is no obvious relationship between the hazard and the cumulative incidence of the main event, the latter depending on the hazard of the competing event too.

6

Consequence for the Information

The hazard and the probability that the event occurs before time t convey the same piece of information.

In the competing risks situation the cause-specific hazard and the cumulative incidence do not convey the same piece of information.

The former tells us about the biological mechanism underlying the specific outcome.

The latter informs us about the probability and, therefore, the actual number of patients failing from a specific cause, taking into account that this type of event could not be observed because hindered or precluded from another type of event⁽²⁾.

7

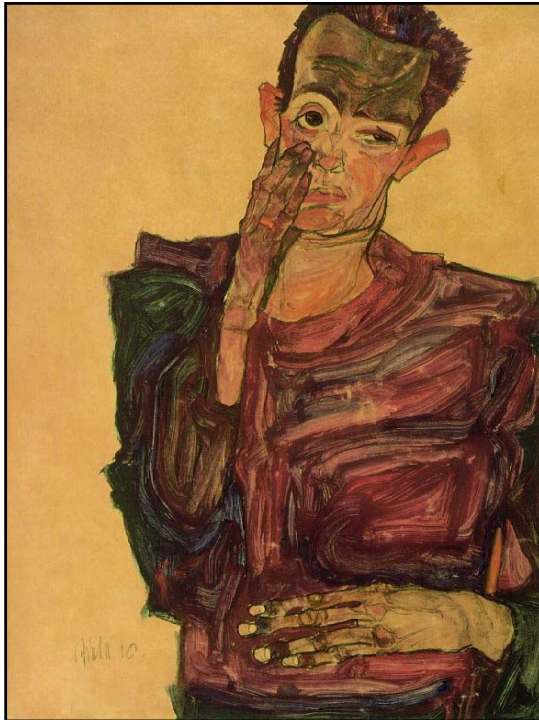
Concluding ...

In a competing risks situation, the cause-specific hazard is an estimable function and we can model it by using, for example, a Cox model.

The parameter estimates we obtain

- are relevant for investigating the factors causing or associated to the occurrence of a specific event
- are not appropriate for detecting whether such factors actually change the probability that the event occurs.

8



Data augmentation method

9

- In a competing risks situation, Cox regression is usually performed by fitting separate models for each cause of failure.
- The hazard corresponding to a specific failure is analyzed considering failures of other causes as censored observations.
- It is possible to make single analysis of two or more cause of failure at the same time rather than fitting separate regression models.
- To perform this analysis a new expanded dataset must be created as follows⁽³⁾.

10

Here are three subjects from the file `malignantmelanoma.dta` containing 205 observations:

| id | time | thick | sex | cause |
|----|------|-------|-----|--------------------|
| 51 | 1516 | -.34 | M | Malignant Melanoma |
| 52 | 1525 | -1.63 | F | Other Causes |
| 53 | 1542 | -2.76 | F | Alive |

This is a competing risks situation because two causes of failures are present:

1. Death from malignant melanoma (coded as 1)
2. Death from other causes (coded as 2).

Two covariates are present: sex and tumor thickness (centered on its mean)

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Expanded format

| id | thick | sex | cause | stratum | _d | _t |
|----|-------|-----|--------------------|---------|----|------|
| 51 | -.34 | M | Malignant Melanoma | 1 | 1 | 1516 |
| 51 | -.34 | M | Malignant Melanoma | 2 | 0 | 1516 |
| 52 | -1.63 | F | Other Causes | 1 | 0 | 1525 |
| 52 | -1.63 | F | Other Causes | 2 | 1 | 1525 |
| 53 | -2.76 | F | Alive | 1 | 0 | 1542 |
| 53 | -2.76 | F | Alive | 2 | 0 | 1542 |

- Each subject is represented twice, one for each cause of failure
- A numeric stratum indicator has been created (`stratum`) taking on the value 1 for the first record and value 2 for the second record of the same subject. This allows that a subject has a specific record for each cause of failure
- The failure indicator `_d` attains the value 1 for each observation of
 - first cause of death in the stratum 1
 - second cause of death in the stratum 2
 and 0 otherwise.

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In the expanded data format we can obtain the same results by fitting a Cox model stratified by the `-stratum-` indicator variable:

```
stcox stratum#(c.sex c.tick), nolog strata(stratum)
```

The model includes an interaction term between `stratum` and the other covariates

| _t | Haz. Ratio | Std. Err. | z | P> z | [95% Conf. Interval] | |
|----------|-----------------|-----------------|------|-------|----------------------|----------|
| ----- | | | | | | |
| stratum# | | | | | | |
| c.sex | | | | | | |
| 1 | 1.775555 | .4709861 | 2.16 | 0.030 | 1.055707 | 2.986242 |
| 2 | 1.720124 | .9280661 | 1.01 | 0.315 | .5974581 | 4.952361 |
| stratum# | | | | | | |
| c.thick | | | | | | |
| 1 | 1.172454 | .0383144 | 4.87 | 0.000 | 1.099714 | 1.250006 |
| 2 | 1.10589 | .0847623 | 1.31 | 0.189 | .9516358 | 1.285149 |
| ----- | | | | | | |

Stratified by stratum

15

Advantages of the expanded data format

- It is possible to fit models where some covariates have exactly the same effect on the main and on the competing event. This cannot be accomplished by fitting separate Cox regressions for each cause of failure⁽⁴⁾.
- A major advantage is that we have at hand the baseline hazard contributions of both events (hazard contributions represent the increment of the cumulative hazard at each event time and are the key quantities for estimating the cumulative incidence function).
- The adjustment for covariates is achieved by multiplying the hazard contributions by the exponentiated linear predictor⁽⁴⁾.

16



Covariate-adjusted cumulative incidence:

`-stcompadj-`

17

`-stcompadj-` is a new Stata macro (v. 10) that computes the adjusted cumulative incidence in the presence of competing risks.

The basic syntax is:

```
stcompadj var [= # var ...] [if] [in] , compet(# [...])
      [ maineffect(varlist) competeffect(varlist) ... ]
```

Fundamentally, `-stcompadj-` :

- expands the dataset as previously described and fits a Cox or a flexible parametric model whose covariates are the variables specified in `var [[= #] var ...]`
- computes the cumulative incidence function from the baseline hazard contributions and the linear predictor
- saves in two variables the cumulative incidence function for the main and competing event adjusted to the mean or to the specified number of each covariate if the `=#` part is specified.

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In the following example we estimate the cumulative incidence for a male with a tumor thickness of 2 mm above the mean.

```
stset time, failure(cause==1)
stcompadj sex=1 thick=2, compet(2) maineffect(thick)
```

- `compet(#)` is not an option. `compet(2)` means that a failure from a competing event occurs whenever `cause` takes on the value 2.
- By default the fitted model considers the covariates as having the same effect on the main as well as on the competing event. In the example `sex` is assumed to have such effect.

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- The options `maineffect(varlist)` and `competeffect(varlist)` allow to fit a model where some of the previously stated variables acts only on the main or on the competing event. In the example `thick` acts only on the main effect.
- Note that the same variable can be specified both in `maineffect(varlist)` and in `competeffect(varlist)`. Then, this variable is assumed to have different effects on the main and competing event.
- `-stcompadj-` creates two variables saving the cumulative incidences functions for the main and competing event. Default names are `CI_Main` and `CI_Comp`.

20

The estimates produced by `-stcompadj-` match the results published by Rosthøj and coll. using the CumInc SAS macro⁽⁴⁾

| stcompadj | | | CumInc | | |
|------------------|----------------------|----------------------|-------------------|------------------|------------------|
| <code>_t</code> | <code>CI_Main</code> | <code>CI_Comp</code> | <code>TIME</code> | <code>P01</code> | <code>P02</code> |
| 10 | 0.00000 | 0.006703 | 10 | 0.00000 | 0.006703 |
| 30 | 0.00000 | 0.013406 | 30 | 0.00000 | 0.013406 |
| 99 | 0.00000 | 0.020155 | 99 | 0.00000 | 0.020155 |
| 185 | 0.00766 | 0.020155 | 185 | 0.00766 | 0.020155 |
| 204 | 0.01545 | 0.020155 | 204 | 0.01545 | 0.020155 |
| 210 | 0.02323 | 0.020155 | 210 | 0.02323 | 0.020155 |
| 232 | 0.03102 | 0.026862 | 232 | 0.03102 | 0.026862 |
| 232 | 0.03102 | 0.026862 | 232 | 0.03102 | 0.026862 |
| 279 | 0.03895 | 0.026862 | 279 | 0.03895 | 0.026862 |
| 295 | 0.04687 | 0.026862 | 295 | 0.04687 | 0.026862 |

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Further validation of the results produced by `-stcompadj-` has been done by using the R-macro (`si.R` and `tutfuncs.R`) prepared by Putter and coll. for a tutorial in competing risks analysis⁽⁵⁾. Using the `si.dta` dataset (see slide 37) the results produced by `-stcompadj-` and R.macros are in very good agreement:

| | stcompadj | | R | | stcompadj | | R | |
|-------------------|-------------------------|------------------------|-------------------------|------------------------|-------------------------|------------------------|-------------------------|------------------------|
| <code>time</code> | <code>CI_ccr1_SI</code> | <code>R_ccr1_SI</code> | <code>CI_ccr0_SI</code> | <code>R_ccr0_SI</code> | <code>CI_ccr0_SI</code> | <code>R_ccr0_SI</code> | <code>CI_ccr0_SI</code> | <code>R_ccr0_SI</code> |
| .112 | .0025065 | .0025065 | .003232 | .003232 | .003232 | .003232 | .003232 | .003232 |
| .137 | .0050148 | .0050148 | .0064639 | .0064639 | .0064639 | .0064639 | .0064639 | .0064639 |
| .474 | .007525 | .007525 | .0096959 | .0096959 | .0096959 | .0096959 | .0096959 | .0096959 |
| .824 | .0100618 | .0100618 | .0129598 | .0129598 | .0129598 | .0129598 | .0129598 | .0129598 |
| .884 | .0125986 | .0125986 | .0162213 | .0162213 | .0162213 | .0162213 | .0162213 | .0162213 |
| | | | | | | | | |
| 12.4 | .3784347 | .3784347 | .3660669 | .3660669 | .3660669 | .3660669 | .3660669 | .3660669 |
| 12.936 | .3872313 | .3872313 | .3705146 | .3705146 | .3705146 | .3705146 | .3705146 | .3705146 |
| 13.361 | .3872313 | .3872313 | .3705146 | .3705146 | .3705146 | .3705146 | .3705146 | .3705146 |
| 13.361 | .3872313 | .3872313 | .3705146 | .3705146 | .3705146 | .3705146 | .3705146 | .3705146 |
| 13.936 | .7015418 | .7015418 | .5211416 | .5211416 | .5211416 | .5211416 | .5211416 | .5211416 |

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| | stcompadj | | R | | stcompadj | | R | |
|---------|--------------|-------------|--------------|-------------|--------------|-------------|--------------|-------------|
| time | CI_ccr1_AIDS | R_ccr1_AIDS | CI_ccr0_AIDS | R_ccr0_AIDS | CI_ccr1_AIDS | R_ccr1_AIDS | CI_ccr0_AIDS | R_ccr0_AIDS |
| 1. 205 | 0 | 0 | 0 | 0 | | | | |
| 1. 44 | .0010797 | .0010797 | .0036907 | .0036907 | | | | |
| 1. 837 | .0021758 | .0021758 | .0074185 | .0074185 | | | | |
| 1. 889 | .0021758 | .0021758 | .0074185 | .0074185 | | | | |
| 2. 048 | .0021758 | .0021758 | .0074185 | .0074185 | | | | |
| ----- | | | | | | | | |
| 11. 387 | .1927379 | .1927379 | .4586331 | .4586331 | | | | |
| 11. 943 | .1962167 | .1962167 | .4635909 | .4635909 | | | | |
| 12. 936 | .1998003 | .1998003 | .4685524 | .4685524 | | | | |
| 13. 936 | .2074857 | .2074858 | .4788584 | .4788584 | | | | |

23

By specifying `-showmod-` we can see the model fitted by `-stcompadj-` before estimating the cumulative incidence function. For example, the model in the slide 13 is shown by `-stcompadj-` as follows:

```
stcompadj sex=1 thick=2, maineffect(sex thick) competeffect(sex thick) ///
        compet(2) showmod
```

Stratified Cox Model in data set expanded in two strata to allow simultaneous assessment of covariates effect on two competing risks.
 Covariates whose name is not changed have the same effect on both events.
 Covariates whose name is prefixed by **Main_** have effect only on the main event.
 Covariates whose name is prefixed by **Compet_** have effect only on the competing event.

Stratified Cox regr. -- no ties

```
-----
```

| _t | Haz. Ratio | Std. Err. | z | P> z | [95% Conf. Interval] |
|---------------------|-----------------|-----------------|-------------|--------------|--------------------------|
| Main_sex | 1.775555 | .4709861 | 2.16 | 0.030 | 1.055707 2.986242 |
| Main_thick | 1.172454 | .0383144 | 4.87 | 0.000 | 1.099714 1.250006 |
| Compet_sex | 1.720124 | .9280661 | 1.01 | 0.315 | .5974581 4.952361 |
| Compet_thick | 1.10589 | .0847623 | 1.31 | 0.189 | .9516358 1.285149 |

Stratified by `_000002` ²⁴

The option `-savexpanded(filename [, replace])-` allows to save the dataset in the expanded format.

Data in expanded format can be used:

- to reproduce the model fitted by `-stcompadj-`
- to test the equality of the covariate effects on the main and competing risks
- to compare the baseline hazards for the main and competing events and test the difference under the assumption of their proportionality.

See reference ⁽⁵⁾ and help file of `-stcompadj-` for details.

25

Flexible Parametric Models

- Flexible parametric models have been proposed as a valid alternative to the Cox model.
- `-stpm-` enabled these models to be fitted by Stata⁽⁶⁾. Recently `-stpm2(7)` allowed the estimates of the confidence intervals of the fitted cumulative hazard function to be obtained too.
- When `-flexible-` is specified, `-stcompadj-` fits a flexible parametric model to the expanded data set. Then, by adding the option `-ci-`, the confidence intervals of the covariate-adjusted cumulative incidence are worked out from the confidence intervals of the fitted cumulative hazard function.

```
stcompadj sex=1 thick=2, compet(2) maineffect(thick) ///
      flexible ci gen(FICI_Main FICI_Comp) df(2)
```

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Flexible Parametric Models

- Flexible parametric models have been proposed as a valid alternative to the Cox model.
- `-stpm-` enabled the fit of these models in Stata⁽⁶⁾. Recently `-stpm2`⁽⁷⁾ extended the methodology allowing to obtain the estimates of the confidence intervals of the fitted cumulative hazard function.
- When `-flexible-` is specified `-stcompadj-` fits a flexible parametric model to the expanded data set. Then, by adding the option `-ci-`, the confidence intervals of the covariate-adjusted cumulative incidence are worked out from the confidence intervals of the fitted cumulative hazard function.

```
stcompadj sex=1 thick=2, compet(2) maineffect(thick) ///
      flexible ci gen(FICI_Main FICI_Comp) df(2)
```

27

Flexible Parametric Models

- Flexible parametric models have been proposed as a valid alternative to the Cox model.
- `-stpm-` enabled the fit of these models in Stata⁽⁶⁾. Recently `-stpm2`⁽⁷⁾ extended the methodology allowing to obtain the estimates of the confidence intervals of the fitted cumulative hazard function.

The option `generate(newvarname1 newvarname2)` allow to give two alternative names to the variables containing the covariate-adjusted CI function for the main and competing event.

Higher and lower confidence bounds of the CI are saved in four new variables whose names are prefixed by `Hi_` and `Lo_`.

```
stcompadj sex=1 thick=2, compet(2) maineffect(thick) ///
      flexible ci gen(FICI_Main FICI_Comp) df(2)
```

28

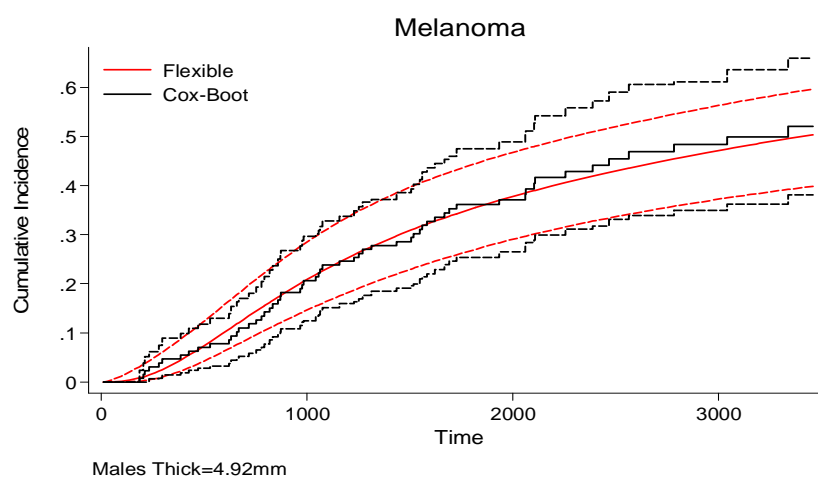
As an alternative, the option `-bootci-` computes the confidence intervals of the cumulative incidence (CI) function by resampling observations from the expanded dataset:

```
stcompadj sex=1 thick=2, compet(2) maineffect(thick) ///
      bootci gen(BootCI_Main BootCI_Comp)
```

In the next graph we compare the CI functions for the main and the competing event estimated by fitting a:

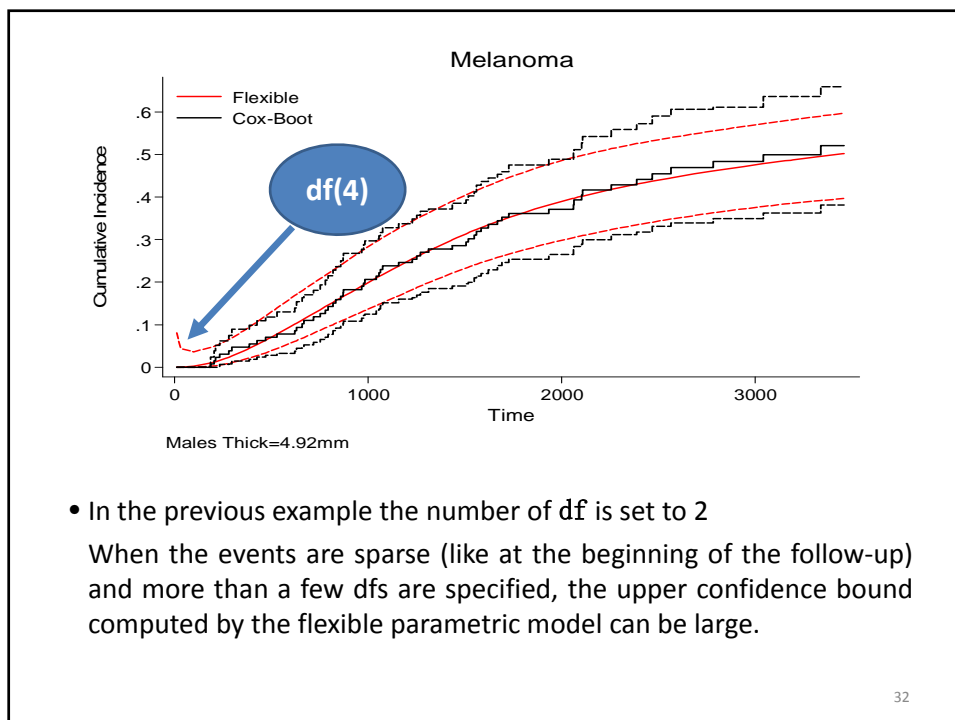
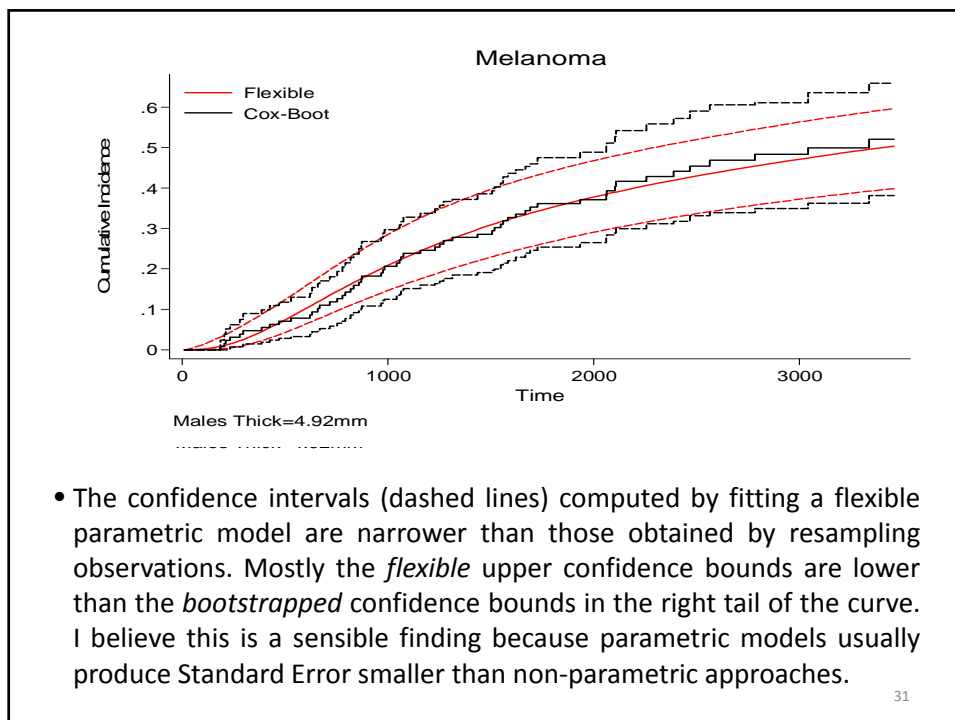
1. **Cox model.** Confidence Intervals are computed by resampling observations (1000 reps are the default);
2. **flexible parametric model.** Confidence intervals are computed from the confidence intervals of the predicted cumulative hazard function

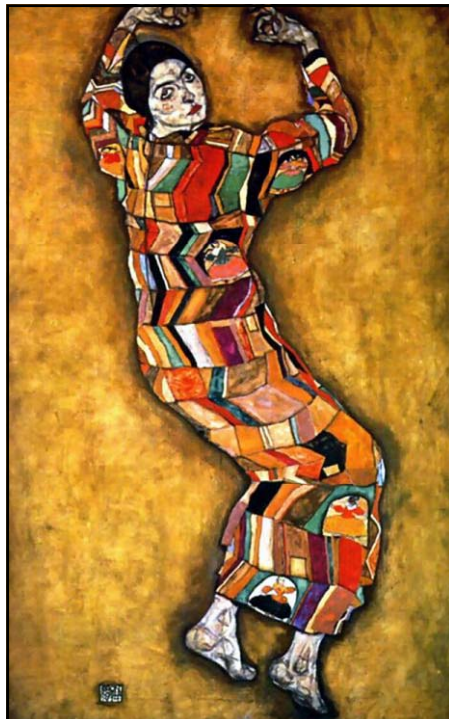
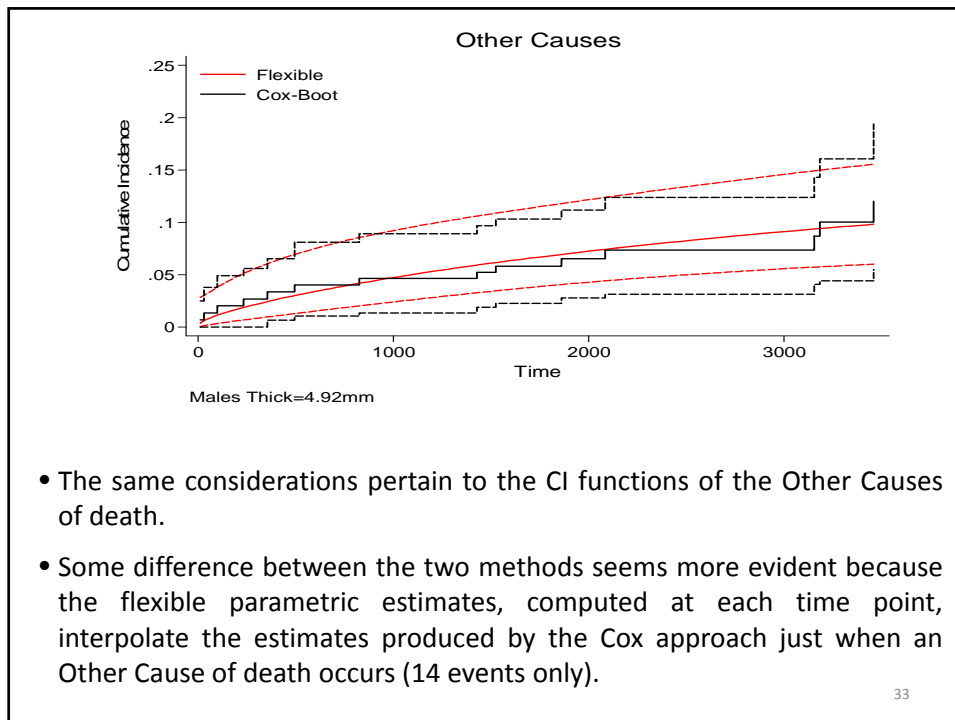
29



- The CI estimates (solid lines) obtained by fitting a Cox model and a flexible parametric model are in good agreement until 1500 days from the diagnosis. After, some difference can be seen.

30





Comparing covariate-adjusted cumulative incidence by two approaches

34

- Stata 11 allows competing risks regression models to be fitted.
- Fine and Gray⁽⁸⁾ proposed a method that directly compares the cumulative incidence function by modeling the so-called hazard of the subdistribution.
- `-stcrreg-` is the new command that fits this model and estimates the hazard of the subdistribution ratios. Furthermore, via `-stcurve-`, we can obtain estimates of the CI predicted by the model.
- In the following example we will compute the CI estimates in males and females by using:
 1. the Fine and Gray regression model (`-stcrreg-`)
 2. the Cox model (`-stcompadj-`)

35

- These estimates will be compared using the cumulative incidence produced in two groups via `-stcompet-` (with no model assumption) to see which approach better fits the data.

```
* Cox estimate for sex
stset time, failure(cause==1) id(id)
stcompadj sex=1, compet(2)           sex is modeled as having
rename CI_Main CI_Msex1             the same effect on the
stcompadj sex=0 , compet(2)         main and on the
rename CI_Main CI_Msex0             competing event
```

```
* Estimates of FG cumulative incidence
stcrreg sex, compete(cause==2)
stcurve, cif at1(sex=0) at2(sex=1) outfile(ci_strreg, replace)
```

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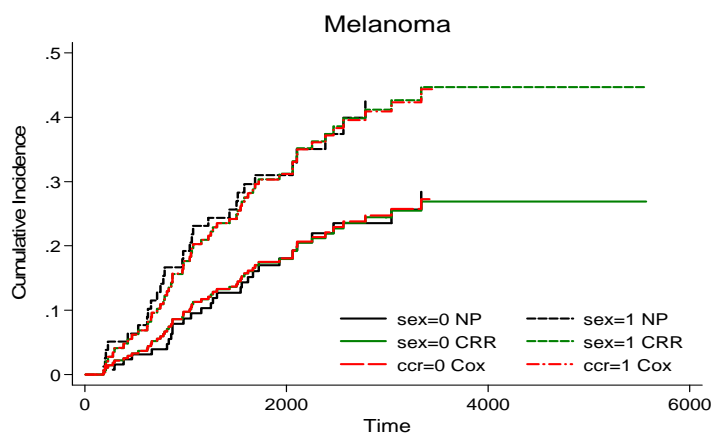
```

* Non parametric CI estimates
stcompet CumInc=ci, compet1(2) by(sex)
g CI_sex0 = CumInc if sex==0 & cause==1
g CI_sex1 = CumInc if sex==1 & cause==1

merge m:m _t using ci_streg

```

37



In this graph we see that:

- the Cox and Fine-Gray approaches provide almost exactly the same estimates
- they both reach an excellent fit to the data.

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This is not always the case.

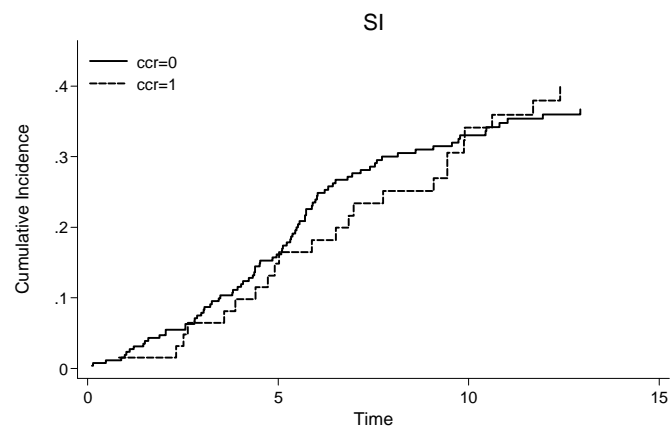
An opposed example can be found in the tutorial by Putter and coll., reproduced in the analysis of [ST] manual (p. 207-211, 226-227).

The data consists of 324 HIV infected patients. The competing events are:

1. the appearance of syncytium inducing (SI) HIV phenotype
2. AIDS

The aim of the analysis is to model the cumulative incidence in relation to the variable `ccr` that equals 1 if a deletion occurs in a receptor gene and 0 otherwise.

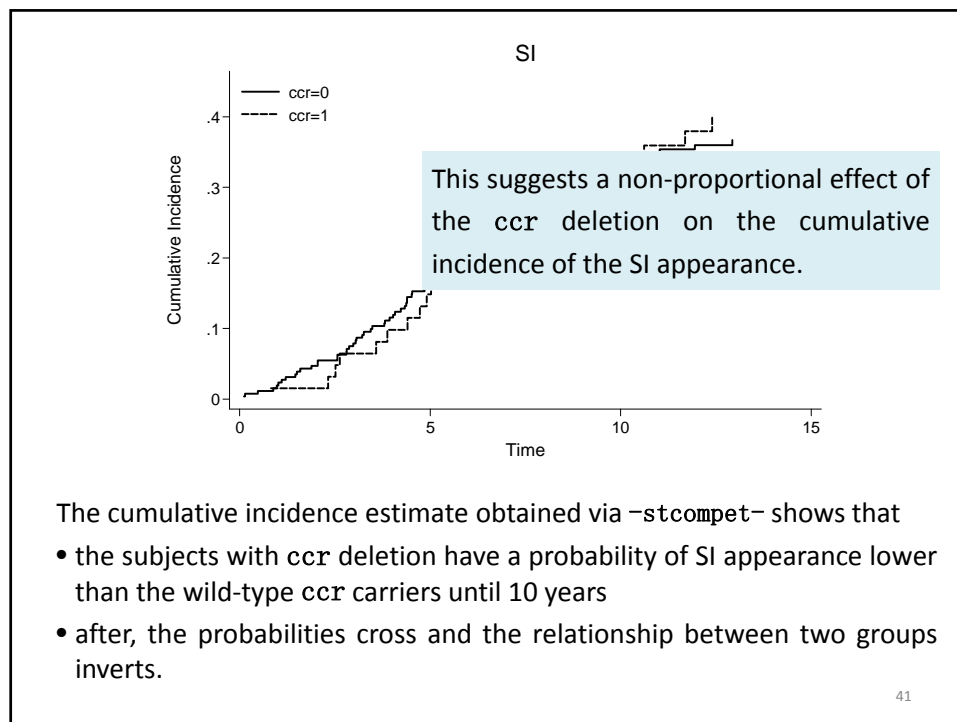
39



The cumulative incidence estimate obtained via `-stcompet-` shows that

- the subjects with `ccr` deletion have a probability of SI appearance lower than the wild-type `ccr` carriers until 10 years
- the probabilities cross and the relationship between two groups inverts after ten years have elapsed.

40



```
use e:\data\si,clear
stset time, failure(status==2) // SI is the event of interest
```

*** Estimates of FG Cumulative Incidence**

```
sterreg ccr, compete(status==1)
stcurve, cif at1(ccr=0) at2(ccr=1) outfile(ci_streg,replace)
```

*** Estimates of Cox CI**

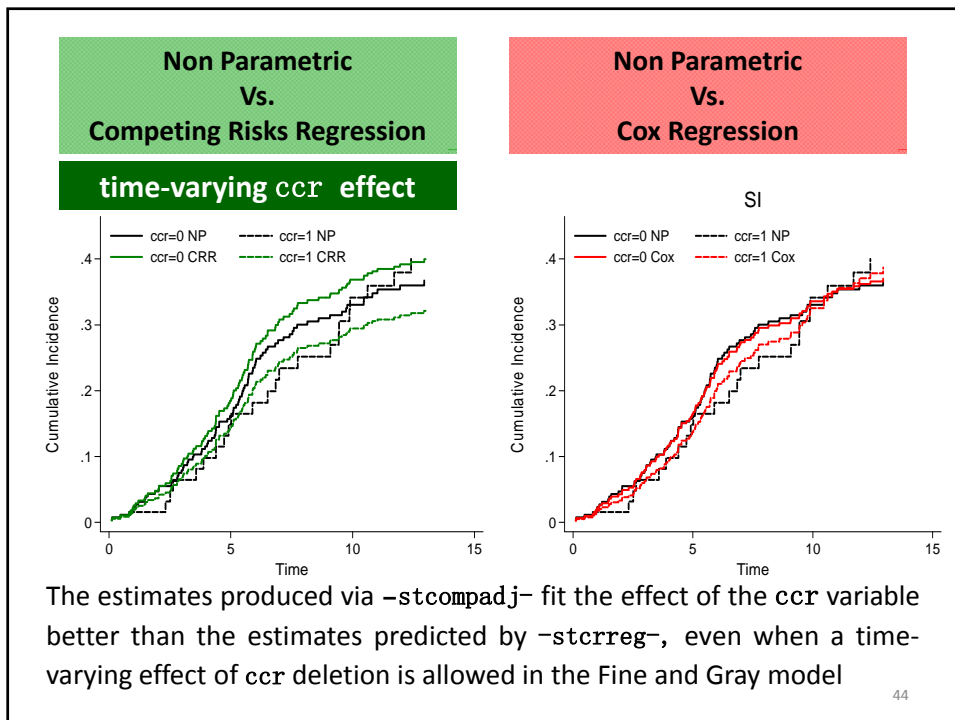
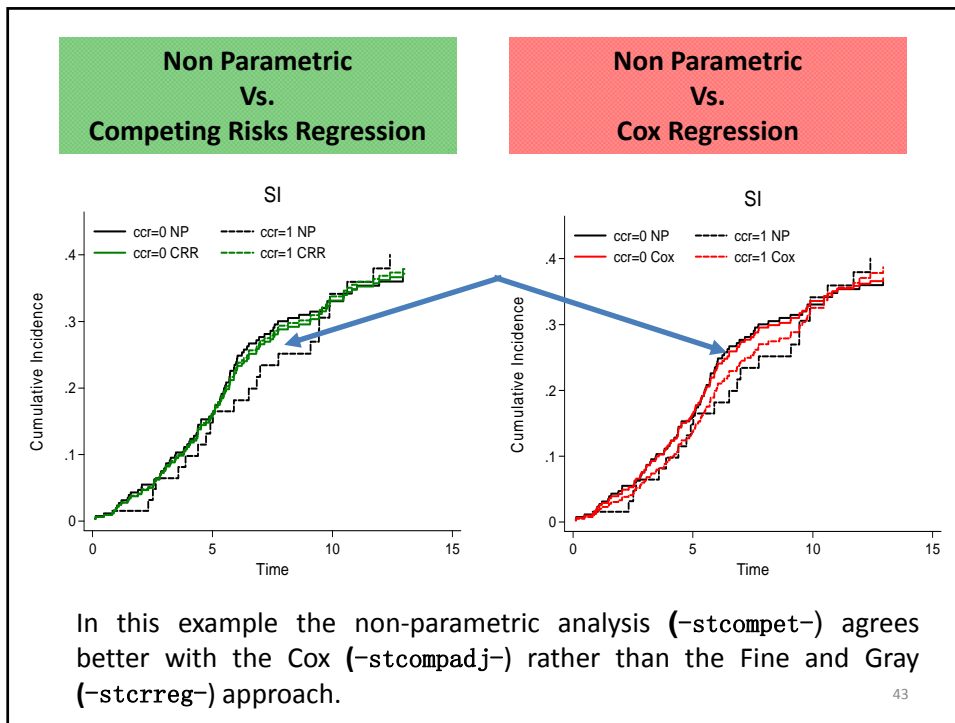
```
stcompadj ccr=0, compet(1) maineffect(ccr) ///
    competeffect(ccr) gen(CI_Main0 CI_Comp0)

stcompadj ccr=1, compet(1) maineffect(ccr) ///
    competeffect(ccr) gen(CI_Main1 CI_Comp1)
```

*** Non parametric CI estimates**

```
stcompet CumInc=ci, compet1(1) by(ccr)
g CI_ccr0 = CumInc if ccr==0 & status==2
g CI_ccr1 = CumInc if ccr==1 & status==2
```

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It may seem surprising that the covariate-adjusted cumulative incidence obtained by `-stcompadj-` (Cox model) fits the data better than the Fine and Gray model prediction. However, we should consider that

- `-stcrreg-` predicts the cumulative incidence function from the cumulative subhazard distribution of the main event alone;
- `-stcompadj-` fits two models, one for the main and one for the competing event. From each
 - it derives separate baseline hazard contributions estimates for the main and for the competing event;
 - it combines these estimates as in the non-parametric approach.
- This allows `-stcompadj-` to achieve a greater flexibility in estimating the cumulative incidence than the Fine and Gray approach.

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Conclusions

- In the context of competing risks, the analysis of cause-specific hazards and the analysis of the cumulative incidence of a specific event convey different pieces of information and they both are worth to be studied.
- The estimate of the cumulative incidence function can be obtained by applying the cause-specific survival and the competing risks (Fine and Gray) regression models.
- Data augmentation technique offers several pros, particularly it consents to easily estimate the covariate-adjusted cumulative incidence according to the cause-specific approach.
- `-stcompadj-` is a new Stata command automating the steps required to prepare data and producing the estimate of this function at a specified level of the covariates included in the model.

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- To this aim `-stcompadj-` can fit the usual Cox model or the more recent flexible parametric models, the latter allowing a straightforward estimate of the confidence intervals of the covariate-adjusted cumulative incidence.
- When the Fine and Gray model does not fit the data, a better estimate of the covariate-adjusted cumulative incidence can be achieved through the cause-specific survival approach, i.e. by `-stcompadj-`.
- The new command is also provided with a help file in which the user can run an example, taken from references ⁽⁴⁾ and ⁽⁵⁾, by clicking on the viewer window.
- `-stcompadj-` is available for download from the SSC-Archive.

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Paintings from Egon Schiele

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