# STATA FUNCTIONS REFERENCE MANUAL RELEASE 19



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### **Cross-referencing the documentation**

When reading this manual, you will find references to other Stata manuals, for example, [U] 27 Overview of Stata estimation commands; [R] regress; and [D] reshape. The first example is a reference to chapter 27, Overview of Stata estimation commands, in the User's Guide; the second is a reference to the regress entry in the Base Reference Manual; and the third is a reference to the reshape entry in the Data Management Reference Manual.

All the manuals in the Stata Documentation have a shorthand notation:

[GSM] [GSU]	Getting Started with Stata for Mac Getting Started with Stata for Unix
[GSW]	Getting Started with Stata for Windows
נטן	Stata User's Guide
[R]	Stata Base Reference Manual
[ADAPT]	Stata Adaptive Designs: Group Sequential Trials Reference Manual
[BAYES]	Stata Bayesian Analysis Reference Manual
[BMA]	Stata Bayesian Model Averaging Reference Manual
[CAUSAL]	Stata Causal Inference and Treatment-Effects Estimation Reference Manual
[CM]	Stata Choice Models Reference Manual
[D]	Stata Data Management Reference Manual
[DSGE]	Stata Dynamic Stochastic General Equilibrium Models Reference Manual
[ERM]	Stata Extended Regression Models Reference Manual
[FMM]	Stata Finite Mixture Models Reference Manual
[FN]	Stata Functions Reference Manual
[G]	Stata Graphics Reference Manual
[H2OML]	Machine Learning in Stata Using H2O: Ensemble Decision Trees Reference Manual
[IRT]	Stata Item Response Theory Reference Manual
[LASSO]	Stata Lasso Reference Manual
[XT]	Stata Longitudinal-Data/Panel-Data Reference Manual
[META]	Stata Meta-Analysis Reference Manual
[ME]	Stata Multilevel Mixed-Effects Reference Manual
[MI]	Stata Multiple-Imputation Reference Manual
[MV]	Stata Multivariate Statistics Reference Manual
[PSS]	Stata Power, Precision, and Sample-Size Reference Manual
[P]	Stata Programming Reference Manual
[RPT]	Stata Reporting Reference Manual
[SP]	Stata Spatial Autoregressive Models Reference Manual
[SEM]	Stata Structural Equation Modeling Reference Manual
[SVY]	Stata Survey Data Reference Manual
[ST]	Stata Survival Analysis Reference Manual
[TABLES]	Stata Customizable Tables and Collected Results Reference Manual
[TS]	Stata Time-Series Reference Manual
[I]	Stata Index
0.0	

[M] Mata Reference Manual

#### Description

This manual describes the functions allowed by Stata. For information on Mata functions, see [M-4] Intro.

A quick note about missing values: Stata denotes a numeric missing value by ., .a, .b, ..., or .z. A string missing value is denoted by "" (the empty string). Here any one of these may be referred to by missing. If a numeric value x is missing, then  $x \ge .$  is true. If a numeric value x is not missing, then x < . is true.

See [U] 12.2.1 Missing values for details.

#### Reference

Cox, N. J. 2011. Speaking Stata: Fun and fluency with functions. Stata Journal 11: 460-471.

#### Also see

[U] 1.3 What's new

#### Contents

Date and time functions Mathematical functions Matrix functions Programming functions Random-number functions Selecting time-span functions Statistical functions String functions Trigonometric functions

#### Date and time functions

$\texttt{age}(e_{d\text{DOB}},e_{d}[,s_{nl}])$	the age in integer years on $e_d$ for date of birth $e_{d{\rm DOB}}$ with $s_{nl}$ the nonleap-year birthday for 29feb birthdates
$\texttt{age\_frac}(e_{d\texttt{DOB}},e_{d}\big[,s_{nl}\big])$	the age in years, including the fractional part, on $e_d$ for date of birth $e_{d\rm DOB}$ with $s_{nl}$ the nonleap-year birthday for 29feb birthdates
$\texttt{birthday}(e_{d\texttt{DOB}}, Y\!\big[\;, s_{nl}\big])$	the $e_d$ date of the birthday in year $Y$ for date of birth $e_{d{\rm DOB}}$ with $s_{nl}$ the nonleap-year birthday for 29feb birthdates
$\texttt{bofd("}{cal"}\texttt{,}e_d\texttt{)}$	the $e_b$ business date corresponding to $e_d$
$Cdhms(e_d, h, m, s)$	the $e_{tC}$ datetime (ms. with leap seconds since 01jan1960 00:00:00000) corresponding to $e_d$ , $h$ , $m$ , $s$
Chms(h, m, s)	the $e_{tC}$ date time (ms. with leap seconds since 01jan1960 00:00:00.000) corresponding to $h, m, s$ on 01jan1960
$\texttt{Clock}(s_1, s_2[\ \textbf{,} Y])$	the $e_{tC}$ date time (ms. with leap seconds since 01jan1960 00:00:00.000) corresponding to $s_1$ based on $s_2$ and $Y$
$\texttt{clock}(s_1, s_2[\ \textbf{,} Y])$	the $e_{tc}$ date time (ms. since 01jan1960 00:00:00.000) corresponding to $s_1$ based on $s_2$ and $Y$
$\texttt{Clockdiff}(e_{tC1}, e_{tC2}, s_u)$	the $e_{tC}$ datetime difference, rounded down to an integer, from $e_{tC1}$ to $e_{tC2}$ in $s_u$ units of days, hours, minutes, seconds, or milliseconds
$\texttt{clockdiff}(e_{tc1}, e_{tc2}, s_u)$	the $e_{tc}$ date time difference, rounded down to an integer, from $e_{tc1}$ to $e_{tc2}$ in $s_u$ units of days, hours, minutes, seconds, or milliseconds
$Clockdiff_frac(e_{tC1}, e_{tC2}, s_u)$	
	the $e_{tC}$ date time difference, including the fractional part, from $e_{tC1}$ to $e_{tC2}$ in $s_u$ units of days, hours, minutes, seconds, or milliseconds
$\texttt{clockdiff\_frac}(e_{tc1}, e_{tc2}, s_u)$	the $e_{tc}$ date time difference, including the fractional part, from $e_{tc1}$ to $e_{tc2}$ in $s_u$ units of days, hours, minutes, seconds, or milliseconds
$\texttt{Clockpart}(e_{tC}, s_u)$	the integer year, month, day, hour, minute, second, or millisecond of $e_{tC}$ with $s_u$ specifying which time part
$\texttt{clockpart}(e_{tc}, s_u)$	the integer year, month, day, hour, minute, second, or millisecond of $e_{tc}$ with $s_u$ specifying which time part
Cmdyhms(M, D, Y, h, m, s)	the $e_{tC}$ datetime (ms. with leap seconds since 01jan1960 00:00:00.000) corresponding to $M$ , $D$ , $Y$ , $h$ , $m$ , $s$

$\operatorname{Cofc}(e_{tc})$	the $e_{tC}$ datetime (ms. with leap seconds since 01jan1960 00:00:00.000) of $e_{tc}$ (ms. without leap seconds since 01jan1960 00:00:00.000)
$\texttt{cofC}(e_{tC})$	the $e_{tc}$ date time (ms. without leap seconds since 01jan1960 00:00:00.000) of $e_{tC}$ (ms. with leap seconds since 01jan1960 00:00:00.000)
$Cofd(e_d)$	the $e_{tC}$ date time (ms. with leap seconds since 01jan1960 00:00:00.000) of date $e_d$ at time 00:00:00.000
$\texttt{cofd}(e_d)$	the $e_{tc}$ date time (ms. since 01jan1960 00:00:00.000) of date $e_d$ at time 00:00:00.000
$\texttt{daily}(s_1, s_2[, Y])$	a synonym for date( $s_1$ , $s_2$ [, $Y$ ])
$\mathtt{date}(s_1,s_2[\ ,Y])$	the $e_d$ date (days since 01jan1960) corresponding to $s_1$ based on $s_2$ and $Y$
$\texttt{datediff}(e_{d1}, e_{d2}, s_u[\ , s_{nl}\ ])$	the difference, rounded down to an integer, from $e_{d1}$ to $e_{d2}$ in $s_u$ units of days, months, or years with $s_{nl}$ the nonleap-year anniversary for $e_{d1}$ on 29feb
$\texttt{datediff\_frac}(e_{d1}, e_{d2}, s_u[\text{,} s_{d2}, s_{d2}, s_{d2}], s_{d2} \in \mathbb{R}^{d}$	<sub>nl</sub> ])
	the difference, including the fractional part, from $e_{d1}$ to $e_{d2}$ in $s_u$ units of days, months, or years with $s_{nl}$ the nonleap-year anniversary for $e_{d1}$ on 29feb
$\texttt{datepart}(e_d, s_u)$	the integer year, month, or day of $e_d$ with $s_u$ specifying year, month, or day
$day(e_d)$	the numeric day of the month corresponding to $e_d$
daysinmonth( $e_d$ )	the number of days in the month of $e_d$
dayssincedow( $e_d$ , $d$ )	a synonym for dayssinceweekday $(e_d, d)$
dayssinceweekday( $e_d$ , $d$ )	the number of days until $e_d$ since previous day-of-week $d$
$daysuntildow(e_d,d)$	a synonym for daysuntilweekday ( $e_d$ , $d$ )
daysuntilweekday $(e_d, d)$	the number of days from $e_d$ until next day-of-week $d$
$dhms(e_d, h, m, s)$	the $e_{tc}$ date time (ms. since 01jan1960 00:00:00.000) corresponding to $e_d,h,m,$ and $s$
dmy(D, M, Y)	the $e_d$ date (days since 01jan1960) corresponding to $D, M, Y$
$dofb(e_b, "cal")$	the $e_d$ date time corresponding to $e_b$
$\texttt{dofC}(e_{tC})$	the $e_d$ date (days since 01jan1960) of datetime $e_{tC}$ (ms. with leap seconds since 01jan1960 00:00:00.000)
$dofc(e_{tc})$	the $e_d$ date (days since 01jan1960) of datetime $e_{tc}$ (ms. since 01jan1960 00:00:00.000)
$dofh(e_h)$	the $e_d$ date (days since 01jan1960) of the start of half-year $e_h$
$\texttt{dofm}(e_m)$	the $e_d$ date (days since 01jan1960) of the start of month $e_m$
$dofq(e_q)$	the $e_d$ date (days since 01jan1960) of the start of quarter $e_q$
$dofw(e_w)$	the $e_d$ date (days since 01jan1960) of the start of week $e_w$
$dofy(e_y)$	the $e_d$ date (days since 01jan1960) of 01jan in year $e_y$
$dow(e_d)$	the numeric day of the week corresponding to date $e_d$ ; $0 =$ Sunday, $1 =$ Monday,, $6 =$ Saturday
$doy(e_d)$	the numeric day of the year corresponding to date $e_d$

```
the e_d date of the first day of the month of e_d
firstdayofmonth(e_d)
firstdowofmonth(M, Y, d)
                                   a synonym for firstweekdayofmonth(M, Y, d)
firstweekdayofmonth(M, Y, d)
                                   the e_d date of the first day-of-week d in month M of year Y
halfyear(e_d)
                                   the numeric half of the year corresponding to date e_d
halfyearly(s_1, s_2[, Y])
                                   the e_h half-yearly date (half-years since 1960h1) corresponding to
                                   s_1 based on s_2 and Y; Y specifies topyear; see date()
hh(e_{tc})
                                   the hour corresponding to date time e_{tc} (ms. since 01 jan 1960
                                   (00:00:00.000)
hhC(e_{tC})
                                   the hour corresponding to date time e_{tC} (ms. with leap seconds since
                                   01jan1960 00:00:00.000)
hms(h,m,s)
                                   the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) corresponding
                                   to h, m, s on 01jan1960
hofd(e_d)
                                   the e_h half-yearly date (half years since 1960h1) containing date e_d
hours(ms)
                                   ms/3,600,000
isleapsecond(e_{tC})
                                   1 if e_{tC} is a leap second; otherwise, 0
isleapyear(Y)
                                   1 if Y is a leap year; otherwise, 0
lastdayofmonth(e_d)
                                   the e_d date of the last day of the month of e_d
lastdowofmonth(M, Y, d)
                                   a synonym for lastweekdayofmonth(M,Y,d)
lastweekdayofmonth(M, Y, d)
                                   the e_d date of the last day-of-week d in month M of year Y
mdy(M, D, Y)
                                   the e_d date (days since 01 jan 1960) corresponding to M, D, Y
                                   the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) corresponding
mdyhms(M, D, Y, h, m, s)
                                   to M, D, Y, h, m, s
minutes(ms)
                                   ms/60,000
                                   the minute corresponding to date time e_{tc} (ms. since 01jan1960
mm(e_{tc})
                                   00:00:00.000)
mmC(e_{tC})
                                   the minute corresponding to date time e_{tC} (ms. with leap seconds
                                   since 01jan1960 00:00:00.000)
mofd(e_d)
                                   the e_m monthly date (months since 1960m1) containing date e_d
month(e_d)
                                   the numeric month corresponding to date e_d
monthly(s_1, s_2[, Y])
                                   the e_m monthly date (months since 1960m1) corresponding to s_1
                                   based on s_2 and Y; Y specifies topyear; see date()
msofhours(h)
                                   h \times 3,600,000
msofminutes(m)
                                   m \times 60,000
msofseconds(s)
                                   s \times 1.000
\texttt{nextbirthday}(e_{d \text{ DOB}}, e_{d}[, s_{nl}])
                                   the e_d date of the first birthday after e_d for date of birth e_{d \text{ DOB}} with
                                   s_{nl} the nonleap-year birthday for 29feb birthdates
                                   a synonym for nextweekday (e_d, d)
nextdow(e_d, d)
                                   the first leap year after year Y
nextleapyear(Y)
nextweekday(e_d, d)
                                   the e_d date of the first day-of-week d after e_d
                                   the current e_{tc} datetime
now()
```

 $\texttt{previousbirthday}(e_{d\,\text{DOB}},e_{d}[\,,s_{nl}\,])$ 

	the $e_d$ date of the birthday immediately before $e_d$ for date of birth $e_{d \text{ DOB}}$ with $s_{nl}$ the nonleap-year birthday for 29 feb birthdates
$previousdow(e_d,d)$	a synonym for previousweekday $(e_d, d)$
previousleapyear(Y)	the leap year immediately before year Y
previousweekday( $e_d$ , $d$ )	the $e_d$ date of the last day-of-week d before $e_d$
$qofd(e_d)$	the $e_q$ quarterly date (quarters since 1960q1) containing date $e_d$
$quarter(e_d)$	the numeric quarter of the year corresponding to date $e_d$
quarterly( $s_1, s_2[, Y]$ )	the $e_q$ quarterly date (quarters since 1960q1) corresponding to $s_1$ based on $s_2$ and Y; Y specifies topyear; see date()
seconds(ms)	ms/1,000
$ss(e_{tc})$	the second corresponding to date time $e_{tc}$ (ms. since 01jan1960 00:00:00.000)
$ssC(e_{tC})$	the second corresponding to date time $e_{tC}$ (ms. with leap seconds since 01jan1960 00:00:00.000)
tC(l)	convenience function to make typing dates and times in expressions easier
tc(l)	convenience function to make typing dates and times in expressions easier
td(l)	convenience function to make typing dates in expressions easier
th(l)	convenience function to make typing half-yearly dates in expressions easier
tm(l)	convenience function to make typing monthly dates in expressions easier
today()	today's $e_d$ date
tq(l)	convenience function to make typing quarterly dates in expressions easier
tw(l)	convenience function to make typing weekly dates in expressions easier
$\texttt{week}(e_d)$	the numeric week of the year corresponding to date $e_d$ , the %td encoded date (days since 01jan1960)
$\texttt{weekly}(s_1, s_2[, Y])$	the $e_w$ weekly date (weeks since 1960w1) corresponding to $s_1$ based on $s_2$ and Y; Y specifies <i>topyear</i> ; see date()
$wofd(e_d)$	the $e_w$ weekly date (weeks since 1960w1) containing date $e_d$
$year(e_d)$	the numeric year corresponding to date $e_d$
$\texttt{yearly}(s_1, s_2[, Y])$	the $e_y$ yearly date (year) corresponding to $s_1$ based on $s_2$ and $Y$ ; $Y$ specifies topyear, see date()
yh(Y,H)	the $e_h$ half-yearly date (half-years since 1960h1) corresponding to year Y, half-year H
ym(Y, M)	the $e_m$ monthly date (months since 1960m1) corresponding to year $Y$ , month $M$
$yofd(e_d)$	the $e_y$ yearly date (year) containing date $e_d$
yq(Y,Q)	the $e_q$ quarterly date (quarters since 1960q1) corresponding to year $Y$ , quarter $Q$
уw (Y, W)	the $e_w$ weekly date (weeks since 1960w1) corresponding to year Y, week W

### **Mathematical functions**

abs(x)	the absolute value of $x$
ceil(x)	the unique integer $n$ such that $n - 1 < x \le n$ ; $x$ (not ".") if $x$ is
	missing, meaning that $ceil(.a) = .a$
cloglog(x)	the complementary log-log of $x$
comb(n,k)	the combinatorial function $n!/\{k!(n-k)!\}$
digamma(x)	the digamma() function, $d\ln\Gamma(x)/dx$
$\exp(x)$	the exponential function $e^x$
expm1(x)	$e^x - 1$ with higher precision than $\exp(x) - 1$ for small values of $ x $
<pre>floor(x)</pre>	the unique integer n such that $n \le x < n + 1$ ; x (not ".") if x is missing, meaning that floor(.a) = .a
int(x)	the integer obtained by truncating x toward 0 (thus, $int(5.2) = 5$ and $int(-5.8) = -5$ ); x (not ".") if x is missing, meaning that int(.a) = .a
invcloglog(x)	the inverse of the complementary log-log function of $x$
<pre>invlogit(x)</pre>	the inverse of the logit function of $x$
ln(x)	the natural logarithm, $\ln(x)$
ln1m(x)	the natural logarithm of $1 - x$ with higher precision than $ln(1 - x)$ for small values of $ x $
ln1p(x)	the natural logarithm of $1 + x$ with higher precision than $ln(1 + x)$ for small values of $ x $
<pre>lnfactorial(n)</pre>	the natural log of $n$ factorial = $\ln(n!)$
lngamma(x)	$\ln\{\Gamma(x)\}$
log(x)	a synonym for $ln(x)$
log10(x)	the base-10 logarithm of $x$
$\log 1m(x)$	a synonym for ln1m(x)
log1p(x)	a synonym for ln1p(x)
logit(x)	the log of the odds ratio of $x$ , logit( $x$ ) = $\ln \{x/(1-x)\}$
$\max(x_1, x_2, \ldots, x_n)$	the maximum value of $x_1, x_2, \ldots, x_n$
$\min(x_1, x_2, \ldots, x_n)$	the minimum value of $x_1, x_2, \ldots, x_n$
mod(x,y)	the modulus of $x$ with respect to $y$
reldif(x,y)	the "relative" difference $ x - y /( y  + 1)$ ; 0 if both arguments are the same type of extended missing value; <i>missing</i> if only one argument is missing or if the two arguments are two different types of missing
round(x,y) or $round(x)$	of missing $x$ rounded in units of $y$ or $x$ rounded to the nearest integer if the argument $y$ is omitted; $x$ (not ".") if $x$ is missing (meaning that round(.a) = .a and that round(.a, $y$ ) = .a if $y$ is not missing) and if $y$ is missing, then "." is returned
sign(x)	the sign of $x$ : $-1$ if $x < 0, 0$ if $x = 0, 1$ if $x > 0$ , or missing if $x$ is missing
<pre>sqrt(x)</pre>	the square root of $x$
sum(x)	the running sum of $x$ , treating missing values as zero

trigamma(x)
trunc(x)

### **Matrix functions**

the second derivative of  $\mbox{lngamma}(x) = d^2 \ln \Gamma(x)/dx^2$  a synonym for  $\mbox{int}(x)$ 

cholesky(M)	the Cholesky decomposition of the matrix: if $R = \text{cholesky}(S)$ , then $RR^T = S$
coleqnumb(M,s)	the equation number of $M$ associated with column equation $s$ ; missing if the column equation cannot be found
colnfreeparms(M)	the number of free parameters in columns of $M$
colnumb(M,s)	the column number of $M$ associated with column name $s$ ; <i>missing</i> if the column cannot be found
colsof(M)	the number of columns of $M$
corr(M)	the correlation matrix of the variance matrix
$\det(M)$	the determinant of matrix $M$
diag( <i>M</i> )	the square, diagonal matrix created from the row or column vector
diag0cnt(M)	the number of zeros on the diagonal of $M$
el(s,i,j)	s[floor(i),floor(j)], the $i, j$ element of the matrix named $s$ ; missing if i or j are out of range or if matrix s does not exist
get(systemname)	a copy of Stata internal system matrix systemname
hadamard(M, N)	a matrix whose $i, j$ element is $M[i, j] \cdot N[i, j]$ (if $M$ and $N$ are not the same size, this function reports a conformability error)
I(n)	an $n \times n$ identity matrix if n is an integer; otherwise, a round $(n) \times$ round $(n)$ identity matrix
inv(M)	the inverse of the matrix $M$
invsym(M)	the inverse of $M$ if $M$ is positive definite
invvech(M)	a symmetric matrix formed by filling in the columns of the lower triangle from a row or column vector
invvecp(M)	a symmetric matrix formed by filling in the columns of the upper triangle from a row or column vector
issymmetric(M)	1 if the matrix is symmetric; otherwise, 0
J(r,c,z)	the $r \times c$ matrix containing elements $z$
matmissing(M)	1 if any elements of the matrix are missing; otherwise, 0
<pre>matuniform(r,c)</pre>	the $r \times c$ matrices containing uniformly distributed pseudorandom numbers on the interval $(0, 1)$
mreldif(X, Y)	the relative difference of X and Y, where the relative difference is defined as $\max_{i,j} \{  x_{ij} - y_{ij}  / ( y_{ij}  + 1) \}$
<pre>nullmat(matname)</pre>	use with the row-join (,) and column-join (\\) operators
roweqnumb(M,s)	the equation number of $M$ associated with row equation $s$ ; missing if the row equation cannot be found
rownfreeparms(M)	the number of free parameters in rows of $M$
rownumb(M,s)	the row number of $M$ associated with row name $s$ ; missing if the
rowsof(M)	row cannot be found the number of rows of $M$

sweep(M,i)	matrix $M$ with <i>i</i> th row/column swept
trace(M)	the trace of matrix $M$
vec(M)	a column vector formed by listing the elements of $M$ , starting with the first column and proceeding column by column
vecdiag(M)	the row vector containing the diagonal of matrix $M$
$\operatorname{vech}(M)$	a column vector formed by listing the lower triangle elements of ${\cal M}$
vecp(M)	a column vector formed by listing the upper triangle elements of ${\cal M}$

# Programming functions

$autocode(x, n, x_0, x_1)$	partitions the interval from $x_0$ to $x_1$ into <i>n</i> equal-length intervals and returns the upper bound of the interval that contains <i>x</i> or the upper bound of the first or last interval if $x < x_0$ or $x > x_1$ , respectively
byteorder()	1 if your computer stores numbers by using a hilo byte order and evaluates to 2 if your computer stores numbers by using a lohi byte
c(name)	order the value of the system or constant result c( <i>name</i> ) (see [P] creturn)
_caller()	version of the program or session that invoked the currently running program; see [P] version
$chop(x, \epsilon)$	round(x) if $abs(x - round(x)) < \epsilon$ ; otherwise, x; or x if x is missing
clip(x,a,b)	x if $a < x < b$ , b if $x \ge b$ , a if $x \le a$ , or missing if x is missing or if $a > b$ ; x if x is missing
cond(x,a,b[,c])	a if $x$ is true and nonmissing, $b$ if $x$ is false, and $c$ if $x$ is missing; $a$ if $c$ is not specified and $x$ evaluates to missing
e(name)	the value of stored result e( <i>name</i> ); see [U] <b>18.8 Accessing results</b> calculated by other programs
e(sample)	1 if the observation is in the estimation sample and 0 otherwise
epsdouble()	the machine precision of a double-precision number
epsfloat()	the machine precision of a floating-point number
fileexists(f)	1 if the file specified by $f$ exists; otherwise, 0
fileread(f)	the contents of the file specified by $f$
filereaderror(s)	0 or positive integer, said value having the interpretation of a return code
filewrite(f, s[, r])	writes the string specified by $s$ to the file specified by $f$ and returns the number of bytes in the resulting file
<pre>float(x)</pre>	the value of $x$ rounded to float precision
<pre>fmtwidth(fmtstr)</pre>	the output length of the % <i>fmt</i> contained in <i>fmtstr</i> ; <i>missing</i> if <i>fmtstr</i> does not contain a valid % <i>fmt</i>
frval()	returns values of variables stored in other frames
_frval()	programmer's version of frval()
has_eprop(name)	1 if <i>name</i> appears as a word in e(properties); otherwise, 0
$\texttt{inlist}(z, a, b, \ldots)$	1 if $z$ is a member of the remaining arguments; otherwise, 0
inrange(z,a,b)	1 if it is known that $a \le z \le b$ ; otherwise, 0

$irecode(x, x_1, \ldots, x_n)$	missing if x is missing or $x_1, \ldots, x_n$ is not weakly increasing; 0 if $x \le x_1$ ; 1 if $x_1 < x \le x_2$ ; 2 if $x_2 < x \le x_3$ ;; n if $x > x_n$
<pre>matrix(exp)</pre>	restricts name interpretation to scalars and matrices; see $scalar()$
maxbyte()	the largest value that can be stored in storage type byte
maxdouble()	the largest value that can be stored in storage type double
maxfloat()	the largest value that can be stored in storage type float
maxint()	the largest value that can be stored in storage type int
maxlong()	the largest value that can be stored in storage type long
$\min(x_1, x_2, \ldots, x_n)$	a synonym for missing $(x_1, x_2, \ldots, x_n)$
minbyte()	the smallest value that can be stored in storage type byte
mindouble()	the smallest value that can be stored in storage type double
minfloat()	the smallest value that can be stored in storage type float
minint()	the smallest value that can be stored in storage type int
minlong()	the smallest value that can be stored in storage type long
$missing(x_1, x_2, \dots, x_n)$	1 if any $x_i$ evaluates to <i>missing</i> ; otherwise, 0
r(name)	the value of the stored result r ( <i>name</i> ); see [U] <b>18.8 Accessing</b> results calculated by other programs
$recode(x, x_1, \dots, x_n)$	$\begin{array}{l} \mbox{missing if } x_1, x_2, \ldots, x_n \mbox{ is not weakly increasing; } x \mbox{ if } x \mbox{ is missing; } \\ x_1 \mbox{ if } x \leq x_1; x_2 \mbox{ if } x \leq x_2, \ldots; \mbox{ otherwise, } x_n \mbox{ if } x > x_1, x_2, \ldots, \\ x_{n-1}. \ x_i \geq . \mbox{ is interpreted as } x_i = +\infty \end{array}$
replay()	1 if the first nonblank character of local macro '0' is a comma, or if '0' is empty
return( <i>name</i> )	the value of the to-be-stored result r ( <i>name</i> ); see [P] return
s(name)	the value of stored result s ( <i>name</i> ); see [U] <b>18.8 Accessing results</b> calculated by other programs
<pre>scalar(exp)</pre>	restricts name interpretation to scalars and matrices
<pre>smallestdouble()</pre>	the smallest double-precision number greater than zero

#### **Random-number functions**

rbeta( <i>a</i> , <i>b</i> )	beta $(a,b)$ random variates, where $a$ and $b$ are the beta distribution shape parameters
<pre>rbinomial(n,p)</pre>	binomial $(n,p)$ random variates, where $n$ is the number of trials and $p$ is the success probability
rcauchy(a,b)	Cauchy $(a,b)$ random variates, where $a$ is the location parameter and $b$ is the scale parameter
rchi2(df)	$\chi^2$ , with $df$ degrees of freedom, random variates
rexponential(b)	exponential random variates with scale b
rgamma(a,b)	gamma $(a,b)$ random variates, where $a$ is the gamma shape parameter and $b$ is the scale parameter
rhypergeometric(N,K,n)	hypergeometric random variates
rigaussian(m,a)	inverse Gaussian random variates with mean $m$ and shape parameter $a$

<pre>rlaplace(m,b)</pre>	Laplace $(m,b)$ random variates with mean $m$ and scale parameter $b$
rlogistic()	logistic variates with mean 0 and standard deviation $\pi/\sqrt{3}$
<pre>rlogistic(s)</pre>	logistic variates with mean 0, scale s, and standard deviation $s\pi/\sqrt{3}$
<pre>rlogistic(m,s)</pre>	logistic variates with mean $m$ , scale $s$ , and standard deviation $s\pi/\sqrt{3}$
rnbinomial(n,p)	negative binomial random variates
rnormal()	standard normal (Gaussian) random variates, that is, variates from a normal distribution with a mean of 0 and a standard deviation of 1
rnormal(m)	normal $(m,1)$ (Gaussian) random variates, where $m$ is the mean and the standard deviation is 1
<pre>rnormal(m,s)</pre>	$\operatorname{normal}(m,s)$ (Gaussian) random variates, where $m$ is the mean and
<pre>rpoisson(m)</pre>	s is the standard deviation Poisson $(m)$ random variates, where m is the distribution mean
rt(df)	Student's $t$ random variates, where $df$ is the degrees of freedom
runiform()	uniformly distributed random variates over the interval $(0, 1)$
<pre>runiform(a,b)</pre>	uniformly distributed random variates over the interval $(a, b)$
<pre>runiformint(a,b)</pre>	uniformly distributed random integer variates on the interval $[a, b]$
<pre>rweibull(a,b)</pre>	Weibull variates with shape $a$ and scale $b$
<pre>rweibull(a,b,g)</pre>	Weibull variates with shape $a$ , scale $b$ , and location $g$
<pre>rweibullph(a,b)</pre>	Weibull (proportional hazards) variates with shape $a$ and scale $b$
<pre>rweibullph(a,b,g)</pre>	Weibull (proportional hazards) variates with shape $a$ , scale $b$ , and location $g$

### Selecting time-span functions

$tin(d_1, d_2)$	true if $d_1 \leq t \leq d_2,$ where $t$ is the time variable previously <code>tsset</code>
$\texttt{twithin}(d_1, d_2)$	true if $d_1 < t < d_2,$ where $t$ is the time variable previously $\verb+tsset$

#### **Statistical functions**

betaden(a,b,x)	the probability density of the beta distribution, where $a$ and $b$ are the shape parameters; 0 if $x < 0$ or $x > 1$
$binomial(n,k,\theta)$	the probability of observing $floor(k)$ or fewer successes in $floor(n)$ trials when the probability of a success on one trial is $\theta$ ; 0 if $k < 0$ ; or 1 if $k > n$
binomialp(n,k,p)	the probability of observing $floor(k)$ successes in $floor(n)$ trials when the probability of a success on one trial is $p$
$binomialtail(n,k,\theta)$	the probability of observing $floor(k)$ or more successes in $floor(n)$ trials when the probability of a success on one trial is $\theta$ ; 1 if $k < 0$ ; or 0 if $k > n$
$binormal(h,k,\rho)$	the joint cumulative distribution $\Phi(h,k,\rho)$ of bivariate normal with correlation $\rho$
$\operatorname{cauchy}(a,b,x)$	the cumulative Cauchy distribution with location parameter $\boldsymbol{a}$ and scale parameter $\boldsymbol{b}$

cauchyden(a,b,x)	the probability density of the Cauchy distribution with location parameter $a$ and scale parameter $b$
<pre>cauchytail(a,b,x)</pre>	the reverse cumulative (upper tail or survivor) Cauchy distribution with location parameter $a$ and scale parameter $b$
chi2(df, x)	the cumulative $\chi^2$ distribution with $df$ degrees of freedom; 0 if $x<0$
chi2den(df, x)	the probability density of the $\chi^2$ distribution with $df$ degrees of freedom; 0 if $x<0$
chi2tail(df,x)	the reverse cumulative (upper tail or survivor) $\chi^2$ distribution with $df$ degrees of freedom; 1 if $x<0$
dgammapda(a,x)	$rac{\partial P(a,x)}{\partial a}$ , where $P(a,x) = \texttt{gammap}(a,x)$ ; 0 if $x < 0$
dgammapdada(a,x)	$\frac{\partial^2 P(a,x)}{\partial a^2},$ where $P(a,x) = \texttt{gammap}(a,x);$ 0 if $x < 0$
dgammapdadx(a, x)	$\frac{\partial^2 P(a,x)}{\partial a \partial x},$ where $P(a,x) = \texttt{gammap}(a,x);$ 0 if $x < 0$
dgammapdx(a,x)	$rac{\partial P(a,x)}{\partial x}$ , where $P(a,x) = \texttt{gammap}(a,x)$ ; 0 if $x < 0$
dgammapdxdx(a,x)	$rac{\partial^2 P(a,x)}{\partial x^2},$ where $P(a,x)= \texttt{gammap}(a,x);$ 0 if $x<0$
dunnettprob( $k$ , $df$ , $x$ )	the cumulative multiple range distribution that is used in Dunnett's multiple-comparison method with k ranges and $df$ degrees of freedom; 0 if $x < 0$
exponential(b, x)	the cumulative exponential distribution with scale $b$
exponentialden(b, x)	the probability density function of the exponential distribution with scale $b$
exponentialtail(b,x)	the reverse cumulative exponential distribution with scale $b$
$F(df_1, df_2, f)$	the cumulative $F{\rm distribution}$ with $df_1$ numerator and $df_2$
	denominator degrees of freedom:
	${f F}(df_1$ , $df_2$ , $f)=\int_0^f {f Fden}(df_1$ , $df_2$ , $t)~dt;$ 0 if $f<0$
$\operatorname{Fden}(df_1, df_2, f)$	the probability density function of the F distribution with $df_1$ numerator and $df_2$ denominator degrees of freedom; 0 if $f < 0$
$Ftail(df_1, df_2, f)$	the reverse cumulative (upper tail or survivor) $F$ distribution with $df_1$ numerator and $df_2$ denominator degrees of freedom; 1 if $f < 0$
gammaden(a, b, g, x)	the probability density function of the gamma distribution; 0 if $x < g$
gammap(a, x)	the cumulative gamma distribution with shape parameter $a$ ; 0 if $x < 0$
gammaptail(a, x)	the reverse cumulative (upper tail or survivor) gamma distribution with shape parameter $a$ ; 1 if $x < 0$
hypergeometric $(N, K, n, k)$	the cumulative probability of the hypergeometric distribution
hypergeometricp( $N, K, n, k$ )	the hypergeometric probability of $k$ successes out of a sample of size $n$ , from a population of size $N$ containing $K$ elements that have the attribute of interest
ibeta(a,b,x)	the cumulative beta distribution with shape parameters $a$ and $b$ ; 0 if $x < 0$ ; or 1 if $x > 1$
ibetatail(a,b,x)	the reverse cumulative (upper tail or survivor) beta distribution with shape parameters $a$ and $b$ ; 1 if $x < 0$ ; or 0 if $x > 1$
igaussian(m,a,x)	the cumulative inverse Gaussian distribution with mean $m$ and shape parameter $a$ ; 0 if $x \le 0$

igaussianden(m,a,x)	the probability density of the inverse Gaussian distribution with mean $m$ and shape parameter $a$ ; 0 if $x \le 0$
<pre>igaussiantail(m,a,x)</pre>	the reverse cumulative (upper tail or survivor) inverse Gaussian
invbinomial(n,k,p)	distribution with mean m and shape parameter a; 1 if $x \le 0$ the inverse of the cumulative binomial; that is, $\theta$ ( $\theta$ = probability of success on one trial) such that the probability of observing floor(k) or fewer successes in floor(n) trials is p
invbinomialtail(n,k,p)	the inverse of the right cumulative binomial; that is, $\theta$ ( $\theta$ = probability of success on one trial) such that the probability of observing floor(k) or more successes in floor(n) trials is p
<pre>invcauchy(a,b,p)</pre>	the inverse of cauchy(): if cauchy( $a, b, x$ ) = $p$ , then invcauchy( $a, b, p$ ) = $x$
<pre>invcauchytail(a,b,p)</pre>	the inverse of cauchytail(): if cauchytail( $a, b, x$ ) = $p$ , then invcauchytail( $a, b, p$ ) = $x$
<pre>invchi2(df,p)</pre>	the inverse of chi2(): if chi2( $df, x$ ) = $p$ , then invchi2( $df, p$ ) = $x$
<pre>invchi2tail(df,p)</pre>	the inverse of chi2tail(): if chi2tail( $df, x$ ) = $p$ , then invchi2tail( $df, p$ ) = $x$
invdunnettprob(k, df, p)	the inverse cumulative multiple range distribution that is used in Dunnett's multiple-comparison method with $k$ ranges and $df$ degrees of freedom
invexponential(b,p)	the inverse cumulative exponential distribution with scale $b$ : if exponential $(b, x) = p$ , then inverse notation $(b, p) = x$
<pre>invexponentialtail(b,p)</pre>	the inverse reverse cumulative exponential distribution with scale $b$ : if exponentialtail( $b, x$ ) = $p$ , then invexponentialtail( $b, p$ ) = $x$
$\texttt{invF}(df_1, df_2, p)$	the inverse cumulative F distribution: if $F(df_1, df_2, f) = p$ , then invF $(df_1, df_2, p) = f$
$invFtail(df_1, df_2, p)$	the inverse reverse cumulative (upper tail or survivor) $F$ distribution: if Ftail( $df_1$ , $df_2$ , $f$ ) = $p$ , then invFtail( $df_1$ , $df_2$ , $p$ ) = $f$
<pre>invgammap(a,p)</pre>	the inverse cumulative gamma distribution: if $gammap(a, x) = p$ , then $invgammap(a, p) = x$
<pre>invgammaptail(a,p)</pre>	the inverse reverse cumulative (upper tail or survivor) gamma distribution: if gammaptail( $a, x$ ) = $p$ , then invgammaptail( $a, p$ ) = $x$
<pre>invibeta(a,b,p)</pre>	the inverse cumulative beta distribution: if $ibeta(a,b,x) = p$ , then $invibeta(a,b,p) = x$
<pre>invibetatail(a,b,p)</pre>	the inverse reverse cumulative (upper tail or survivor) beta distribution: if ibetatail( $a, b, x$ ) = $p$ , then invibetatail( $a, b, p$ ) = $x$
invigaussian(m,a,p)	the inverse of igaussian(): if igaussian $(m,a,x) = p$ , then invigaussian $(m,a,p) = x$
<pre>invigaussiantail(m,a,p)</pre>	the inverse of igaussiantail(): if igaussiantail( $m, a, x$ ) = $p$ , then invigaussiantail( $m, a, p$ ) = $x$
<pre>invlaplace(m,b,p)</pre>	the inverse of laplace(): if laplace( $m, b, x$ ) = $p$ , then invlaplace( $m, b, p$ ) = $x$

invlaplacetail(m,b,p) invlogistic(p) invlogistic(s,p)invlogistic(m,s,p)invlogistictail(p) invlogistictail(s,p) invlogistictail(m,s,p)invnbinomial(n, k, q)invnbinomialtail(n,k,q)invnchi2(df,np,p) invnchi2tail(df,np,p)  $invnF(df_1, df_2, np, p)$  $invnFtail(df_1, df_2, np, p)$ invnibeta(a, b, np, p)invnormal(p) invnt(df, np, p)invnttail(df,np,p) invpoisson(k,p)invpoissontail(k,q)invt(df, p)

invttail(df,p)

the inverse of laplacetail(): if laplacetail(m, b, x) = p, then invlaplacetail (m, b, p) = xthe inverse cumulative logistic distribution: if logistic(x) = p, then invlogistic(p) = xthe inverse cumulative logistic distribution: if logistic(s, x) = p, then invlogistic(s, p) = xthe inverse cumulative logistic distribution: if logistic(m, s, x)= p, then invlogistic(m, s, p) = xthe inverse reverse cumulative logistic distribution: if logistictail(x) = p, then invlogistictail(p) = xthe inverse reverse cumulative logistic distribution: if logistictail(s, x) = p, then invlogistictail(s, p) = xthe inverse reverse cumulative logistic distribution: if logistictail(m, s, x) = p, then invlogistictail(m,s,p) = xthe value of the negative binomial parameter, p, such that q = nbinomial(n, k, p)the value of the negative binomial parameter, p, such that q = nbinomialtail(n, k, p)the inverse cumulative noncentral  $\chi^2$  distribution: if nchi2(df, np, x) = p, then invnchi2(df, np, p) = xthe inverse reverse cumulative (upper tail or survivor) noncentral  $\chi^2$ distribution: if nchi2tail(df, np, x) = p, then invnchi2tail(df, np, p) = xthe inverse cumulative noncentral F distribution: if  $nF(df_1, df_2, np, f) = p$ , then  $invnF(df_1, df_2, np, p) = f$ the inverse reverse cumulative (upper tail or survivor) noncentral Fdistribution: if nFtail( $df_1$ ,  $df_2$ , np, f) = p, then  $invnFtail(df_1, df_2, np, p) = f$ the inverse cumulative noncentral beta distribution: if nibeta(a,b,np,x) = p, then invibeta(a,b,np,p) = xthe inverse cumulative standard normal distribution: if normal(z) = p, then invnormal(p) = zthe inverse cumulative noncentral Student's t distribution: if nt(df, np, t) = p, then invnt(df, np, p) = tthe inverse reverse cumulative (upper tail or survivor) noncentral Student's t distribution: if nttail(df, np, t) = p, then invnttail(df, np, p) = tthe Poisson mean such that the cumulative Poisson distribution evaluated at k is p: if poisson(m,k) = p, then invpoisson(k,p)= mthe Poisson mean such that the reverse cumulative Poisson distribution evaluated at k is q: if poissontail(m, k) = q, then invpoissontail(k,q) = mthe inverse cumulative Student's t distribution: if t(df, t) = p, then invt(df, p) = tthe inverse reverse cumulative (upper tail or survivor) Student's t distribution: if ttail(df, t) = p, then invttail(df, p) = t

invtukeyprob(k, df, p)	the inverse cumulative Tukey's Studentized range distribution with $k$ ranges and $df$ degrees of freedom
<pre>invweibull(a,b,p)</pre>	the inverse cumulative Weibull distribution with shape <i>a</i> and scale <i>b</i> :
	if weibull $(a,b,x) = p$ , then invweibull $(a,b,p) = x$
invweibull(a,b,g,p)	the inverse cumulative Weibull distribution with shape $a$ , scale $b$ ,
(,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	and location g: if weibull $(a, b, g, x) = p$ , then
	invweibull $(a,b,g,p) = x$
<pre>invweibullph(a,b,p)</pre>	the inverse cumulative Weibull (proportional hazards) distribution
	with shape a and scale b: if weibullph $(a, b, x) = p$ , then
	invweibullph(a,b,p) = x
invweibullph(a,b,g,p)	the inverse cumulative Weibull (proportional hazards) distribution
	with shape a, scale b, and location g: if weibullph( $a, b, g, x$ ) = p,
	then invweibullph( $a, b, g, p$ ) = $x$
invweibullphtail(a,b,p)	the inverse reverse cumulative Weibull (proportional hazards)
	distribution with shape $a$ and scale $b$ : if
	weibullphtail( $a, b, x$ ) = $p$ , then
	invweibullphtail( $a, b, p$ ) = $x$
<pre>invweibullphtail(a,b,g,p)</pre>	the inverse reverse cumulative Weibull (proportional hazards)
	distribution with shape $a$ , scale $b$ , and location $g$ : if
	weibullphtail $(a, b, g, x) = p$ , then
	invweibullphtail $(a,b,g,p) = x$
<pre>invweibulltail(a,b,p)</pre>	the inverse reverse cumulative Weibull distribution with shape $a$ and
	scale b: if weibulltail $(a, b, x) = p$ , then
<pre>invweibulltail(a,b,g,p)</pre>	invweibulltail( $a, b, p$ ) = $x$ the inverse reverse cumulative Weibull distribution with shape $a$ ,
(a, b, g, p)	scale b, and location g: if weibulltail( $a, b, g, x$ ) = p, then
	invweibulltail( $a,b,g,p$ ) = $x$
laplace(m,b,x)	the cumulative Laplace distribution with mean $m$ and scale
2492400(110,00,00)	parameter b
laplaceden(m,b,x)	the probability density of the Laplace distribution with mean $m$ and
1	scale parameter b
laplacetail(m,b,x)	the reverse cumulative (upper tail or survivor) Laplace distribution
-	with mean $m$ and scale parameter $b$
lncauchyden(a,b,x)	the natural logarithm of the density of the Cauchy distribution with
	location parameter $a$ and scale parameter $b$
lnigammaden(a,b,x)	the natural logarithm of the inverse gamma density, where $a$ is the
	shape parameter and $b$ is the scale parameter
lnigaussianden(m,a,x)	the natural logarithm of the inverse Gaussian density with mean $m$
	and shape parameter a
lniwishartden(df, V, X)	the natural logarithm of the density of the inverse Wishart
	distribution; missing if $df \le n-1$
lnlaplaceden(m,b,x)	the natural logarithm of the density of the Laplace distribution with
	mean $m$ and scale parameter $b$
lnmvnormalden(M,V,X)	the natural logarithm of the multivariate normal density
lnnormal(z)	the natural logarithm of the cumulative standard normal distribution
lnnormalden(z)	the natural logarithm of the standard normal density, $N(0,1)$
$lnnormalden(x,\sigma)$	the natural logarithm of the normal density with mean 0 and
	standard deviation $\sigma$

lnnormalden( $x, \mu, \sigma$ )	the natural logarithm of the normal density with mean $\mu$ and standard deviation $\sigma$ , $N(\mu, \sigma^2)$
lnwishartden(df,V,X)	the natural logarithm of the density of the Wishart distribution;
logistic(x)	missing if $df \le n-1$ the cumulative logistic distribution with mean 0 and standard deviation $\pi/\sqrt{3}$
<pre>logistic(s,x)</pre>	the cumulative logistic distribution with mean 0, scale s, and standard deviation $s\pi/\sqrt{3}$
logistic(m,s,x)	the cumulative logistic distribution with mean $m$ , scale $s$ , and standard deviation $s\pi/\sqrt{3}$
logisticden(x)	the density of the logistic distribution with mean 0 and standard deviation $\pi/\sqrt{3}$
<pre>logisticden(s,x)</pre>	the density of the logistic distribution with mean 0, scale s, and standard deviation $s\pi/\sqrt{3}$
logisticden(m,s,x)	the density of the logistic distribution with mean $m$ , scale $s$ , and standard deviation $s\pi/\sqrt{3}$
<pre>logistictail(x)</pre>	the reverse cumulative logistic distribution with mean 0 and standard deviation $\pi/\sqrt{3}$
<pre>logistictail(s,x)</pre>	the reverse cumulative logistic distribution with mean 0, scale s, and standard deviation $s\pi/\sqrt{3}$
logistictail(m,s,x)	the reverse cumulative logistic distribution with mean $m$ , scale $s$ , and standard deviation $s\pi/\sqrt{3}$
nbetaden(a,b,np,x)	the probability density function of the noncentral beta distribution; 0 if $x < 0$ or $x > 1$
nbinomial(n,k,p)	the cumulative probability of the negative binomial distribution
nbinomialp(n,k,p)	the negative binomial probability
nbinomialtail(n,k,p)	the reverse cumulative probability of the negative binomial distribution
nchi2(df, np, x)	the cumulative noncentral $\chi^2$ distribution; 0 if $x < 0$
nchi2den(df, np, x)	the probability density of the noncentral $\chi^2$ distribution; 0 if $x<0$
nchi2tail(df, np, x)	the reverse cumulative (upper tail or survivor) noncentral $\chi^2$ distribution; 1 if $x < 0$
$\texttt{nF}(df_1, df_2, np, f)$	the cumulative noncentral $F$ distribution with $df_1$ numerator and $df_2$ denominator degrees of freedom and noncentrality parameter $np$ ; 0 if $f < 0$
$\texttt{nFden}(df_1, df_2, np, f)$	the probability density function of the noncentral $F$ distribution with $df_1$ numerator and $df_2$ denominator degrees of freedom and noncentrality parameter $np$ ; 0 if $f < 0$
$nFtail(df_1, df_2, np, f)$	the reverse cumulative (upper tail or survivor) noncentral $F$ distribution with $df_1$ numerator and $df_2$ denominator degrees of freedom and noncentrality parameter $np$ ; 1 if $f < 0$
nibeta(a,b,np,x)	the cumulative noncentral beta distribution; 0 if $x < 0$ ; or 1 if $x > 1$
normal(z)	the cumulative standard normal distribution
normalden(z)	the standard normal density, $N(0, 1)$
normalden $(x,\sigma)$	the normal density with mean 0 and standard deviation $\sigma$
normalden( $x, \mu, \sigma$ )	the normal density with mean $\mu$ and standard deviation $\sigma, N(\mu, \sigma^2)$

npnchi2( $df, x, p$ )	the noncentrality parameter, $np$ , for noncentral $\chi^2$ : if
	nchi2(df, np, x) = p, then $npnchi2(df, x, p) = np$
$\mathtt{npnF}(df_1, df_2, f, p)$	the noncentrality parameter, $np$ , for the noncentral $F$ : if
	$nF(df_1, df_2, np, f) = p$ , then $npnF(df_1, df_2, f, p) = np$
npnt(df,t,p)	the noncentrality parameter, $np$ , for the noncentral Student's
	t distribution: if $nt(df, np, t) = p$ , then $npnt(df, t, p) = np$
nt(df, np, t)	the cumulative noncentral Student's $t$ distribution with $df$ degrees of
	freedom and noncentrality parameter np
ntden(df, np, t)	the probability density function of the noncentral Student's
	t distribution with $df$ degrees of freedom and noncentrality
	parameter <i>np</i>
nttail(df, np, t)	the reverse cumulative (upper tail or survivor) noncentral Student's
	t distribution with $df$ degrees of freedom and noncentrality
	parameter $np$
poisson(m,k)	the probability of observing $floor(k)$ or fewer outcomes that are
poissonp(m,k)	distributed as Poisson with mean $m$ the probability of observing floor( $k$ ) outcomes that are distributed
po1350mp( <i>m</i> , <i>n</i> )	as Poisson with mean $m$
poissontail(m,k)	the probability of observing $floor(k)$ or more outcomes that are
•	distributed as Poisson with mean $m$
t(df,t)	the cumulative Student's $t$ distribution with $df$ degrees of freedom
tden(df,t)	the probability density function of Student's $t$ distribution
ttail(df,t)	the reverse cumulative (upper tail or survivor) Student's $t$
<b>u</b> .	distribution; the probability $T > t$
tukeyprob(k, df, x)	the cumulative Tukey's Studentized range distribution with k ranges
	and $df$ degrees of freedom; 0 if $x < 0$
weibull( $a, b, x$ )	the cumulative Weibull distribution with shape $a$ and scale $b$
weibull( $a, b, g, x$ )	the cumulative Weibull distribution with shape a, scale b, and
	location g
weibullden $(a, b, x)$	the probability density function of the Weibull distribution with
	shape $a$ and scale $b$
weibullden( $a, b, g, x$ )	the probability density function of the Weibull distribution with
	shape $a$ , scale $b$ , and location $g$
weibullph( $a, b, x$ )	the cumulative Weibull (proportional hazards) distribution with
	shape $a$ and scale $b$
weibullph( $a, b, g, x$ )	the cumulative Weibull (proportional hazards) distribution with
	shape $a$ , scale $b$ , and location $g$
weibullphden $(a, b, x)$	the probability density function of the Weibull (proportional
	hazards) distribution with shape <i>a</i> and scale <i>b</i>
weibullphden( $a, b, g, x$ )	the probability density function of the Weibull (proportional
	hazards) distribution with shape $a$ , scale $b$ , and location $g$
weibullphtail( $a, b, x$ )	the reverse cumulative Weibull (proportional hazards) distribution
	with shape $a$ and scale $b$
weibullphtail( $a, b, g, x$ )	the reverse cumulative Weibull (proportional hazards) distribution
weibulltail( $a, b, x$ )	with shape $a$ , scale $b$ , and location $g$ the reverse cumulative Weibull distribution with shape $a$ and scale $b$
	the reverse cumulative Weibull distribution with shape $a$ and scale $b$
weibulltail( $a, b, g, x$ )	the reverse cumulative Weibull distribution with shape $a$ , scale $b$ ,
	and location $g$

# String functions

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strmatch(s_1, s_2)
                                   1 if s_1 matches the pattern s_2; otherwise, 0
strofreal(n)
                                   n converted to a string
strofreal(n,s)
                                   n converted to a string using the specified display format
strpos(s_1, s_2)
                                  the position in s_1 at which s_2 is first found, 0 if s_2 does not occur,
                                   and 1 if s_2 is empty
                                   a string with the first ASCII letter and any other letters immediately
strproper(s)
                                   following characters that are not letters capitalized; all other ASCII
                                   letters converted to lowercase
strreverse(s)
                                   the reverse of ASCII string s
strrpos(s_1, s_2)
                                   the position in s_1 at which s_2 is last found, 0 if s_2 does not occur,
                                   and 1 if s_2 is empty
strrtrim(s)
                                   s without trailing blanks (ASCII space character char (32))
strtoname(s[,p])
                                   s translated into a Stata 13 compatible name
strtrim(s)
                                   s without leading and trailing blanks (ASCII space character
                                   char(32)); equivalent to strltrim(strrtrim(s))
strupper(s)
                                   uppercase ASCII characters in string s
                                   s_1, where the first n occurrences in s_1 of s_2 have been replaced with
subinstr(s_1, s_2, s_3, n)
                                   s_3
subinword(s_1, s_2, s_3, n)
                                   s_1, where the first n occurrences in s_1 of s_2 as a word have been
                                   replaced with s_3
                                   the substring of s, starting at n_1, for a length of n_2
substr(s, n_1, n_2)
tobytes(s[,n])
                                   escaped decimal or hex digit strings of up to 200 bytes of s
uchar(n)
                                   the Unicode character corresponding to Unicode code point n or an
                                   empty string if n is beyond the Unicode code-point range
udstrlen(s)
                                   the number of display columns needed to display the Unicode string
                                   s in the Stata Results window
udsubstr(s, n_1, n_2)
                                   the Unicode substring of s, starting at character n_1, for n_2 display
                                  columns
uisdigit(s)
                                   1 if the first Unicode character in s is a Unicode decimal digit;
                                   otherwise, 0
uisletter(s)
                                   1 if the first Unicode character in s is a Unicode letter; otherwise, 0
ustrcompare(s_1, s_2[,loc])
                                  compares two Unicode strings
ustrcompareex(s<sub>1</sub>,s<sub>2</sub>,loc,st,case,cslv,norm,num,alt,fr)
                                   compares two Unicode strings
ustrfix(s[,rep])
                                  replaces each invalid UTF-8 sequence with a Unicode character
ustrfrom(s,enc,mode)
                                   converts the string s in encoding enc to a UTF-8 encoded Unicode
                                  string
ustrinvalidcnt(s)
                                  the number of invalid UTF-8 sequences in s
ustrleft(s,n)
                                   the first n Unicode characters of the Unicode string s
ustrlen(s)
                                   the number of characters in the Unicode string s
ustrlower(s[,loc])
                                  lowercase all characters of Unicode string s under the given locale
                                   loc
ustrltrim(s)
                                  removes the leading Unicode whitespace characters and blanks from
                                   the Unicode string s
                                   normalizes Unicode string s to one of the five normalization forms
ustrnormalize(s,norm)
                                   specified by norm
```

$ustrpos(s_1, s_2[, n])$	the position in $s_1$ at which $s_2$ is first found; otherwise, 0
ustrregexm(s, re[, noc])	performs a match of a regular expression and evaluates to 1 if regular
	expression $re$ is satisfied by the Unicode string $s$ ; otherwise, 0
$ustrregexra(s_1, re, s_2[, noc])$	replaces all substrings within the Unicode string $s_1$ that match $re$ with $s_2$ and returns the resulting string
$\texttt{ustrregexrf}(s_1, re, s_2[, noc])$	replaces the first substring within the Unicode string $s_1$ that matches $re$ with $s_2$ and returns the resulting string
ustrregexs(n)	subexpression $n$ from a previous ustrregexm() match
ustrreverse(s)	the reverse of Unicode string s
ustrright(s,n)	the last $n$ Unicode characters of the Unicode string $s$
$ustrrpos(s_1,s_2[,n])$	the position in $s_1$ at which $s_2$ is last found; otherwise, 0
ustrrtrim(s)	remove trailing Unicode whitespace characters and blanks from the Unicode string $s$
ustrsortkey(s[,loc])	generates a null-terminated byte array that can be used by the sort command to produce the same order as ustrcompare()
<pre>ustrsortkeyex(s,loc,st,case)</pre>	
	generates a null-terminated byte array that can be used by the sort command to produce the same order as ustrcompare()
ustrtitle(s[,loc])	a string with the first characters of Unicode words titlecased and
ustrto(s,enc,mode)	other characters lowercased converts the Unicode string $s$ in UTF-8 encoding to a string in encoding $enc$
ustrtohex(s[,n])	escaped hex digit string of $s$ up to 200 Unicode characters
ustrtoname( $s[,p]$ )	string s translated into a Stata name
ustrtrim(s)	removes leading and trailing Unicode whitespace characters and
	blanks from the Unicode string s
ustrunescape(s)	the Unicode string corresponding to the escaped sequences of $s$
ustrupper(s[,loc])	uppercase all characters in string $s$ under the given locale $loc$
ustrword(s, n[, loc])	the $n$ th Unicode word in the Unicode string $s$
ustrwordcount(s[,loc])	the number of nonempty Unicode words in the Unicode string $\boldsymbol{s}$
$usubinstr(s_1, s_2, s_3, n)$	replaces the first $n$ occurrences of the Unicode string $s_2$ with the Unicode string $s_3$ in $s_1$
$usubstr(s, n_1, n_2)$	the Unicode substring of $s$ , starting at $n_1$ , for a length of $n_2$
word(s,n)	the <i>n</i> th word in <i>s</i> ; <i>missing</i> ("") if <i>n</i> is missing
wordbreaklocale( $loc, type$ )	the most closely related locale supported by ICU from $loc$ if $type$ is 1, the actual locale where the word-boundary analysis data come from if $type$ is 2; or an empty string is returned for any other $type$
wordcount(s)	the number of words in s

# **Trigonometric functions**

acos(x)	the radian value of the arccosine of $x$
acosh(x)	the inverse hyperbolic cosine of $x$
asin(x)	the radian value of the arcsine of $x$

asinh(x)	the inverse hyperbolic sine of $x$
atan(x)	the radian value of the arctangent of $x$
atan2(y, x)	the radian value of the arctangent of $y/x$ , where the signs of the parameters $y$ and $x$ are used to determine the quadrant of the answer
atanh(x)	the inverse hyperbolic tangent of $x$
$\cos(x)$	the cosine of $x$ , where $x$ is in radians
$\cosh(x)$	the hyperbolic cosine of $x$
sin(x)	the sine of $x$ , where $x$ is in radians
$\sinh(x)$	the hyperbolic sine of $x$
$\tan(x)$	the tangent of $x$ , where $x$ is in radians
tanh(x)	the hyperbolic tangent of $x$

#### Also see

- [FN] Functions by name
  [D] egen Extensions to generate
  [D] generate Create or change contents of variable
  [M-4] Intro Categorical guide to Mata functions
- [U] 13.3 Functions

### Functions by name

abbrev(s,n)	name $s$ , abbreviated to a length of $n$
abs(x)	the absolute value of $x$
acos(x)	the radian value of the arccosine of $x$
acosh(x)	the inverse hyperbolic cosine of $x$
$\texttt{age}(e_{d \text{ DOB}}, e_{d}[, s_{nl}])$	the age in integer years on $e_d$ for date of birth $e_{d \text{ DOB}}$ with $s_{nl}$ the nonleap-year birthday for 29feb birthdates
$\texttt{age\_frac}(e_{d\texttt{DOB}},e_d[,s_{nl}])$	the age in years, including the fractional part, on $e_d$ for date of birth $e_{d{\rm DOB}}$ with $s_{nl}$ the nonleap-year birthday for 29feb birthdates
asin(x)	the radian value of the arcsine of $x$
asinh(x)	the inverse hyperbolic sine of $x$
atan(x)	the radian value of the arctangent of $x$
atan2(y, x)	the radian value of the arctangent of $y/x$ , where the signs of the parameters $y$ and $x$ are used to determine the quadrant of the answer
$\operatorname{atanh}(x)$	the inverse hyperbolic tangent of x
$autocode(x, n, x_0, x_1)$	partitions the interval from $x_0$ to $x_1$ into $n$ equal-length intervals and returns the upper bound of the interval that contains $x$ or the upper bound of the first or last interval if $x < x_0$ or $x > x_1$ , respectively
betaden(a,b,x)	the probability density of the beta distribution, where $a$ and $b$ are the shape parameters; 0 if $x < 0$ or $x > 1$
$binomial(n,k,\theta)$	the probability of observing $floor(k)$ or fewer successes in $floor(n)$ trials when the probability of a success on one trial is $\theta$ ; 0 if $k < 0$ ; or 1 if $k > n$
binomialp(n,k,p)	the probability of observing $floor(k)$ successes in $floor(n)$ trials when the probability of a success on one trial is $p$
$binomialtail(n,k,\theta)$	the probability of observing $floor(k)$ or more successes in $floor(n)$ trials when the probability of a success on one trial is $\theta$ ; 1 if $k < 0$ ; or 0 if $k > n$
$binormal(h,k,\rho)$	the joint cumulative distribution $\Phi(h,k,\rho)$ of bivariate normal with correlation $\rho$
$\texttt{birthday}(e_{d\texttt{DOB}},Y\!\big[,s_{nl}\big])$	the $e_d$ date of the birthday in year Y for date of birth $e_{d \text{ DOB}}$ with $s_{nl}$ the nonleap-year birthday for 29feb birthdates
$\texttt{bofd}("cal",e_d)$	the $\boldsymbol{e}_b$ business date corresponding to $\boldsymbol{e}_d$
byteorder()	1 if your computer stores numbers by using a hilo byte order and evaluates to 2 if your computer stores numbers by using a lohi byte order
c(name)	the value of the system or constant result c( <i>name</i> ) (see [P] creturn)
_caller()	version of the program or session that invoked the currently running program; see [P] version
cauchy(a,b,x)	the cumulative Cauchy distribution with location parameter $a$ and scale parameter $b$
cauchyden(a, b, x)	the probability density of the Cauchy distribution with location parameter $a$ and scale parameter $b$

cauchytail(a,b,x)	the reverse cumulative (upper tail or survivor) Cauchy distribution with location parameter $a$ and caula parameter $b$ .
$Cdhms(e_d, h, m, s)$	with location parameter $a$ and scale parameter $b$ the $e_{tC}$ datetime (ms. with leap seconds since 01jan1960
$Curmis(e_d,n,m,s)$	$\theta_{tC}$ date time (ins. with reap seconds since of jampion 00:00:000) corresponding to $e_d$ , $h$ , $m$ , $s$
ceil(x)	the unique integer n such that $n-1 < x \le n$ ; x (not ".") if x is
0011(2)	missing, meaning that $ceil(.a) = .a$
char(n)	the character corresponding to ASCII or extended ASCII code $n$ ; "" if
	n is not in the domain
chi2(df, x)	the cumulative $\chi^2$ distribution with $df$ degrees of freedom; 0 if
	x < 0
chi2den(df, x)	the probability density of the $\chi^2$ distribution with $df$ degrees of freedom; 0 if $x < 0$
chi2tail(df,x)	the reverse cumulative (upper tail or survivor) $\chi^2$ distribution with
	df degrees of freedom; 1 if $x < 0$
Chms(h, m, s)	the $e_{tC}$ date time (ms. with leap seconds since 01 jan 1960
	00:00:00.000) corresponding to h, m, s on 01jan1960
$chop(x, \epsilon)$	round(x) if $abs(x - round(x)) < \epsilon$ ; otherwise, x; or x if x is
	missing
cholesky(M)	the Cholesky decomposition of the matrix: if $R = \text{cholesky}(S)$ ,
	then $RR^T = S$
clip(x,a,b)	x if $a < x < b, b$ if $x \ge b, a$ if $x \le a$ , or missing if x is missing or if
	a > b; x if x is missing
$\texttt{Clock}(s_1, s_2[\ ,Y])$	the $e_{tC}$ date time (ms. with leap seconds since 01jan1960
	00:00:00.000) corresponding to $s_1$ based on $s_2$ and Y
$\texttt{clock}(s_1, s_2[\ ,Y])$	the $e_{tc}$ datetime (ms. since 01jan1960 00:00:00.000) corresponding
	to $s_1$ based on $s_2$ and Y
$Clockdiff(e_{tC1}, e_{tC2}, s_u)$	the $e_{tC}$ date time difference, rounded down to an integer, from $e_{tC1}$
$clockdiff(e_{tc1}, e_{tc2}, s_u)$	to $e_{tC2}$ in $s_u$ units of days, hours, minutes, seconds, or milliseconds the <i>c</i> datatime difference rounded down to an integer from <i>c</i> to
$c_{tc1}, c_{tc2}, s_u$	the $e_{tc}$ date time difference, rounded down to an integer, from $e_{tc1}$ to $e_{tc2}$ in $s_u$ units of days, hours, minutes, seconds, or milliseconds
$Clockdiff_frac(e_{tC1}, e_{tC2}, s_u)$	
	the $e_{tC}$ datetime difference, including the fractional part, from $e_{tC1}$
	to $e_{tC2}$ in $s_u$ units of days, hours, minutes, seconds, or milliseconds
$clockdiff_frac(e_{tc1}, e_{tc2}, s_u)$	
	$e_{tc2}$ in $s_u$ units of days, hours, minutes, seconds, or milliseconds
$\texttt{Clockpart}(e_{tC},s_u)$	the integer year, month, day, hour, minute, second, or millisecond of
	$e_{tC}$ with $s_u$ specifying which time part
$clockpart(e_{tc}, s_u)$	the integer year, month, day, hour, minute, second, or millisecond of
	$e_{tc}$ with $s_u$ specifying which time part
cloglog(x)	the complementary log-log of $x$
Cmdyhms(M, D, Y, h, m, s)	the $e_{tC}$ datetime (ms. with leap seconds since 01jan1960
	00:00:00.000) corresponding to $M, D, Y, h, m, s$
$Cofc(e_{tc})$	the $e_{tC}$ date time (ms. with leap seconds since 01jan1960
	00:00:00.000) of $e_{tc}$ (ms. without leap seconds since 01jan1960
	00:00:0000)
$\texttt{cofC}(e_{tC})$	the $e_{tc}$ date time (ms. without leap seconds since 01jan1960
	00:00:00.000) of $e_{tC}$ (ms. with leap seconds since 01jan1960
	00:00:0000)

```
Cofd(e_d)
                                     the e_{tC} datetime (ms. with leap seconds since 01 jan 1960)
                                     00:00:00.000) of date e_d at time 00:00:00.000
                                     the e_{tc} datetime (ms. since 01jan1960 00:00:00.000) of date e_d at
cofd(e_d)
                                     time 00:00:00.000
coleqnumb(M, s)
                                     the equation number of M associated with column equation s;
                                     missing if the column equation cannot be found
                                     the most closely related locale supported by ICU from loc if type is
collatorlocale(loc,type)
                                     1; the actual locale where the collation data comes from if type is 2
collatorversion(loc)
                                     the version string of a collator based on locale loc
colnfreeparms(M)
                                     the number of free parameters in columns of M
colnumb(M,s)
                                     the column number of M associated with column name s; missing if
                                     the column cannot be found
colsof(M)
                                     the number of columns of M
comb(n,k)
                                     the combinatorial function n!/\{k!(n-k)!\}
cond(x,a,b[,c])
                                     a if x is true and nonmissing, b if x is false, and c if x is missing; a if
                                     c is not specified and x evaluates to missing
\operatorname{corr}(M)
                                     the correlation matrix of the variance matrix
\cos(x)
                                     the cosine of x, where x is in radians
\cosh(x)
                                     the hyperbolic cosine of x
daily(s_1, s_2[, Y])
                                     a synonym for date(s_1, s_2[, Y])
date(s_1, s_2[, Y])
                                     the e_d date (days since 01jan1960) corresponding to s_1 based on s_2
                                     and Y
datediff(e_{d1}, e_{d2}, s_u[,s_{nl}])
                                     the difference, rounded down to an integer, from e_{d1} to e_{d2} in s_u
                                     units of days, months, or years with s_{nl} the nonleap-year
                                     anniversary for e_{d1} on 29 feb
datediff_frac(e_{d1}, e_{d2}, s_u[,s_{nl}])
                                     the difference, including the fractional part, from e_{d1} to e_{d2} in s_u
                                     units of days, months, or years with s<sub>nl</sub> the nonleap-year
                                     anniversary for e_{d1} on 29feb
                                     the integer year, month, or day of e_d with s_u specifying year, month,
datepart(e_d, s_u)
                                     or dav
day(e_d)
                                     the numeric day of the month corresponding to e_d
daysinmonth(e_d)
                                     the number of days in the month of e_d
dayssincedow(e_d, d)
                                     a synonym for dayssinceweekday (e_d, d)
dayssinceweekday(e_d, d)
                                     the number of days until e_d since previous day-of-week d
                                     a synonym for daysuntilweekday(e_d, d)
daysuntildow(e_d, d)
daysuntilweekday(e_d, d)
                                     the number of days from e_d until next day-of-week d
                                     the determinant of matrix M
\det(M)
                                     rac{\partial P(a,x)}{\partial a}, where P(a,x) = \texttt{gammap}(a,x); 0 if x < 0
dgammapda(a, x)
                                     rac{\partial^2 P(a,x)}{\partial a^2}, where P(a,x) = \texttt{gammap}(a,x); 0 if x < 0
dgammapdada(a, x)
                                     \frac{\partial^2 P(a,x)}{\partial a \partial x}, where P(a,x) = \texttt{gammap}(a,x); 0 if x < 0
dgammapdadx(a, x)
                                     \frac{\partial P(a,x)}{\partial x}, where P(a,x)=\texttt{gammap}(a,x); 0 if x<0
dgammapdx(a, x)
                                     rac{\partial^2 P(a,x)}{\partial x^2}, where P(a,x) = \texttt{gammap}(a,x); 0 if x < 0
dgammapdxdx(a, x)
```

$dhms(e_d, h, m, s)$	the $e_{tc}$ date time (ms. since 01jan1960 00:00:00.000) corresponding to $e_d$ , $h$ , $m$ , and $s$
diag( <i>M</i> )	the square, diagonal matrix created from the row or column vector $\vec{r}$
diagOcnt(M)	the number of zeros on the diagonal of $M$
digamma(x)	the digamma () function, $d \ln \Gamma(x)/dx$
dmy(D, M, Y)	the $e_d$ date (days since 01jan1960) corresponding to $D, M, Y$
$dofb(e_b, "cal")$	the $e_d$ date time corresponding to $e_b$
$dofC(e_{tC})$	the $e_d$ date (days since 01jan1960) of datetime $e_{tC}$ (ms. with leap seconds since 01jan1960 00:00:00000)
$dofc(e_{tc})$	the $e_d$ date (days since 01jan1960) of datetime $e_{tc}$ (ms. since 01jan1960 00:00:00.000)
$dofh(e_h)$	the $e_d$ date (days since 01jan1960) of the start of half-year $e_h$
$\texttt{dofm}(e_m)$	the $e_d$ date (days since 01jan1960) of the start of month $e_m$
$dofq(e_q)$	the $e_d$ date (days since 01jan1960) of the start of quarter $e_q$
$dofw(e_w)$	the $e_d$ date (days since 01jan1960) of the start of week $e_w$
$dofy(e_y)$	the $e_d$ date (days since 01jan1960) of 01jan in year $e_y$
$dow(e_d)$	the numeric day of the week corresponding to date $e_d$ ; $0 =$ Sunday, $1 =$ Monday,, $6 =$ Saturday
$doy(e_d)$	the numeric day of the year corresponding to date $e_d$
dunnettprob( $k$ , $df$ , $x$ )	the cumulative multiple range distribution that is used in Dunnett's multiple-comparison method with k ranges and $df$ degrees of freedom; 0 if $x < 0$
e(name)	the value of stored result e( <i>name</i> ); see [U] <b>18.8</b> Accessing results calculated by other programs
el( <i>s</i> , <i>i</i> , <i>j</i> )	s[floor(i), floor(j)], the $i, j$ element of the matrix named $s$ ; missing if $i$ or $j$ are out of range or if matrix $s$ does not exist
e(sample)	1 if the observation is in the estimation sample and 0 otherwise
epsdouble()	the machine precision of a double-precision number
epsfloat()	the machine precision of a floating-point number
$\exp(x)$	the exponential function $e^x$
expm1(x)	$e^x - 1$ with higher precision than $exp(x) - 1$ for small values of $ x $
exponential(b, x)	the cumulative exponential distribution with scale $b$
exponentialden(b, x)	the probability density function of the exponential distribution with scale $b$
exponentialtail(b, x)	the reverse cumulative exponential distribution with scale $b$
$F(df_1, df_2, f)$	the cumulative $F$ distribution with $df_1$ numerator and $df_2$ denominator degrees of freedom:
	F( $df_1$ , $df_2$ , $f$ ) $=\int_0^f$ Fden( $df_1$ , $df_2$ , $t$ ) $dt$ ; 0 if $f < 0$
$\mathtt{Fden}(df_1,df_2,f)$	the probability density function of the $F$ distribution with $df_1$ numerator and $df_2$ denominator degrees of freedom; 0 if $f<0$
fileexists(f)	1 if the file specified by $f$ exists; otherwise, 0
<pre>fileread(f)</pre>	the contents of the file specified by $f$
filereaderror(s)	0 or positive integer, said value having the interpretation of a return code

filewrite(f,s[,r])	writes the string specified by $s$ to the file specified by $f$ and returns the number of bytes in the resulting file
$firstdayofmonth(e_d)$	the $e_d$ date of the first day of the month of $e_d$
firstdowofmonth( $M, Y, d$ )	a synonym for firstweekdayofmonth $(M, Y, d)$
firstweekdayofmonth( $M, Y, a$	
<i>.</i>	the $e_d$ date of the first day-of-week $d$ in month $M$ of year $Y$
float(x)	the value of $x$ rounded to float precision
<pre>floor(x)</pre>	the unique integer n such that $n \le x < n + 1$ ; x (not ".") if x is missing, meaning that floor(.a) = .a
<pre>fmtwidth(fmtstr)</pre>	the output length of the % <i>fmt</i> contained in <i>fmtstr</i> ; <i>missing</i> if <i>fmtstr</i> does not contain a valid % <i>fmt</i>
frval()	returns values of variables stored in other frames
_frval()	programmer's version of frval()
$\texttt{Ftail}(df_1, df_2, f)$	the reverse cumulative (upper tail or survivor) F distribution with
	$df_1$ numerator and $df_2$ denominator degrees of freedom; 1 if $f<0$
gammaden(a, b, g, x)	the probability density function of the gamma distribution; 0 if $x < g$
gammap(a, x)	the cumulative gamma distribution with shape parameter $a$ ; 0 if $x < 0$
gammaptail(a,x)	the reverse cumulative (upper tail or survivor) gamma distribution with shape parameter $a$ ; 1 if $x < 0$
get(systemname)	a copy of Stata internal system matrix systemname
hadamard( $M, N$ )	a matrix whose $i, j$ element is $M[i, j] \cdot N[i, j]$ (if $M$ and $N$ are not the same size, this function reports a conformability error)
$halfyear(e_d)$	the numeric half of the year corresponding to date $e_d$
$halfyearly(s_1, s_2[, Y])$	the $e_h$ half-yearly date (half-years since 1960h1) corresponding to $s_1$ based on $s_2$ and Y; Y specifies <i>topyear</i> ; see date()
has_eprop(name)	1 if <i>name</i> appears as a word in e(properties); otherwise, 0
$hh(e_{tc})$	the hour corresponding to date time $e_{tc}$ (ms. since 01 jan 1960
	00:00:00000)
$\mathtt{hhC}(e_{tC})$	the hour corresponding to date time $e_{tC}$ (ms. with leap seconds since 01jan 1960 00:00:00.000)
hms(h,m,s)	the $e_{tc}$ date time (ms. since 01jan1960 00:00:00.000) corresponding to $h, m, s$ on 01jan1960
$hofd(e_d)$	the $e_h$ half-yearly date (half years since 1960h1) containing date $e_d$
hours(ms)	<i>ms</i> /3,600,000
hypergeometric( $N, K, n, k$ )	the cumulative probability of the hypergeometric distribution
hypergeometricp( $N, K, n, k$ )	the hypergeometric probability of $k$ successes out of a sample of size
	n, from a population of size $N$ containing $K$ elements that have the attribute of interest
I(n)	an $n \times n$ identity matrix if n is an integer; otherwise, a
	round( $n$ ) × round( $n$ ) identity matrix
ibeta(a,b,x)	the cumulative beta distribution with shape parameters $a$ and $b$ ; 0 if
ibetatail(a,b,x)	x < 0; or 1 if $x > 1the reverse cumulative (upper tail or survivor) beta distribution withshape parameters a and b; 1 if x < 0; or 0 if x > 1$

igaussian(m,a,x)	the cumulative inverse Gaussian distribution with mean $m$ and shape parameter $a$ ; 0 if $x \le 0$
igaussianden(m,a,x)	the probability density of the inverse Gaussian distribution with mean $m$ and shape parameter $a$ ; 0 if $x \le 0$
igaussiantail(m,a,x)	the reverse cumulative (upper tail or survivor) inverse Gaussian distribution with mean $m$ and shape parameter $a$ ; 1 if $x \le 0$
$indexnot(s_1, s_2)$	the position in ASCII string $s_1$ of the first character of $s_1$ not found in ASCII string $s_2$ , or 0 if all characters of $s_1$ are found in $s_2$
$inlist(z,a,b,\ldots)$	1 if $z$ is a member of the remaining arguments; otherwise, 0
inrange(z,a,b)	1 if it is known that $a \le z \le b$ ; otherwise, 0
int(x)	the integer obtained by truncating x toward 0 (thus, $int(5.2) = 5$ and $int(-5.8) = -5$ ); x (not ".") if x is missing, meaning that
inv( <i>M</i> )	int(.a) = .a the inverse of the matrix $M$
<pre>invbinomial(n,k,p)</pre>	the inverse of the cumulative binomial; that is, $\theta$ ( $\theta$ = probability of success on one trial) such that the probability of observing floor(k) or fewer successes in floor(n) trials is p
<pre>invbinomialtail(n,k,p)</pre>	the inverse of the right cumulative binomial; that is, $\theta$ ( $\theta$ = probability of success on one trial) such that the probability of observing floor(k) or more successes in floor(n) trials is p
invcauchy(a,b,p)	the inverse of cauchy(): if cauchy $(a, b, x) = p$ , then invcauchy $(a, b, p) = x$
<pre>invcauchytail(a,b,p)</pre>	the inverse of cauchytail(): if cauchytail( $a, b, x$ ) = $p$ , then invcauchytail( $a, b, p$ ) = $x$
<pre>invchi2(df,p)</pre>	the inverse of chi2(): if chi2( $df, x$ ) = $p$ , then invchi2( $df, p$ ) = $x$
invchi2tail(df,p)	the inverse of chi2tail(): if chi2tail( $df, x$ ) = $p$ , then invchi2tail( $df, p$ ) = $x$
<pre>invcloglog(x)</pre>	the inverse of the complementary log-log function of $x$
invdunnettprob(k, df, p)	the inverse cumulative multiple range distribution that is used in Dunnett's multiple-comparison method with $k$ ranges and $df$ degrees of freedom
invexponential(b,p)	the inverse cumulative exponential distribution with scale b: if exponential $(b, x) = p$ , then inverse netial $(b, p) = x$
<pre>invexponentialtail(b,p)</pre>	the inverse reverse cumulative exponential distribution with scale $b$ : if exponentialtail( $b, x$ ) = $p$ , then invexponentialtail( $b, p$ ) = $x$
$\texttt{invF}(df_1, df_2, p)$	the inverse cumulative F distribution: if $F(df_1, df_2, f) = p$ , then inv $F(df_1, df_2, p) = f$
$invFtail(df_1, df_2, p)$	the inverse reverse cumulative (upper tail or survivor) $F$ distribution: if Ftail( $df_1, df_2, f$ ) = $p$ , then invFtail( $df_1, df_2, p$ ) = $f$
invgammap(a,p)	the inverse cumulative gamma distribution: if gammap $(a, x) = p$ , then invgammap $(a, p) = x$
invgammaptail(a,p)	the inverse reverse cumulative (upper tail or survivor) gamma distribution: if gammaptail( $a, x$ ) = $p$ , then invgammaptail( $a, p$ )
invibeta(a,b,p)	= x the inverse cumulative beta distribution: if ibeta( $a$ , $b$ , $x$ ) $= p$ , then invibeta( $a$ , $b$ , $p$ ) $= x$

```
invibetatail(a, b, p)
invigaussian(m,a,p)
invigaussiantail(m,a,p)
invlaplace(m, b, p)
invlaplacetail(m, b, p)
invlogistic(p)
invlogistic(s,p)
invlogistic(m,s,p)
invlogistictail(p)
invlogistictail(s,p)
invlogistictail(m,s,p)
invlogit(x)
invnbinomial(n,k,q)
invnbinomialtail(n, k, q)
invnchi2(df,np,p)
invnchi2tail(df,np,p)
invnF(df_1, df_2, np, p)
invnFtail(df_1, df_2, np, p)
invnibeta(a, b, np, p)
invnormal(p)
invnt(df, np, p)
invnttail(df, np, p)
```

the inverse reverse cumulative (upper tail or survivor) beta distribution: if ibetatail(a, b, x) = p, then invibetatail(a, b, p) = xthe inverse of igaussian(): if igaussian(m,a,x) = p, then invigaussian(m,a,p) = xthe inverse of igaussiantail(): if igaussiantail(m, a, x) = p, then invigaussiantail(m,a,p) = xthe inverse of laplace(): if laplace(m, b, x) = p, then invlaplace(m, b, p) = xthe inverse of laplacetail(): if laplacetail(m, b, x) = p, then invlaplacetail(m, b, p) = xthe inverse cumulative logistic distribution: if logistic(x) = p, then invlogistic(p) = xthe inverse cumulative logistic distribution: if logistic(s, x) = p, then invlogistic(s, p) = xthe inverse cumulative logistic distribution: if logistic(m, s, x)= p, then invlogistic(m, s, p) = xthe inverse reverse cumulative logistic distribution: if logistictail(x) = p, then invlogistictail(p) = xthe inverse cumulative logistic distribution: if logistic(s, x) = p, then invlogistic(s, p) = xthe inverse cumulative logistic distribution: if logistic(m,s,x)= p, then invlogistic(m, s, p) = xthe inverse of the logit function of xthe value of the negative binomial parameter, p, such that q = nbinomial(n, k, p)the value of the negative binomial parameter, p, such that q = nbinomialtail(n, k, p)the inverse cumulative noncentral  $\chi^2$  distribution: if nchi2(df, np, x) = p, then invnchi2(df, np, p) = xthe inverse reverse cumulative (upper tail or survivor) noncentral  $\chi^2$ distribution: if nchi2tail(df, np, x) = p, then invnchi2tail(df, np, p) = xthe inverse cumulative noncentral F distribution: if  $nF(df_1, df_2, np, f) = p$ , then  $invnF(df_1, df_2, np, p) = f$ the inverse reverse cumulative (upper tail or survivor) noncentral Fdistribution: if nFtail( $df_1, df_2, np, f$ ) = p, then  $invnFtail(df_1, df_2, np, p) = f$ the inverse cumulative noncentral beta distribution: if nibeta(a,b,np,x) = p, then invibeta(a,b,np,p) = xthe inverse cumulative standard normal distribution: if normal(z)= p, then invnormal(p) = zthe inverse cumulative noncentral Student's t distribution: if nt(df, np, t) = p, then invnt(df, np, p) = tthe inverse reverse cumulative (upper tail or survivor) noncentral Student's t distribution: if nttail(df, np, t) = p, then invnttail(df, np, p) = t

invpoisson(k,p)	the Poisson mean such that the cumulative Poisson distribution evaluated at $k$ is $p$ : if poisson $(m,k) = p$ , then invpoisson $(k,p)$
invpoissontail(k,q)	m = m the Poisson mean such that the reverse cumulative Poisson distribution evaluated at k is q: if poissontail( $m, k$ ) = q, then invpoissontail( $k, q$ ) = m
invsym(M)	the inverse of M if M is positive definite
<pre>invt(df,p)</pre>	the inverse cumulative Student's t distribution: if $t(df, t) = p$ , then
0 * 1	invt(df,p) = t
invttail(df,p)	the inverse reverse cumulative (upper tail or survivor) Student's $t$ distribution: if ttail( $df, t$ ) = $p$ , then invttail( $df, p$ ) = $t$
invtukeyprob(k, df, p)	the inverse cumulative Tukey's Studentized range distribution with $k$ ranges and $df$ degrees of freedom
invvech(M)	a symmetric matrix formed by filling in the columns of the lower
	triangle from a row or column vector
invvecp(M)	a symmetric matrix formed by filling in the columns of the upper
	triangle from a row or column vector
invweibull(a,b,p)	the inverse cumulative Weibull distribution with shape a and scale b:
1	if weibull( $a,b,x$ ) = $p$ , then invweibull( $a,b,p$ ) = $x$
<pre>invweibull(a,b,g,p)</pre>	the inverse cumulative Weibull distribution with shape a, scale b,
	and location g: if weibull $(a, b, g, x) = p$ , then
	invweibull(a,b,g,p) = x
invweibullph(a, b, p)	the inverse cumulative Weibull (proportional hazards) distribution
	with shape $a$ and scale $b$ : if weibullph( $a, b, x$ ) = $p$ , then
	invweibullph(a, b, p) = x
invweibullph(a,b,g,p)	the inverse cumulative Weibull (proportional hazards) distribution
	with shape $a$ , scale $b$ , and location $g$ : if weibullph( $a$ , $b$ , $g$ , $x$ ) = $p$ ,
	then invweibullph( $a, b, g, p$ ) = $x$
invweibullphtail( $a, b, p$ )	the inverse reverse cumulative Weibull (proportional hazards)
	distribution with shape $a$ and scale $b$ : if
	weibullphtail( $a, b, x$ ) = $p$ , then
	invweibullphtail( $a, b, p$ ) = $x$
<pre>invweibullphtail(a,b,g,p)</pre>	the inverse reverse cumulative Weibull (proportional hazards)
rr(,.,.,.,.,.,.,.,.,.,.,.,.,.,.,.,.,	distribution with shape $a$ , scale $b$ , and location $g$ : if
	weibullphtail( $a, b, g, x$ ) = $p$ , then
	invweibullphtail( $a, b, g, p$ ) = $x$
invweibulltail(a,b,p)	the inverse reverse cumulative Weibull distribution with shape $a$ and
_	scale b: if weibulltail( $a, b, x$ ) = $p$ , then
	invweibulltail(a,b,p) = x
<pre>invweibulltail(a,b,g,p)</pre>	the inverse reverse cumulative Weibull distribution with shape a,
	scale b, and location g: if weibulltail( $a, b, g, x$ ) = p, then
	invweibulltail(a,b,g,p) = x
$irecode(x, x_1, \dots, x_n)$	missing if x is missing or $x_1, \ldots, x_n$ is not weakly increasing; 0 if
	$x \leq x_1;$ 1 if $x_1 < x \leq x_2;$ 2 if $x_2 < x \leq x_3; \ldots; n$ if $x > x_n$
$ t isleapsecond(e_{tC})$	1 if $e_{tC}$ is a leap second; otherwise, 0
isleapyear(Y)	1 if Y is a leap year; otherwise, 0
issymmetric(M)	1 if the matrix is symmetric; otherwise, 0

```
J(r,c,z)
                                  the r \times c matrix containing elements z
laplace(m, b, x)
                                  the cumulative Laplace distribution with mean m and scale
                                  parameter b
laplaceden(m,b,x)
                                  the probability density of the Laplace distribution with mean m and
                                  scale parameter b
laplacetail(m,b,x)
                                  the reverse cumulative (upper tail or survivor) Laplace distribution
                                  with mean m and scale parameter b
lastdayofmonth(e_d)
                                  the e_d date of the last day of the month of e_d
lastdowofmonth(M, Y, d)
                                  a synonym for lastweekdayofmonth (M, Y, d)
lastweekdayofmonth(M, Y, d)
                                  the e_d date of the last day-of-week d in month M of year Y
ln(x)
                                  the natural logarithm, \ln(x)
ln1m(x)
                                  the natural logarithm of 1 - x with higher precision than ln(1 - x)
                                  for small values of |x|
                                  the natural logarithm of 1 + x with higher precision than ln(1 + x)
ln1p(x)
                                  for small values of |x|
lncauchyden(a, b, x)
                                  the natural logarithm of the density of the Cauchy distribution with
                                  location parameter a and scale parameter b
lnfactorial(n)
                                  the natural log of n factorial = \ln(n!)
lngamma(x)
                                  \ln\{\Gamma(x)\}
lnigammaden(a, b, x)
                                  the natural logarithm of the inverse gamma density, where a is the
                                  shape parameter and b is the scale parameter
lnigaussianden(m, a, x)
                                  the natural logarithm of the inverse Gaussian density with mean m
                                  and shape parameter a
lniwishartden(df, V, X)
                                  the natural logarithm of the density of the inverse Wishart
                                  distribution; missing if df < n-1
                                  the natural logarithm of the density of the Laplace distribution with
lnlaplaceden(m, b, x)
                                  mean m and scale parameter b
lnmvnormalden(M, V, X)
                                  the natural logarithm of the multivariate normal density
lnnormal(z)
                                  the natural logarithm of the cumulative standard normal distribution
lnnormalden(z)
                                  the natural logarithm of the standard normal density, N(0, 1)
lnnormalden(x, \sigma)
                                  the natural logarithm of the normal density with mean 0 and
                                  standard deviation \sigma
                                  the natural logarithm of the normal density with mean \mu and
lnnormalden(x, \mu, \sigma)
                                  standard deviation \sigma, N(\mu, \sigma^2)
                                  the natural logarithm of the density of the Wishart distribution;
lnwishartden(df, V, X)
                                  missing if df \leq n-1
log(x)
                                  a synonym for \ln(x)
log10(x)
                                  the base-10 logarithm of x
log1m(x)
                                  a synonym for ln1m(x)
log1p(x)
                                  a synonym for ln1p(x)
logistic(x)
                                  the cumulative logistic distribution with mean 0 and standard
                                  deviation \pi/\sqrt{3}
logistic(s, x)
                                  the cumulative logistic distribution with mean 0, scale s, and
                                  standard deviation s\pi/\sqrt{3}
```

<pre>logistic(m,s,x)</pre>	the cumulative logistic distribution with mean m, scale s, and standard deviation $s\pi/\sqrt{3}$
logisticden(x)	the density of the logistic distribution with mean 0 and standard deviation $\pi/\sqrt{3}$
<pre>logisticden(s,x)</pre>	the density of the logistic distribution with mean 0, scale s, and standard deviation $s\pi/\sqrt{3}$
<pre>logisticden(m,s,x)</pre>	the density of the logistic distribution with mean m, scale s, and standard deviation $s\pi/\sqrt{3}$
logistictail(x)	the reverse cumulative logistic distribution with mean 0 and standard deviation $\pi/\sqrt{3}$
<pre>logistictail(s,x)</pre>	the reverse cumulative logistic distribution with mean 0, scale s, and standard deviation $s\pi/\sqrt{3}$
<pre>logistictail(m,s,x)</pre>	the reverse cumulative logistic distribution with mean m, scale s, and standard deviation $s\pi/\sqrt{3}$
logit(x)	the log of the odds ratio of x, logit(x) = $\ln \{x/(1-x)\}$
matmissing(M)	1 if any elements of the matrix are missing; otherwise, 0
matrix( <i>exp</i> )	restricts name interpretation to scalars and matrices; see scalar()
matuniform(r,c)	the $r \times c$ matrices containing uniformly distributed pseudorandom numbers on the interval $(0, 1)$
$\max(x_1, x_2, \ldots, x_n)$	the maximum value of $x_1, x_2, \ldots, x_n$
maxbyte()	the largest value that can be stored in storage type byte
maxdouble()	the largest value that can be stored in storage type double
maxfloat()	the largest value that can be stored in storage type float
maxint()	the largest value that can be stored in storage type int
maxlong()	the largest value that can be stored in storage type long
mdy(M, D, Y)	the $e_d$ date (days since 01jan1960) corresponding to $M, D, Y$
mdyhms(M, D, Y, h, m, s)	the $e_{tc}$ date time (ms. since 01jan1960 00:00:00.000) corresponding to $M, D, Y, h, m, s$
$\min(x_1, x_2, \dots, x_n)$	a synonym for missing $(x_1, x_2, \ldots, x_n)$
$\min(x_1, x_2, \ldots, x_n)$	the minimum value of $x_1, x_2, \ldots, x_n$
minbyte()	the smallest value that can be stored in storage type byte
mindouble()	the smallest value that can be stored in storage type double
minfloat()	the smallest value that can be stored in storage type float
minint()	the smallest value that can be stored in storage type int
minlong()	the smallest value that can be stored in storage type long
minutes(ms)	ms/60,000
missing( $x_1, x_2, \ldots, x_n$ )	1 if any $x_i$ evaluates to missing; otherwise, 0
$mm(e_{tc})$	the minute corresponding to date time $e_{tc}$ (ms. since 01jan1960 00:00:00.000)
$\mathtt{mmC}(e_{tC})$	the minute corresponding to date time $e_{tC}$ (ms. with leap seconds since 01jan1960 00:00:00.000)
mod(x,y)	the modulus of $x$ with respect to $y$
$mofd(e_d)$	the $e_m$ monthly date (months since 1960m1) containing date $e_d$

 $month(e_d)$ the numeric month corresponding to date  $e_d$ monthly( $s_1, s_2[, Y]$ ) the  $e_m$  monthly date (months since 1960m1) corresponding to  $s_1$ based on  $s_2$  and Y; Y specifies topyear; see date() mreldif(X,Y)the relative difference of X and Y, where the relative difference is defined as  $\max_{i,j} \{ |x_{ij} - y_{ij}| / (|y_{ij}| + 1) \}$ msofhours(h)  $h \times 3,600,000$ msofminutes(m) $m \times 60.000$ msofseconds(s) $s \times 1.000$ nbetaden(a, b, np, x)the probability density function of the noncentral beta distribution; 0 if x < 0 or x > 1nbinomial(n, k, p)the cumulative probability of the negative binomial distribution the negative binomial probability nbinomialp(n,k,p)nbinomialtail(n, k, p)the reverse cumulative probability of the negative binomial distribution nchi2(df, np, x)the cumulative noncentral  $\chi^2$  distribution; 0 if x < 0nchi2den(df, np, x)the probability density of the noncentral  $\chi^2$  distribution; 0 if x < 0the reverse cumulative (upper tail or survivor) noncentral  $\chi^2$ nchi2tail(df, np, x)distribution: 1 if x < 0nextbirthday( $e_{d \text{ DOB}}, e_d$ ,  $s_{nl}$ )) the  $e_d$  date of the first birthday after  $e_d$  for date of birth  $e_{d \text{ DOB}}$  with  $\boldsymbol{s}_{nl}$  the nonleap-year birthday for 29feb birthdates  $nextdow(e_d, d)$ a synonym for nextweekday  $(e_d, d)$ nextleapyear(Y)the first leap year after year Ynextweekday( $e_d$ , d) the  $e_d$  date of the first day-of-week d after  $e_d$  $nF(df_1, df_2, np, f)$ the cumulative noncentral F distribution with  $df_1$  numerator and  $df_2$  denominator degrees of freedom and noncentrality parameter np; 0 if f < 0 $nFden(df_1, df_2, np, f)$ the probability density function of the noncentral F distribution with  $df_1$  numerator and  $df_2$  denominator degrees of freedom and noncentrality parameter np; 0 if f < 0 $nFtail(df_1, df_2, np, f)$ the reverse cumulative (upper tail or survivor) noncentral Fdistribution with  $df_1$  numerator and  $df_2$  denominator degrees of freedom and noncentrality parameter np; 1 if f < 0the cumulative noncentral beta distribution; 0 if x < 0; or 1 if x > 1nibeta(a, b, np, x)the cumulative standard normal distribution normal(z)normalden(z)the standard normal density, N(0, 1)normalden( $x, \sigma$ ) the normal density with mean 0 and standard deviation  $\sigma$ normalden( $x, \mu, \sigma$ ) the normal density with mean  $\mu$  and standard deviation  $\sigma$ ,  $N(\mu, \sigma^2)$ now() the current  $e_{tc}$  datetime npnchi2(df, x, p)the noncentrality parameter, np, for noncentral  $\chi^2$ : if nchi2(df, np, x) = p, then npnchi2(df, x, p) = np $npnF(df_1, df_2, f, p)$ the noncentrality parameter, np, for the noncentral F: if  $nF(df_1, df_2, np, f) = p$ , then  $npnF(df_1, df_2, f, p) = np$ npnt(df, t, p)the noncentrality parameter, np, for the noncentral Student's t distribution: if nt(df, np, t) = p, then npnt(df, t, p) = np

nt(df, np, t)	the cumulative noncentral Student's $t$ distribution with $df$ degrees of freedom and noncentrality parameter $np$
ntden(df, np, t)	the probability density function of the noncentral Student's $t$ distribution with $df$ degrees of freedom and noncentrality
	parameter np
nttail(df, np, t)	the reverse cumulative (upper tail or survivor) noncentral Student's
	t distribution with $df$ degrees of freedom and noncentrality
<pre>nullmat(matname)</pre>	parameter $np$ use with the row-join (,) and column-join (\\) operators
plural(n,s)	the plural of s if $n \neq \pm 1$
plural $(n, s_1, s_2)$	the plural of $s_1$ , as modified by or replaced with $s_2$ , if $n \neq \pm 1$
poisson $(m,k)$	the probability of observing floor $(k)$ or fewer outcomes that are
	distributed as Poisson with mean $m$
poissonp(m,k)	the probability of observing $floor(k)$ outcomes that are distributed
	as Poisson with mean $m$
poissontail(m,k)	the probability of observing $floor(k)$ or more outcomes that are distributed as Poisson with mean $m$
previous birthday ( $e_{d \text{ DOB}}$ , $e_d$ ] ,	
providuobil blady $(e_{d \text{ DOB}}, e_{d}]$ ,	the $e_d$ date of the birthday immediately before $e_d$ for date of birth
	$e_{d \text{ DOB}}$ with $s_{nl}$ the nonleap-year birthday for 29 feb birthdates
$previousdow(e_d,d)$	a synonym for previousweekday ( $e_d$ , $d$ )
previousleapyear(Y)	the leap year immediately before year $Y$
${\tt previousweekday}(e_d$ , $d)$	the $e_d$ date of the last day-of-week $d$ before $e_d$
$qofd(e_d)$	the $e_q$ quarterly date (quarters since 1960q1) containing date $e_d$
$quarter(e_d)$	the numeric quarter of the year corresponding to date $e_d$
quarterly( $s_1, s_2[, Y]$ )	the $e_q$ quarterly date (quarters since 1960q1) corresponding to $s_1$
	based on $s_2$ and Y; Y specifies topyear; see date()
r(name)	the value of the stored result r (name); see [U] 18.8 Accessing
	results calculated by other programs
rbeta(a,b)	beta $(a,b)$ random variates, where $a$ and $b$ are the beta distribution
<pre>rbinomial(n,p)</pre>	shape parameters binomial $(n,p)$ random variates, where n is the number of trials and p
ibinomiai( <i>n</i> , <i>p</i> )	is the success probability
rcauchy(a,b)	Cauchy $(a,b)$ random variates, where $a$ is the location parameter and
	b is the scale parameter
rchi2(df)	$\chi^2$ , with $df$ degrees of freedom, random variates
$recode(x, x_1, \ldots, x_n)$	missing if $x_1, x_2, \ldots, x_n$ is not weakly increasing; x if x is missing;
	$x_1$ if $x \le x_1$ ; $x_2$ if $x \le x_2$ ,; otherwise, $x_n$ if $x > x_1, x_2,,$
- ( )	$x_{n-1}$ . $x_i \ge .$ is interpreted as $x_i = +\infty$
real(s)	s converted to numeric or missing
regexcapture(n)	<pre>subexpression n from a previous regerm() or regermatch()</pre>
regexcapturenamed(grp)	match subexpression corresponding to matching group named $grp$ in
2 - 6 Shoup our onamou (g, p)	regular expression from a previous regexm() or regexmatch()
	match
<pre>regexm(s,re)</pre>	a match of a regular expression, which evaluates to 1 if regular
	expression $re$ is satisfied by the ASCII string $s$ ; otherwise, 0

regermatch(s, re[, noc[, std[,	
	a match of a regular expression, which evaluates to 1 if regular
	expression $re$ is satisfied by the ASCII string $s$ ; otherwise, 0
$regexr(s_1, re, s_2)$	replaces the first substring within ASCII string $s_1$ that matches $re$ with ASCII string $s_2$ and returns the resulting string
regexreplace( $s_1$ , $re$ , $s_2$ [, $noc$ ]	, fmt[, std[, nlalt]]])
	replaces the first substring within ASCII string $s_1$ that matches $re$
	with ASCII string $s_2$ and returns the resulting string
regexreplaceall( $s_1$ , $re$ , $s_2$ [, $re$	
	replaces all substrings within ASCII string $s_1$ that match $re$ with
	ASCII string $s_2$ and returns the resulting string
regexs(n)	subexpression $n$ from a previous regexm() or regexmatch() match, where $0 \le n < 10$
reldif(x,y)	the "relative" difference $ x - y /( y  + 1)$ ; 0 if both arguments are
	the same type of extended missing value; missing if only one
	argument is missing or if the two arguments are two different types of <i>missing</i>
replay()	1 if the first nonblank character of local macro '0' is a comma, or if '0' is empty
return( <i>name</i> )	the value of the to-be-stored result r ( <i>name</i> ); see [P] return
rexponential(b)	exponential random variates with scale <i>b</i>
rgamma(a,b)	gamma $(a,b)$ random variates, where $a$ is the gamma shape parameter and $b$ is the scale parameter
rhypergeometric(N, K, n)	hypergeometric random variates
rigaussian(m,a)	inverse Gaussian random variates with mean $m$ and shape
iigaussian(m,u)	parameter a
rlaplace(m,b)	Laplace $(m,b)$ random variates with mean $m$ and scale parameter $b$
rlogistic()	logistic variates with mean 0 and standard deviation $\pi/\sqrt{3}$
<pre>rlogistic(s)</pre>	logistic variates with mean 0, scale s, and standard deviation $s\pi/\sqrt{3}$
<pre>rlogistic(m,s)</pre>	logistic variates with mean $m$ , scale $s$ , and standard deviation
-	$s\pi/\sqrt{3}$
rnbinomial(n,p)	negative binomial random variates
rnormal()	standard normal (Gaussian) random variates, that is, variates from a
<pre>rnormal(m)</pre>	normal distribution with a mean of 0 and a standard deviation of 1 $\frac{1}{10000000000000000000000000000000000$
rnormal( <i>m</i> )	normal $(m,1)$ (Gaussian) random variates, where $m$ is the mean and the standard deviation is 1
<pre>rnormal(m,s)</pre>	normal(m,s) (Gaussian) random variates, where $m$ is the mean and
round(x,y) or $round(x)$	s is the standard deviation $x$ rounded in units of $y$ or $x$ rounded to the nearest integer if the
	argument y is omitted; $x \pmod{"."}$ if x is missing (meaning that round (.a) = .a and that round (.a, y) = .a if y is not missing)
	and if $y$ is missing, then "." is returned
roweqnumb(M,s)	the equation number of $M$ associated with row equation $s$ ; missing if
-	the row equation cannot be found
rownfreeparms(M)	the number of free parameters in rows of $M$
rownumb(M,s)	the row number of $M$ associated with row name $s$ ; missing if the
	row cannot be found

rowsof(M)	the number of rows of $M$
rpoisson(m)	Poisson(m) random variates, where $m$ is the distribution mean
rt(df)	Student's $t$ random variates, where $df$ is the degrees of freedom
<pre>runiform()</pre>	uniformly distributed random variates over the interval $(0, 1)$
runiform(a,b)	uniformly distributed random variates over the interval $(a, b)$
runiformint(a, b)	uniformly distributed random integer variates on the interval $[a, b]$
<pre>rweibull(a,b)</pre>	Weibull variates with shape $a$ and scale $b$
<pre>rweibull(a,b,g)</pre>	Weibull variates with shape $a$ , scale $b$ , and location $g$
<pre>rweibullph(a,b)</pre>	Weibull (proportional hazards) variates with shape $a$ and scale $b$
rweibullph(a,b,g)	Weibull (proportional hazards) variates with shape $a$ , scale $b$ , and location $g$
s(name)	the value of stored result s ( <i>name</i> ); see [U] <b>18.8 Accessing results</b> calculated by other programs
<pre>scalar(exp)</pre>	restricts name interpretation to scalars and matrices
seconds(ms)	ms/1,000
sign(x)	the sign of $x$ : $-1$ if $x < 0, 0$ if $x = 0, 1$ if $x > 0$ , or missing if $x$ is missing
$\sin(x)$	the sine of $x$ , where $x$ is in radians
$\sinh(x)$	the hyperbolic sine of $x$
<pre>smallestdouble()</pre>	the smallest double-precision number greater than zero
<pre>soundex(s)</pre>	the soundex code for a string, s
$soundex_nara(s)$	the US Census soundex code for a string, $s$
sqrt(x)	the square root of $x$
$ss(e_{tc})$	the second corresponding to date time $e_{tc}\ ({\rm ms.\ since\ 01jan1960\ 00:00:00.000})$
$ssC(e_{tC})$	the second corresponding to date time $e_{tC}$ (ms. with leap seconds since 01jan 1960 00:00:00.000)
$strcat(s_1, s_2)$	there is no strcat() function; instead the addition operator is used to concatenate strings
$strdup(s_1,n)$	there is no strdup() function; instead the multiplication operator is used to create multiple copies of strings
<pre>string(n)</pre>	a synonym for $strofreal(n)$
string(n,s)	a synonym for $strofreal(n,s)$
<pre>stritrim(s)</pre>	s with multiple, consecutive internal blanks (ASCII space character char (32)) collapsed to one blank
<pre>strlen(s)</pre>	the number of characters in ASCII $s$ or length in bytes
<pre>strlower(s)</pre>	lowercase ASCII characters in string s
<pre>strltrim(s)</pre>	s without leading blanks (ASCII space character char(32))
$\mathtt{strmatch}(s_1, s_2)$	1 if $s_1$ matches the pattern $s_2$ ; otherwise, 0
<pre>strofreal(n)</pre>	n converted to a string
<pre>strofreal(n,s)</pre>	n converted to a string using the specified display format
$strpos(s_1, s_2)$	the position in $s_1$ at which $s_2$ is first found, 0 if $s_2$ does not occur, and 1 if $s_2$ is empty

```
a string with the first ASCII letter and any other letters immediately
strproper(s)
                                    following characters that are not letters capitalized; all other ASCII
                                    letters converted to lowercase
strreverse(s)
                                    the reverse of ASCII string s
                                   the position in s_1 at which s_2 is last found, 0 if s_2 does not occur,
strrpos(s_1, s_2)
                                    and 1 if s_2 is empty
strrtrim(s)
                                    s without trailing blanks (ASCII space character char (32))
strtoname(s[,p])
                                    s translated into a Stata 13 compatible name
strtrim(s)
                                    s without leading and trailing blanks (ASCII space character
                                    char(32)); equivalent to strltrim(strrtrim(s))
strupper(s)
                                    uppercase ASCII characters in string s
                                   \boldsymbol{s}_1, where the first n occurrences in \boldsymbol{s}_1 of \boldsymbol{s}_2 have been replaced with
subinstr(s_1, s_2, s_3, n)
                                    s_3
subinword(s_1, s_2, s_3, n)
                                    s_1, where the first n occurrences in s_1 of s_2 as a word have been
                                   replaced with s_3
substr(s, n_1, n_2)
                                    the substring of s, starting at n_1, for a length of n_2
sum(x)
                                   the running sum of x, treating missing values as zero
                                   matrix M with ith row/column swept
sweep(M,i)
t(df,t)
                                    the cumulative Student's t distribution with df degrees of freedom
\tan(x)
                                   the tangent of x, where x is in radians
tanh(x)
                                    the hyperbolic tangent of x
tC(l)
                                    convenience function to make typing dates and times in expressions
                                    easier
tc(l)
                                   convenience function to make typing dates and times in expressions
                                    easier
td(l)
                                    convenience function to make typing dates in expressions easier
tden(df,t)
                                   the probability density function of Student's t distribution
th(l)
                                    convenience function to make typing half-yearly dates in
                                    expressions easier
tin(d_1, d_2)
                                    true if d_1 \leq t \leq d_2, where t is the time variable previously tsset
tm(l)
                                    convenience function to make typing monthly dates in expressions
                                    easier
tobytes(s[,n])
                                   escaped decimal or hex digit strings of up to 200 bytes of s
today()
                                   today's e_d date
tq(l)
                                   convenience function to make typing quarterly dates in expressions
                                   easier
                                   the trace of matrix M
trace(M)
                                   the second derivative of \ln \text{gamma}(x) = d^2 \ln \Gamma(x) / dx^2
trigamma(x)
trunc(x)
                                    a synonym for int(x)
ttail(df,t)
                                    the reverse cumulative (upper tail or survivor) Student's t
                                    distribution; the probability T > t
                                    the cumulative Tukey's Studentized range distribution with k ranges
tukeyprob(k, df, x)
                                    and df degrees of freedom; 0 if x < 0
tw(l)
                                    convenience function to make typing weekly dates in expressions
                                    easier
```

$\texttt{twithin}(d_1, d_2)$	true if $d_1 < t < d_2$ , where t is the time variable previously tsset
uchar(n)	the Unicode character corresponding to Unicode code point $n$ or an empty string if $n$ is beyond the Unicode code-point range
udstrlen(s)	the number of display columns needed to display the Unicode string <i>s</i> in the Stata Results window
$udsubstr(s, n_1, n_2)$	the Unicode substring of $s$ , starting at character $n_1$ , for $n_2$ display columns
uisdigit(s)	1 if the first Unicode character in $s$ is a Unicode decimal digit; otherwise, 0
uisletter(s)	1 if the first Unicode character in $s$ is a Unicode letter; otherwise, 0
$ustrcompare(s_1, s_2[, loc])$	compares two Unicode strings
$ustrcompareex(s_1, s_2, loc, st, c)$	case, cslv, norm, num, alt, fr) compares two Unicode strings
<pre>ustrfix(s[,rep])</pre>	replaces each invalid UTF-8 sequence with a Unicode character
ustrfrom(s,enc,mode)	converts the string $s$ in encoding $enc$ to a UTF-8 encoded Unicode string
ustrinvalidcnt(s)	the number of invalid UTF-8 sequences in s
ustrleft(s,n)	the first $n$ Unicode characters of the Unicode string $s$
ustrlen(s)	the number of characters in the Unicode string $s$
ustrlower(s[,loc])	lowercase all characters of Unicode string <i>s</i> under the given locale <i>loc</i>
ustrltrim(s)	removes the leading Unicode whitespace characters and blanks from the Unicode string $\boldsymbol{s}$
<pre>ustrnormalize(s,norm)</pre>	normalizes Unicode string $s$ to one of the five normalization forms specified by $norm$
$ustrpos(s_1,s_2[,n])$	the position in $s_1$ at which $s_2$ is first found; otherwise, 0
ustrregexm(s, re[, noc])	performs a match of a regular expression and evaluates to 1 if regular expression $re$ is satisfied by the Unicode string $s$ ; otherwise, 0
$ustrregexra(s_1, re, s_2[, noc])$	replaces all substrings within the Unicode string $s_1$ that match $re$ with $s_2$ and returns the resulting string
$ustrregexrf(s_1, re, s_2[, noc])$	replaces the first substring within the Unicode string $s_1$ that matches $re$ with $s_2$ and returns the resulting string
ustrregexs(n)	subexpression $n$ from a previous ustrregerm() match
ustrreverse(s)	the reverse of Unicode string s
ustrright(s,n)	the last $n$ Unicode characters of the Unicode string $s$
$ustrrpos(s_1, s_2[, n])$	the position in $s_1$ at which $s_2$ is last found; otherwise, 0
ustrrtrim(s)	remove trailing Unicode whitespace characters and blanks from the Unicode string $\boldsymbol{s}$
ustrsortkey(s[,loc])	generates a null-terminated byte array that can be used by the sort command to produce the same order as ustrcompare()
ustrsortkeyex( <i>s</i> , <i>loc</i> , <i>st</i> , <i>case</i> )	
ustrtitle(s[,loc])	a string with the first characters of Unicode words titlecased and other characters lowercased

```
ustrto(s,enc,mode)
                                  converts the Unicode string s in UTF-8 encoding to a string in
                                  encoding enc
ustrtohex(s[,n])
                                  escaped hex digit string of s up to 200 Unicode characters
ustrtoname(s[,p])
                                  string s translated into a Stata name
ustrtrim(s)
                                  removes leading and trailing Unicode whitespace characters and
                                  blanks from the Unicode string s
ustrunescape(s)
                                  the Unicode string corresponding to the escaped sequences of s
ustrupper(s[,loc])
                                  uppercase all characters in string s under the given locale loc
ustrword(s,n[,loc])
                                  the nth Unicode word in the Unicode string s
ustrwordcount(s[,loc])
                                  the number of nonempty Unicode words in the Unicode string s
usubinstr(s_1, s_2, s_3, n)
                                  replaces the first n occurrences of the Unicode string s_2 with the
                                  Unicode string s_3 in s_1
usubstr(s, n_1, n_2)
                                  the Unicode substring of s, starting at n_1, for a length of n_2
vec(M)
                                  a column vector formed by listing the elements of M, starting with
                                  the first column and proceeding column by column
vecdiag(M)
                                  the row vector containing the diagonal of matrix M
                                  a column vector formed by listing the lower triangle elements of M
vech(M)
vecp(M)
                                  a column vector formed by listing the upper triangle elements of M
week(e_d)
                                  the numeric week of the year corresponding to date e_d, the %td
                                  encoded date (days since 01jan1960)
                                  the e_w weekly date (weeks since 1960w1) corresponding to s_1 based
weekly(s_1, s_2[, Y])
                                  on s<sub>2</sub> and Y; Y specifies topyear; see date()
weibull(a, b, x)
                                  the cumulative Weibull distribution with shape a and scale b
weibull(a, b, q, x)
                                  the cumulative Weibull distribution with shape a, scale b, and
                                  location q
                                  the probability density function of the Weibull distribution with
weibullden(a, b, x)
                                  shape a and scale b
weibullden(a, b, g, x)
                                  the probability density function of the Weibull distribution with
                                  shape a, scale b, and location g
weibullph(a, b, x)
                                  the cumulative Weibull (proportional hazards) distribution with
                                  shape a and scale b
weibullph(a, b, g, x)
                                  the cumulative Weibull (proportional hazards) distribution with
                                  shape a, scale b, and location g
                                  the probability density function of the Weibull (proportional
weibullphden(a, b, x)
                                  hazards) distribution with shape a and scale b
                                  the probability density function of the Weibull (proportional
weibullphden(a, b, g, x)
                                  hazards) distribution with shape a, scale b, and location q
weibullphtail(a, b, x)
                                  the reverse cumulative Weibull (proportional hazards) distribution
                                  with shape a and scale b
weibullphtail(a, b, g, x)
                                  the reverse cumulative Weibull (proportional hazards) distribution
                                  with shape a, scale b, and location q
weibulltail(a, b, x)
                                  the reverse cumulative Weibull distribution with shape a and scale b
weibulltail(a, b, q, x)
                                  the reverse cumulative Weibull distribution with shape a, scale b,
                                  and location q
wofd(e_d)
                                  the e_w weekly date (weeks since 1960w1) containing date e_d
```

word(s,n)	the <i>n</i> th word in <i>s</i> ; <i>missing</i> ("") if <i>n</i> is missing
<pre>wordbreaklocale(loc,type)</pre>	the most closely related locale supported by ICU from $loc$ if $type$ is 1, the actual locale where the word-boundary analysis data come from if $type$ is 2; or an empty string is returned for any other $type$
wordcount(s)	the number of words in s
$year(e_d)$	the numeric year corresponding to date $e_d$
$\texttt{yearly}(s_1, s_2\big[, Y\big])$	the $e_y$ yearly date (year) corresponding to $s_1$ based on $s_2$ and Y; Y specifies topyear; see date()
yh(Y,H)	the $e_h$ half-yearly date (half-years since 1960h1) corresponding to year Y, half-year H
ym(Y, M)	the $e_m$ monthly date (months since 1960m1) corresponding to year $Y$ , month $M$
$yofd(e_d)$	the $e_y$ yearly date (year) containing date $e_d$
yq(Y,Q)	the $e_q$ quarterly date (quarters since 1960q1) corresponding to year $Y$ , quarter $Q$
yw(Y,W)	the $e_w$ weekly date (weeks since 1960w1) corresponding to year Y, week W

# Also see

- [FN] Functions by category
- [D] egen Extensions to generate
- [D] generate Create or change contents of variable
- [M-4] Intro Categorical guide to Mata functions
- [U] 13.3 Functions

# Date and time functions

Contents
References

Functions Also see

Remarks and examples Methods and formulas

## Contents

$\texttt{age}(e_{d\text{\tiny DOB}},e_{d}[,s_{nl}])$	the age in integer years on $e_d$ for date of birth $e_{d{\rm DOB}}$ with $s_{nl}$ the nonleap-year birthday for 29feb birthdates
$\texttt{age\_frac}(e_{d\texttt{DOB}},e_d\big[,s_{nl}\big])$	the age in years, including the fractional part, on $e_d$ for date of birth $e_{d\rm DOB}$ with $s_{nl}$ the nonleap-year birthday for 29feb birthdates
$\texttt{birthday}(e_{d\texttt{DOB}}, Y\!\big[, s_{nl}\big])$	the $e_d$ date of the birthday in year $Y$ for date of birth $e_{d{\rm DOB}}$ with $s_{nl}$ the nonleap-year birthday for 29feb birthdates
$\texttt{bofd}("cal",e_d)$	the $e_b$ business date corresponding to $e_d$
$Cdhms(e_d, h, m, s)$	the $e_{tC}$ date time (ms. with leap seconds since 01jan1960 00:00:00.000) corresponding to $e_d$ , $h$ , $m$ , $s$
Chms(h,m,s)	the $e_{tC}$ date time (ms. with leap seconds since 01jan1960 00:00:00.000) corresponding to $h, m, s$ on 01jan1960
$\texttt{Clock}(s_1, s_2[\text{,}Y])$	the $e_{tC}$ date time (ms. with leap seconds since 01jan1960 00:00:00.000) corresponding to $s_1$ based on $s_2$ and $Y$
$\texttt{clock}(s_1, s_2[\ \textbf{,} Y])$	the $e_{tc}$ date time (ms. since 01jan1960 00:00:00.000) corresponding to $s_1$ based on $s_2$ and $Y$
$\texttt{Clockdiff}(e_{tC1}, e_{tC2}, s_u)$	the $e_{tC}$ datetime difference, rounded down to an integer, from $e_{tC1}$ to $e_{tC2}$ in $s_u$ units of days, hours, minutes, seconds, or milliseconds
$\texttt{clockdiff}(e_{tc1}, e_{tc2}, s_u)$	the $e_{tc}$ date time difference, rounded down to an integer, from $e_{tc1}$ to $e_{tc2}$ in $s_u$ units of days, hours, minutes, seconds, or milliseconds
$Clockdiff_frac(e_{tC1}, e_{tC2}, s_u)$	
	the $e_{tC}$ date time difference, including the fractional part, from $e_{tC1}$ to $e_{tC2}$ in $s_u$ units of days, hours, minutes, seconds, or milliseconds
$clockdiff_frac(e_{tc1}, e_{tc2}, s_u)$	
	the $e_{tc}$ date time difference, including the fractional part, from $e_{tc1}$ to $e_{tc2}$ in $s_u$ units of days, hours, minutes, seconds, or milliseconds
$Clockpart(e_{tC}, s_u)$	the integer year, month, day, hour, minute, second, or millisecond of $e_{tC}$ with $s_u$ specifying which time part
$\texttt{clockpart}(e_{tc}, s_u)$	the integer year, month, day, hour, minute, second, or millisecond of $e_{tc}$ with $s_u$ specifying which time part
Cmdyhms(M, D, Y, h, m, s)	the $e_{tC}$ datetime (ms. with leap seconds since 01jan1960 00:00:00000) corresponding to $M$ , $D$ , $Y$ , $h$ , $m$ , $s$
$\operatorname{Cofc}(e_{tc})$	the $e_{tC}$ date time (ms. with leap seconds since 01jan1960 00:00:00.000) of $e_{tc}$ (ms. without leap seconds since 01jan1960 00:00:00.000)
$\texttt{cofC}(e_{tC})$	the $e_{tc}$ date time (ms. without leap seconds since 01jan1960 00:00:00.000) of $e_{tC}$ (ms. with leap seconds since 01jan1960 00:00:00.000)
$\operatorname{Cofd}(e_d)$	the $e_{tC}$ date time (ms. with leap seconds since 01jan1960 00:00:00.000) of date $e_d$ at time 00:00:00.000

$cofd(e_d)$	the $e_{tc}$ date time (ms. since 01jan1960 00:00:0000) of date $e_d$ at
$\texttt{daily}(s_1, s_2[, Y])$	time 00:00:00.000 a synonym for date $(s_1, s_2[, Y])$
date( $s_1, s_2[, Y]$ )	the $e_d$ date (days since 01jan1960) corresponding to $s_1$ based on $s_2$
$uate(s_1, s_2[, 1])$	and $Y$
$\texttt{datediff}(e_{d1},e_{d2},s_u[,s_{nl}])$	the difference, rounded down to an integer, from $e_{d1}$ to $e_{d2}$ in $s_u$ units of days, months, or years with $s_{nl}$ the nonleap-year
	anniversary for $e_{d1}$ on 29feb
datediff_frac( $e_{d1}$ , $e_{d2}$ , $s_u$ [, $s$	
	the difference, including the fractional part, from $e_{d1}$ to $e_{d2}$ in $s_u$
	units of days, months, or years with $s_{nl}$ the nonleap-year
	anniversary for $e_{d1}$ on 29feb
$datepart(e_d, s_u)$	the integer year, month, or day of $e_d$ with $s_u$ specifying year, month, or day
$day(e_d)$	the numeric day of the month corresponding to $e_d$
daysinmonth( $e_d$ )	the number of days in the month of $e_d$
dayssincedow( $e_d$ , $d$ )	a synonym for dayssinceweekday $(e_d, d)$
dayssinceweekday( $e_d$ , $d$ )	the number of days until $e_d$ since previous day-of-week $d$
daysuntildow $(e_d, d)$	a synonym for daysuntilweekday $(e_d, d)$
daysuntilweekday $(e_d, d)$	
	the number of days from $e_d$ until next day-of-week d the $e_d$ datatime (mg since 01 in 1960 00:00:00 000) corresponding
$dhms(e_d,h,m,s)$	the $e_{tc}$ date time (ms. since 01jan1960 00:00:00.000) corresponding to $e_d$ , $h$ , $m$ , and $s$
dmy(D, M, Y)	the $e_d$ date (days since 01jan1960) corresponding to $D, M, Y$
$\texttt{dofb}(e_b,\texttt{"}cal")$	the $e_d$ date time corresponding to $e_b$
$\texttt{dofC}(e_{tC})$	the $e_d$ date (days since 01jan1960) of datetime $e_{tC}$ (ms. with leap seconds since 01jan1960 00:00:00.000)
$dofc(e_{tc})$	the $e_d$ date (days since 01jan1960) of datetime $e_{tc}$ (ms. since 01jan1960 00:00:00.000)
$dofh(e_h)$	the $e_d$ date (days since 01jan1960) of the start of half-year $e_h$
$\texttt{dofm}(e_m)$	the $e_d$ date (days since 01jan1960) of the start of month $e_m$
$dofq(e_a)$	the $e_d$ date (days since 01jan1960) of the start of quarter $e_q$
$dofw(e_w)$	the $e_d$ date (days since 01jan1960) of the start of week $e_w$
$dofy(e_y)$	the $e_d$ date (days since 01jan1960) of 01jan in year $e_y$
$dow(e_d)$	the numeric day of the week corresponding to date $e_d$ ; 0 = Sunday,
	$1 = Monday, \dots, 6 = Saturday$
$doy(e_d)$	the numeric day of the year corresponding to date $e_d$
$firstdayofmonth(e_d)$	the $\boldsymbol{e}_d$ date of the first day of the month of $\boldsymbol{e}_d$
firstdowofmonth(M,Y,d)	a synonym for firstweekdayofmonth $(M, Y, d)$
firstweekdayofmonth(M,Y,a)	
	the $e_d$ date of the first day-of-week $d$ in month $M$ of year $Y$
$halfyear(e_d)$	the numeric half of the year corresponding to date $e_d$
$\texttt{halfyearly}(s_1, s_2[, Y])$	the $e_h$ half-yearly date (half-years since 1960h1) corresponding to
	$s_1$ based on $s_2$ and Y; Y specifies topyear; see date()

$hh(e_{tc})$	the hour corresponding to date time $e_{tc}$ (ms. since 01jan1960 00:00:00000)
$\mathtt{hhC}(e_{tC})$	the hour corresponding to date time $e_{tC}~({\rm ms.~with~leap~seconds~since~}01{\rm jan1960}~00{\rm :}00{\rm :}00{\rm .}000)$
hms(h,m,s)	the $e_{tc}$ date time (ms. since 01jan1960 00:00:00.000) corresponding to h,m,s on 01jan1960
$hofd(e_d)$	the $e_h$ half-yearly date (half years since 1960h1) containing date $e_d$
hours(ms)	<i>ms</i> / <b>3</b> ,600,000
$\texttt{isleapsecond}(e_{tC})$	1 if $e_{tC}$ is a leap second; otherwise, 0
isleapyear(Y)	1 if Y is a leap year; otherwise, 0
$lastdayofmonth(e_d)$	the $\boldsymbol{e}_d$ date of the last day of the month of $\boldsymbol{e}_d$
lastdowofmonth(M,Y,d)	a synonym for lastweekdayofmonth $(M, Y, d)$
lastweekdayofmonth(M,Y,d)	
	the $e_d$ date of the last day-of-week $d$ in month $M$ of year $Y$
mdy(M, D, Y)	the $e_d$ date (days since 01jan1960) corresponding to $M, D, Y$
mdyhms(M, D, Y, h, m, s)	the $e_{tc}$ date time (ms. since 01jan1960 00:00:00.000) corresponding to M,D,Y,h,m,s
minutes(ms)	ms/60,000
$mm(e_{tc})$	the minute corresponding to date time $e_{tc}~({\rm ms.~since~01jan1960}~00{:}00{:}00{:}00{:}00{:}00{:}00{:}00$
$\mathtt{mmC}(e_{tC})$	the minute corresponding to date time $e_{tC}$ (ms. with leap seconds since 01jan 1960 00:00:00.000)
$mofd(e_d)$	the $e_m$ monthly date (months since 1960m1) containing date $e_d$
$month(e_d)$	the numeric month corresponding to date $e_d$
$\texttt{monthly}(s_1, s_2[\ , Y])$	the $e_m$ monthly date (months since 1960m1) corresponding to $s_1$ based on $s_2$ and Y; Y specifies <i>topyear</i> ; see date()
msofhours(h)	$h \times 3,600,000$
msofminutes(m)	m  imes 60,000
msofseconds(s)	s imes1,000
$\texttt{nextbirthday(}e_{d\text{\tiny DOB}}\textit{,}e_{d}[\textit{,}s_{nl}]\textit{)}$	
	the $e_d$ date of the first birthday after $e_d$ for date of birth $e_{d \text{ DOB}}$ with $s_{nl}$ the nonleap-year birthday for 29feb birthdates
$\texttt{nextdow}(e_d,d)$	a synonym for nextweekday ( $e_d$ , $d$ )
nextleapyear(Y)	the first leap year after year $Y$
$\texttt{nextweekday}(e_d,d)$	the $\boldsymbol{e}_d$ date of the first day-of-week $d$ after $\boldsymbol{e}_d$
now()	the current $e_{tc}$ datetime
previous birthday ( $e_{d{\rm DOB}}$ , $e_{d}$ [ , , previous dow ( $e_{d}$ , $d$ )	$s_{nl}$ ]) the $e_d$ date of the birthday immediately before $e_d$ for date of birth $e_{d \text{ DOB}}$ with $s_{nl}$ the nonleap-year birthday for 29feb birthdates a synonym for previousweekday $(e_d, d)$
previousleapyear( $Y$ )	the leap year immediately before year $Y$
previousweekday( $e_d$ , $d$ )	the $e_d$ date of the last day-of-week d before $e_d$
$qofd(e_d)$	the $e_d$ quarterly date (quarters since 1960q1) containing date $e_d$
Yora(Cd)	and $c_q$ quarterly date (quarters since 1700q1) containing date $c_d$

$quarter(e_d)$	the numeric quarter of the year corresponding to date $e_d$
$\texttt{quarterly}(s_1, s_2[, Y])$	the $e_q$ quarterly date (quarters since 1960q1) corresponding to $s_1$ based on $s_2$ and Y; Y specifies topyear; see date()
seconds(ms)	ms/1,000
$ss(e_{tc})$	the second corresponding to date time $e_{tc}$ (ms. since 01jan1960 00:00:00.000)
$ssC(e_{tC})$	the second corresponding to date time $e_{tC}$ (ms. with leap seconds since 01jan1960 00:00:00.000)
tC(l)	convenience function to make typing dates and times in expressions easier
tc(l)	convenience function to make typing dates and times in expressions easier
td(l)	convenience function to make typing dates in expressions easier
th(l)	convenience function to make typing half-yearly dates in expressions easier
tm(l)	convenience function to make typing monthly dates in expressions easier
today()	today's $e_d$ date
tq(l)	convenience function to make typing quarterly dates in expressions easier
tw(l)	convenience function to make typing weekly dates in expressions easier
$\texttt{week}(e_d)$	the numeric week of the year corresponding to date $e_d$ , the %td encoded date (days since 01jan1960)
$\texttt{weekly}(s_1, s_2[\ \textbf{,} Y])$	the $e_w$ weekly date (weeks since 1960w1) corresponding to $s_1$ based on $s_2$ and Y; Y specifies <i>topyear</i> ; see date()
$wofd(e_d)$	the $e_w$ weekly date (weeks since 1960w1) containing date $e_d$
$year(e_d)$	the numeric year corresponding to date $e_d$
$\texttt{yearly}(s_1, s_2[, Y])$	the $e_y$ yearly date (year) corresponding to $s_1$ based on $s_2$ and Y; Y specifies topyear, see date()
yh(Y,H)	the $e_h$ half-yearly date (half-years since 1960h1) corresponding to year Y, half-year H
ym(Y, M)	the $e_m$ monthly date (months since 1960m1) corresponding to year $Y$ , month $M$
$yofd(e_d)$	the $e_y$ yearly date (year) containing date $e_d$
yq(Y,Q)	the $e_q$ quarterly date (quarters since 1960q1) corresponding to year Y, quarter Q
уш (Y, W)	the $e_w$ weekly date (weeks since 1960w1) corresponding to year Y, week W

#### **Functions**

Stata's date and time functions are described with examples in [U] **25 Working with dates and times**, [D] **Datetime**, [D] **Datetime durations**, and [D] **Datetime relative dates**. What follows is a technical description. We use the following notation:

- $e_b$  %tb business calendar date (days)
- $e_{tc}$  %tc encoded datetime (ms. since 01jan1960 00:00:00.000)
- $e_{tC}$  %tC encoded datetime (ms. with leap seconds since 01jan1960 00:00:00.000)
- $e_d$  %td encoded date (days since 01jan1960)
- $e_w$  %tw encoded weekly date (weeks since 1960w1)
- $e_m$  %tm encoded monthly date (months since 1960m1)
- $e_q$  %tq encoded quarterly date (quarters since 1960q1)
- $e_h^{\dagger}$  %th encoded half-yearly date (half-years since 1960h1)
- $e_y$  %ty encoded yearly date (years)
- M month, 1–12
- D day of month, 1–31
- *Y* year, 0100–9999
- *h* hour, 0–23
- m minute, 0–59
- s second, 0–59 or 60 if leap seconds
- ms milliseconds
- W week number, 1–52
- *Q* quarter number, 1–4
- *H* half-year number, 1 or 2
- d numeric day of the week, 0 =Sunday, 1 =Monday, ..., 6 = Saturday

The date and time functions, where integer arguments are required, allow noninteger values and use the floor() of the value.

A Stata date-and-time variable is recorded as the number of milliseconds, days, weeks, etc., depending upon the units, from 01jan1960. Negative values indicate dates and times before 01jan1960. Allowable dates and times are those between 01jan0100 and 31dec9999, inclusive, but all functions are based on the Gregorian calendar, and values do not correspond to historical dates before Friday, 15oct1582.

age ( $e_{d \text{ DOB}}$ , $e_d$ [, $s_{nl}$ Description:	]) the age in integer years on $e_d$ for date of birth $e_{d{\rm DOB}}$ with $s_{nl}$ the nonleap-year birthday for 29feb birthdates
	$s_{nl}$ specifies when someone born on 29feb becomes another year older in nonleap years. $s_{nl} = "01mar"$ (the default) means the birthday is taken to be 01mar. $s_{nl} = "28feb"$ means the birthday is taken to be 28feb. See Methods and formulas.
	When $e_d < e_{d \text{ DOB}}$ , the result is <i>missing</i> .
Domain $e_{d \text{ DOB}}$ :	$e_d$ dates 01jan0101 to 31dec9998 (integers -678,985 to 2,936,184)
Domain $e_d$ :	$e_d$ dates 01jan0101 to 31dec9998 (integers -678,985 to 2,936,184)
Domain $s_{nl}$ :	strings "28feb", "feb28", "01mar", "1mar", "mar01", and "mar1" (case
Range:	insensitive) integers 0 to 9897 or <i>missing</i>

age_frac( $e_{d \text{ DOB}}$ , $e$ Description:	$e_d[, s_{nl}])$ the age in years, including the fractional part, on $e_d$ for date of birth $e_{d \text{ DOB}}$ with $s_{nl}$ the nonleap-year birthday for 29feb birthdates
	$s_{nl}$ specifies when someone born on 29feb becomes another year older in nonleap years. $s_{nl} = "01mar"$ (the default) means the birthday is taken to be 01mar. $s_{nl} = "28feb"$ means the birthday is taken to be 28feb. See Methods and formulas.
	When $e_d < e_{d \text{ DOB}}$ , the result is <i>missing</i> .
Domain $e_{d \text{ DOB}}$ : Domain $e_d$ : Domain $s_{nl}$ :	$e_d$ dates 01jan0101 to 31dec9998 (integers -678,985 to 2,936,184) $e_d$ dates 01jan0101 to 31dec9998 (integers -678,985 to 2,936,184) strings "28feb", "feb28", "01mar", "1mar", "mar01", and "mar1" (case
Range:	insensitive) reals 0 to 9897.997 or missing
himthday (o )	
birthday ( $e_{d \text{ DOB}}$ , ) Description:	the $e_d$ date of the birthday in year Y for date of birth $e_{d \text{ DOB}}$ with $s_{nl}$ the nonleap-year birthday for 29 feb birthdates
	$s_{nl}$ specifies when someone born on 29feb becomes another year older in nonleap years. $s_{nl} = "01mar"$ (the default) means the birthday is taken to be 01mar. $s_{nl} = "28feb"$ means the birthday is taken to be 28feb. See Methods and formulas.
Domain $e_{d \text{ DOB}}$ : Domain Y:	$e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) integers 0100 to 9999 (but probably 1800 to 2100)
Domain $s_{nl}$ :	strings "28feb", "feb28", "01mar", "1mar", "mar01", and "mar1" (case
Range:	insensitive) $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) or missing
$bofd("cal",e_d)$	
Description: Domain <i>cal</i> :	the $e_b$ business date corresponding to $e_d$ business calendar names and formats
Domain $e_d$ :	$e_d$ as defined by business calendar named $cal$
Range:	as defined by business calendar named <i>cal</i>
$Cdhms(e_d, h, m, s)$	)
Description:	the $e_{tC}$ date time (ms. with leap seconds since 01jan1960 00:00:00.000) corresponding to $e_d$ , $h$ , $m$ , $s$
Domain $e_d$ :	$e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)
Domain <i>h</i> : Domain <i>m</i> :	integers 0 to 23 integers 0 to 59
Domain $m$ . Domain $s$ :	reals 0.000 to 60.999
Range:	$e_{tC}$ date times 01jan0100 00:00:00.000 to 31dec 9999 23:59:59.999 (integers -58,695,840,000,000 to
	(11112) $(1112)$

Chms $(h, m, s)$ Description: Domain $h$ : Domain $m$ : Domain $s$ : Range:	the $e_{tC}$ date time (ms. with leap seconds since 01jan1960 00:00:00.000) corresponding to $h, m, s$ on 01jan1960 integers 0 to 23 integers 0 to 59 reals 0.000 to 60.999 $e_{tC}$ date times 01jan0100 00:00:00.000 to 31de c9999 23:59:59.999 (integers -58,695,840,000,000 to 253,717,919,999,999 + number of leap seconds) or missing
$Clock(s_1, s_2[, Y])$	
Description:	the $e_{tC}$ date time (ms. with leap seconds since 01jan1960 00:00:00.000) corresponding to $s_1$ based on $s_2$ and $Y$
Domain $s_1$ : Domain $s_2$ :	Function $Clock()$ works the same as function $clock()$ except that $Clock()$ returns a leap second-adjusted $t_c$ value rather than an unadjusted $t_c$ value. Use $Clock()$ only if original time values have been adjusted for leap seconds. strings
Domain Y: Range:	integers 1000 to 9998 (but probably 2001 to 2099) $e_{tC}$ datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999
	(integers -58,695,840,000,000 to 253,717,919,999,999 + number of leap seconds) or <i>missing</i>
$clock(s_1, s_2[, Y])$ Description:	) the $e_{tc}$ date time (ms. since 01jan1960 00:00:00.000) corresponding to $s_1$ based on $s_2$ and $Y$
	$s_1$ contains the date, time, or both, recorded as a string, in virtually any format. Months can be spelled out, abbreviated (to three characters), or indicated as numbers; years can include or exclude the century; blanks and punctuation are allowed.
	$s_2$ is any permutation of M, D, $[\#\#]$ Y, h, m, and s, with their order defining the order that month, day, year, hour, minute, and second occur (and whether they occur) in $s_1$ . $\#\#$ , if specified, indicates the default century for two-digit years in $s_1$ . For instance, $s_2 =$ "MD19Y hm" would translate $s_1 =$ "11/15/91 21:14" as 15nov1991 21:14. The space in "MD19Y hm" was not significant and the string would have translated just as well with "MD19Yhm".
	Y provides an alternate way of handling two-digit years. Y specifies the largest year that is to be returned when a two-digit year is encountered; see function date() below. If neither ## nor Y is specified, clock() returns <i>missing</i> when it encounters a two-digit year.
Domain $s_1$ : Domain $s_2$ : Domain Y: Range:	$\begin{array}{l} {\rm strings} \\ {\rm strings} \\ {\rm integers \ 1000 \ to \ 9998} \ (but \ probably \ 2001 \ to \ 2099)} \\ e_{tc} \ datetimes \ 01 jan 0100 \ 00:00:00.000 \ to \ 31 dec 9999 \ 23:59:59.999 \\ ({\rm integers \ -58,695,840,000,000 \ to \ 253,717,919,999,999}) \ or \ missing \end{array}$

Clockdiff( $e_{tC1}$ , e Description:	$e_{tC2}, s_u$ ) the $e_{tC}$ datetime difference, rounded down to an integer, from $e_{tC1}$ to $e_{tC2}$ in $s_u$ units of days, hours, minutes, seconds, or milliseconds
	Note that $Clockdiff(e_{tC1}, e_{tC2}, s_u) = -Clockdiff(e_{tC2}, e_{tC1}, s_u)$ .
Domain $e_{tC1}$ :	$e_{tC}$ datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999 (integers -58,695,840,000,000 to 253,717,919,999,999 + number of leap seconds)
Domain $e_{tC2}$ :	(integers $-58,695,840,000,000$ to $253,717,919,999,999$ + number of leap seconds) (integers $-58,695,840,000,000$ to $253,717,919,999,999$ + number of leap seconds)
Domain $s_u$ :	strings "day" or "d" for day; "hour" or "h" for hour; "minute", "min", or "m" for minute; "second", "sec", or "s" for second; and "millisecond" or "ms"
Range:	for millisecond (case insensitive) integers -312,413,759,999,999 – number of leap seconds to 312,413,759,999,999 + number of leap seconds or <i>missing</i>
$clockdiff(e_{tc1},e$	
Description:	the $e_{tc}$ date time difference, rounded down to an integer, from $e_{tc1}$ to $e_{tc2}$ in $s_u$ units of days, hours, minutes, seconds, or milliseconds
Domain $e_{tc1}$ :	Note that clockdiff $(e_{tc1}, e_{tc2}, s_u) = -clockdiff (e_{tc2}, e_{tc1}, s_u)$ . $e_{tc}$ date times 01jan0100:00:00:00:00 to 31dec9999 23:59:59.999 (ctores) 58 (05 840 000 000 to 252 717 010 000 000)
Domain $e_{tc2}$ :	(integers $-58,695,840,000,000$ to $253,717,919,999,999$ ) $e_{tc}$ datetimes 01jan0100 00:00:000000 to 31dec9999 23:59:59.999 (integers $-58,695,840,000,000$ to $253,717,919,999,999$ )
Domain $s_u$ :	strings "day" or "d" for day; "hour" or "h" for hour; "minute", "min", or "m" for minute; "second", "sec", or "s" for second; and "millisecond" or "ms"
Range:	for millisecond (case insensitive) integers -312,413,759,999,999 to 312,413,759,999,999 or <i>missing</i>
Clockdiff_frac( Description:	$(e_{tC1}, e_{tC2}, s_u)$ the $e_{tC}$ date time difference, including the fractional part, from $e_{tC1}$ to $e_{tC2}$ in $s_u$ units of days, hours, minutes, seconds, or milliseconds
	Note that
<b>_</b> .	$\texttt{Clockdiff\_frac}(e_{tC1}, e_{tC2}, s_u) = -\texttt{Clockdiff\_frac}(e_{tC2}, e_{tC1}, s_u).$
Domain $e_{tC1}$ :	$e_{tC}$ datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999 (integers -58,695,840,000,000 to 253,717,919,999,999 + number of leap seconds)
Domain $e_{tC2}$ :	$e_{tC}$ datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999
Domain $s_u$ :	(integers -58,695,840,000,000 to 253,717,919,999,999 + number of leap seconds) strings "day" or "d" for day; "hour" or "h" for hour; "minute", "min", or "m" for minute; "second", "sec", or "s" for second; and "millisecond" or "ms"
Range:	for millisecond (case insensitive) reals -312,413,759,999,999 – number of leap seconds to 312,413,759,999,999 + number of leap seconds or <i>missing</i>

clockdiff_frac	$c(e_{tc1}, e_{tc2}, s_u)$
Description:	the $e_{tc}$ date time difference, including the fractional part, from $e_{tc1}$ to $e_{tc2}$ in $s_u$ units of days, hours, minutes, seconds, or millise conds
	Note that
	$\texttt{clockdiff\_frac}(e_{tc1}, e_{tc2}, s_u) = -\texttt{clockdiff\_frac}(e_{tc2}, e_{tc1}, s_u).$
$\text{Domain} \ e_{tc1}\text{:}$	$e_{tc}$ datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999 (integers -58,695,840,000,000 to 253,717,919,999,999)
Domain $e_{tc2}$ :	$e_{tc}$ datetimes 01jan0100 00:00:00.000 to 213,717,919,999 23:59:59.999 (integers -58,695,840,000,000 to 253,717,919,999,999)
Domain $s_u$ :	strings "day" or "d" for day; "hour" or "h" for hour; "minute", "min", or "m"
<i>u</i> -	for minute; "second", "sec", or "s" for second; and "millisecond" or "ms"
	for millisecond (case insensitive)
Range:	reals -312,413,759,999,999 to 312,413,759,999,999 or missing
$Clockpart(e_{tC},$	$s_u$ )
Description:	the integer year, month, day, hour, minute, second, or millisecond of $e_{tC}$ with $s_u$
	specifying which time part
Domain $e_{tC}$ :	$e_{tC}$ datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999
Domain a 1	(integers -58,695,840,000,000 to 253,717,919,999,999 + number of leap seconds) strings "year" or "y" for year; "month" or "mon" for month; "day" or "d" for
Domain $s_u$ :	day; "hour" or "h" for hour; "minute" or "min" for minute; "second", "sec",
	or "s" for second; and "millisecond" or "ms" for millisecond (case insensitive)
Range:	integers 0 to 9999 or missing
$clockpart(e_{tc})$	s)
Description:	the integer year, month, day, hour, minute, second, or millisecond of $e_{tc}$ with $s_u$
	specifying which time part
Domain $e_{tc}$ :	$e_{tc}$ date times 01 jan 0100 00:00:00.000 to 31 dec 9999 23:59:59.999
	(integers -58,695,840,000,000 to 253,717,919,999,999)
Domain $s_u$ :	strings "year" or "y" for year; "month" or "mon" for month; "day" or "d" for
	day; "hour" or "h" for hour; "minute" or "min" for minute; "second", "sec",
Range:	or "s" for second; and "millisecond" or "ms" for millisecond (case insensitive) integers 0 to 9999 or <i>missing</i>
Cmdyhms(M, D, D)	
Description:	the $e_{tC}$ date time (ms. with leap seconds since 01jan1960 00:00:00.000)
Domain M:	corresponding to M, D, Y, h, m, s integers 1 to 12
Domain <i>D</i> :	integers 1 to 31
Domain <i>Y</i> :	integers 0100 to 9999 (but probably 1800 to 2100)
Domain <i>h</i> :	integers 0 to 23
Domain $m$ :	integers 0 to 59
Domain <i>s</i> :	reals 0.000 to 60.999
Range:	$e_{tC}$ date times 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999
0	(integers $-58,695,840,000,000$ to
	253,717,919,999,999 + number of leap seconds) or <i>missing</i>

Cofc $(e_{tc})$ Description: Domain $e_{tc}$ : Range:	the $e_{tC}$ date time (ms. with leap seconds since 01jan1960 00:00:00.000) of $e_{tc}$ (ms. without leap seconds since 01jan1960 00:00:00.000) $e_{tc}$ date times 01jan0100 00:00:00.000 to 31de c9999 23:59:59.999 (integers -58,695,840,000,000 to 253,717,919,999,999) $e_{tC}$ date times 01jan0100 00:00:00.000 to 31de c9999 23:59:59.999 (integers -58,695,840,000,000 to 253,717,919,999,999 + number of leap seconds)
$cofC(e_{tC})$ Description: Domain $e_{tC}$ : Range	the $e_{tc}$ date time (ms. without leap seconds since 01jan1960 00:00:00.000) of $e_{tC}$ (ms. with leap seconds since 01jan1960 00:00:00.000) $e_{tC}$ date times 01jan0100 00:00:00.000 to 31de c9999 23:59:59.999 (integers -58,695,840,000,000 to 253,717,919,999,999 + number of leap seconds) $e_{tc}$ date times 01jan0100 00:00:00.000 to 31de c9999 23:59:59.999 (integers -58,695,840,000,000 to 253,717,919,999,999)
Cofd $(e_d)$ Description: Domain $e_d$ : Range:	the $e_{tC}$ date time (ms. with leap seconds since 01jan1960 00:00:00.000) of date $e_d$ at time 00:00:00.000 $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) $e_{tC}$ date times 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999 (integers -58,695,840,000,000 to 253,717,919,999,999 + number of leap seconds)
$cofd(e_d)$ Description: Domain $e_d$ : Range:	the $e_{tc}$ date time (ms. since 01jan1960 00:00:00.000) of date $e_d$ at time 00:00:00.000 $e_d$ dates 01jan0100 to 31de c9999 (integers -679,350 to 2,936,549) $e_{tc}$ date times 01jan0100 00:00:00.000 to 31de c9999 23:59:59.999 (integers -58,695,840,000,000 to 253,717,919,999,999)
daily $(s_1, s_2[.Y])$	)

$\operatorname{daily}(s_1, s_2[, Y])$	
Description:	a synonym for date( $s_1, s_2[, Y]$ )

$date(s_1, s_2[, Y])$	
Description:	

the  $e_d$  date (days since 01jan1960) corresponding to  $s_1$  based on  $s_2$  and Y

 $s_1$  contains the date, recorded as a string, in virtually any format. Months can be spelled out, abbreviated (to three characters), or indicated as numbers; years can include or exclude the century; blanks and punctuation are allowed.

 $s_2$  is any permutation of M, D, and [##]Y, with their order defining the order that month, day, and year occur in  $s_1$ . ##, if specified, indicates the default century for two-digit years in  $s_1$ . For instance,  $s_2 = "MD19Y"$  would translate  $s_1 = "11/15/91"$  as 15nov1991.

Y provides an alternate way of handling two-digit years. When a two-digit year is encountered, the largest year, topyear, that does not exceed Y is returned.

	<pre>date("1/15/08","MDY",1999) = 15jan1908 date("1/15/08","MDY",2019) = 15jan2008</pre>
	<pre>date("1/15/51","MDY",2000) = 15jan1951 date("1/15/50","MDY",2000) = 15jan1950 date("1/15/49","MDY",2000) = 15jan1949</pre>
	<pre>date("1/15/01","MDY",2050) = 15jan2001 date("1/15/00","MDY",2050) = 15jan2000</pre>
Domain $s_1$ : Domain $s_2$ : Domain Y: Range:	If neither ## nor Y is specified, date() returns missing when it encounters a two-digit year. See Working with two-digit years in [D] Datetime conversion for more information. strings strings integers 1000 to 9998 (but probably 2001 to 2099) $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) or missing
datediff( $e_{d1}, e_{d2}$ ) Description:	$s_u[s_{nl}]$ ) the difference, rounded down to an integer, from $e_{d1}$ to $e_{d2}$ in $s_u$ units of days, months, or years with $s_{nl}$ the nonleap-year anniversary for $e_{d1}$ on 29feb
	$s_{nl}$ specifies the anniversary when $e_{d1}$ is on 29feb. $s_{nl} = "01mar"$ (the default) means the anniversary is taken to be 01mar. $s_{nl} = "28feb"$ means the anniversary is taken to be 28feb. See Methods and formulas.
	Note that datediff $(e_{d1}, e_{d2}, s_u, s_{nl}) = -datediff (e_{d2}, e_{d1}, s_u, s_{nl}).$
Domain $e_{d1}$ : Domain $e_{d2}$ : Domain $s_u$ :	$e_d$ dates 01jan0101 to 31dec9998 (integers -678,985 to 2,936,184) $e_d$ dates 01jan0101 to 31dec9998 (integers -678,985 to 2,936,184) strings "day" or "d" for day; "month", "mon", or "m" for month; and "year" or "y" for year (case insensitive)
Domain $s_{nl}$ :	strings "28feb", "feb28", "01mar", "1mar", "mar01", and "mar1" (case insensitive)

integers -3,615,169 to 3,615,169 or missing Range:

datediff_frac( <i>e</i> Description:	$[a_{d1}, e_{d2}, s_u[s_{nl}])$ the difference, including the fractional part, from $e_{d1}$ to $e_{d2}$ in $s_u$ units of days, months, or years with $s_{nl}$ the nonleap-year anniversary for $e_{d1}$ on 29feb	
	$s_{nl}$ specifies the anniversary when $e_{d1}$ is on 29feb. $s_{nl} = "01mar"$ (the default) means the anniversary is taken to be 01mar. $s_{nl} = "28feb"$ means the anniversary is taken to be 28feb. See Methods and formulas.	
	Note that datediff_frac( $e_{d1}$ , $e_{d2}$ , $s_u$ , $s_{nl}$ ) = -datediff_frac( $e_{d2}$ , $e_{d1}$ , $s_u$ , $s_{nl}$ ).	
Domain $e_{d1}$ :	$e_d$ dates 01jan0101 to 31dec9998 (integers -678,985 to 2,936,184)	
Domain $e_{d2}$ :	$e_d$ dates 01jan0101 to 31dec9998 (integers -678,985 to 2,936,184) strings "day" or "d" for day; "month", "mon", or "m" for month; and "year" or	
Domain $s_u$ :	"y" for year (case insensitive)	
Domain $s_{nl}$ :	strings "28feb", "feb28", "Olmar", "lmar", "marOl", and "mar1" (case insensitive)	
Range:	reals -3,615,169 to 3,615,169 or <i>missing</i>	
$datepart(e_d, s_u)$		
Description: Domain $e_d$ :	the integer year, month, or day of $e_d$ with $s_u$ specifying year, month, or day $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)	
Domain $s_d$ :	strings "day" or "d" for day; "month", "mon", or "m" for month; and "year" or	
Range:	"y" for year (case insensitive) integers 1 to 9999 or missing	
Range.		
$day(e_d)$		
Description:	the numeric day of the month corresponding to $e_d$	
Domain $e_d$ : Range:	$e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) integers 1 to 31 or missing	
8		
$daysinmonth(e_d)$		
Description:	the number of days in the month of $e_d$	
Domain $e_d$ : Range:	$e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) integers 28 to 31 or <i>missing</i>	
6	6 6	
$dayssincedow(e_d,d)$		
Description:	a synonym for dayssinceweekday $(\boldsymbol{e}_d,d)$	
dayssinceweekda Description:	$y(e_d, d)$ the number of days until $e_d$ since previous day-of-week $d$	
Domain $e_d$ :	$e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)	
Domain d:	integers 0 to 6 (0=Sunday, 1=Monday,, 6=Saturday); alternatively, strings with the first two or more letters of the day of week (case insensitive)	
Range:	integers 1 to 7 or <i>missing</i>	

daysuntildow( $e_d$ Description:	,d) a synonym for daysuntilweekday( $e_d$ ,d)
daysuntilweekda Description: Domain $e_d$ : Domain $d$ : Range:	the number of days from $e_d$ until next day-of-week $d$ $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) integers 0 to 6 (0=Sunday, 1=Monday,, 6=Saturday); alternatively, strings with the first two or more letters of the day of week (case insensitive) integers 1 to 7 or <i>missing</i>
dhms $(e_d, h, m, s)$ Description: Domain $e_d$ : Domain $h$ : Domain $m$ : Domain $s$ : Range:	the $e_{tc}$ date time (ms. since 01jan1960 00:00:00.000) corresponding to $e_d$ , $h$ , $m$ , and $s$ $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) integers 0 to 23 integers 0 to 59 reals 0.000 to 59.999 $e_{tc}$ date times 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999 (integers -58,695,840,000,000 to 253,717,919,999,999) or missing
dmy $(D, M, Y)$ Description: Domain $D$ : Domain $M$ : Domain $Y$ : Range:	the $e_d$ date (days since 01jan1960) corresponding to $D$ , $M$ , $Y$ integers 1 to 31 integers 1 to 12 integers 0100 to 9999 (but probably 1800 to 2100) $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) or missing
dofb $(e_b$ , "cal") Description: Domain $e_b$ : Domain cal: Range:	the $e_d$ date time corresponding to $e_b$ $e_b$ as defined by business calendar named $cal$ business calendar names and formats as defined by business calendar named $cal$
dofC $(e_{tC})$ Description: Domain $e_{tC}$ : Range:	the $e_d$ date (days since 01jan1960) of date time $e_{tC}$ (ms. with leap seconds since 01jan1960 00:00:00.000) $e_{tC}$ date times 01jan0100 00:00:00.000 to 31de c9999 23:59:59.999 (integers -58,695,840,000,000 to 253,717,919,999,999 + number of leap seconds) $e_d$ dates 01jan0100 to 31de c9999 (integers -679,350 to 2,936,549)

dof c $(e_{tc})$ Description: Domain $e_{tc}$ : Range:	the $e_d$ date (days since 01jan1960) of datetime $e_{tc}$ (ms. since 01jan1960 00:00:00.000) $e_{tc}$ datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999 (integers -58,695,840,000,000 to 253,717,919,999,999) $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)
dofh( $e_h$ ) Description: Domain $e_h$ : Range:	the $e_d$ date (days since 01jan1960) of the start of half-year $e_h$ $e_h$ dates 0100h1 to 9999h2 (integers -3,720 to 16,079) $e_d$ dates 01jan0100 to 01jul9999 (integers -679,350 to 2,936,366)
$dofm(e_m)$ Description: Domain $e_m$ : Range:	the $e_d$ date (days since 01jan1960) of the start of month $e_m$ $e_m$ dates 0100m1 to 9999m12 (integers -22,320 to 96,479) $e_d$ dates 01jan0100 to 01dec9999 (integers -679,350 to 2,936,519)
dofq $(e_q)$ Description: Domain $e_q$ : Range:	the $e_d$ date (days since 01jan1960) of the start of quarter $e_q$ $e_q$ dates 0100q1 to 9999q4 (integers -7,440 to 32,159) $e_d$ dates 01jan0100 to 01oct9999 (integers -679,350 to 2,936,458)
dofw $(e_w)$ Description: Domain $e_w$ : Range:	the $e_d$ date (days since 01jan1960) of the start of week $e_w$ $e_w$ dates 0100w1 to 9999w52 (integers -96,720 to 418,079) $e_d$ dates 01jan0100 to 24dec9999 (integers -679,350 to 2,936,542)
dofy $(e_y)$ Description: Domain $e_y$ : Range:	the $e_d$ date (days since 01jan1960) of 01jan in year $e_y$ $e_y$ dates 0100 to 9999 (integers 0100 to 9999) $e_d$ dates 01jan0100 to 01jan9999 (integers -679,350 to 2,936,185)
dow $(e_d)$ Description: Domain $e_d$ : Range:	the numeric day of the week corresponding to date $e_d$ ; $0 = $ Sunday, $1 =$ Monday, $\dots, 6 =$ Saturday $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) integers 0 to 6 or <i>missing</i>
doy $(e_d)$ Description: Domain $e_d$ : Range:	the numeric day of the year corresponding to date $e_d$ $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) integers 1 to 366 or <i>missing</i>

firstdayofmonth Description: Domain $e_d$ : Range:	$(e_d)$ the $e_d$ date of the first day of the month of $e_d$ $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) $e_d$ dates 01jan0100 to 01dec9999 (integers -679,350 to 2,936,519) or missing
firstdowofmonth Description:	(M, Y, d) a synonym for firstweekdayofmonth $(M, Y, d)$
firstweekdayofm Description: Domain M: Domain Y: Domain d: Range:	month(M, Y, d) the $e_d$ date of the first day-of-week $d$ in month $M$ of year $Y$ integers 1 to 12 integers 0100 to 9999 (but probably 1800 to 2100) integers 0 to 6 (0=Sunday, 1=Monday,, 6=Saturday); alternatively, strings with the first two or more letters of the day of week (case insensitive) $e_d$ dates 01jan0100 to 07dec9999 (integers -679,350 to 2,936,525) or missing
halfyear( $e_d$ ) Description: Domain $e_d$ : Range:	the numeric half of the year corresponding to date $e_d$ $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) integers 1, 2, or <i>missing</i>
halfyearly $(s_1, s_2)$ Description: Domain $s_1$ : Domain $s_2$ : Domain Y: Range:	${}_{2}[,Y])$ the $e_{h}$ half-yearly date (half-years since 1960h1) corresponding to $s_{1}$ based on $s_{2}$ and Y; Y specifies topyear; see date() strings strings "HY" and "YH"; Y may be prefixed with ## integers 1000 to 9998 (but probably 2001 to 2099) $e_{h}$ dates 0100h1 to 9999h2 (integers -3,720 to 16,079) or missing
hh $(e_{tc})$ Description: Domain $e_{tc}$ : Range:	the hour corresponding to date time $e_{tc}$ (ms. since 01jan1960 00:00:00.000) $e_{tc}$ date times 01jan0100 00:00:00.000 to 31de c9999 23:59:59.999 (integers $-58,695,840,000,000$ to 253,717,919,999,999) integers 0 through 23 or missing
hhC( $e_{tC}$ ) Description: Domain $e_{tC}$ : Range:	the hour corresponding to date time $e_{tC}$ (ms. with leap seconds since 01jan1960 00:00:00.000) $e_{tC}$ date times 01jan0100 00:00:00.000 to 31dec 9999 23:59:59.999 (integers $-58,695,840,000,000$ to 253,717,919,999,999 + number of leap seconds) integers 0 through 23 or missing

hms $(h, m, s)$ Description: Domain $h$ : Domain $m$ : Domain $s$ : Range:	the $e_{tc}$ date time (ms. since 01jan1960 00:00:00.000) corresponding to $h, m, s$ on 01jan1960 integers 0 to 23 integers 0 to 59 reals 0.000 to 59.999 date times 01jan1960 00:00:00.000 to 01jan1960 23:59:59.999 (integers 0 to 86,399,999 or missing)
hofd $(e_d)$ Description: Domain $e_d$ : Range:	the $e_h$ half-yearly date (half years since 1960h1) containing date $e_d$ $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) $e_h$ dates 0100h1 to 9999h2 (integers -3,720 to 16,079)
hours ( <i>ms</i> ) Description: Domain <i>ms</i> : Range:	<i>ms</i> /3,600,000 real; milliseconds real or <i>missing</i>
isleapsecond( $e_{tt}$ Description: Domain $e_{tC}$ : Range:	C) 1 if $e_{tC}$ is a leap second; otherwise, 0 $e_{tC}$ datetimes 01jan0100 00:00:00.000 to 31dec99999 23:59:59.999 (integers -58,695,840,000,000 to 253,717,919,999,999 + number of leap seconds) 0, 1, or missing
isleapyear(Y) Description: Domain Y: Range:	1 if Y is a leap year; otherwise, 0 integers 0100 to 9999 (but probably 1800 to 2100) 0, 1, or <i>missing</i>
lastdayofmonth $(e_d)$ Description:the $e_d$ date of the last day of the month of $e_d$ Domain $e_d$ : $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)Range: $e_d$ dates 31jan0100 to 31dec9999 (integers -679,320 to 2,936,549) or missing	
lastdowofmonth( Description:	(M, Y, d) a synonym for lastweekdayofmonth $(M, Y, d)$

lastweekdayofmc Description: Domain M: Domain Y: Domain d: Range:	bonth $(M, Y, d)$ the $e_d$ date of the last day-of-week $d$ in month $M$ of year $Y$ integers 1 to 12 integers 0100 to 9999 (but probably 1800 to 2100) integers 0 to 6 (0=Sunday, 1=Monday,, 6=Saturday); alternatively, strings with the first two or more letters of the day of week (case insensitive) $e_d$ dates 25jan0100 to 31dec9999 (integers -679,326 to 2,936,549) or missing
mdy $(M, D, Y)$ Description: Domain $M$ : Domain $D$ : Domain $Y$ : Range:	the $e_d$ date (days since 01jan1960) corresponding to $M$ , $D$ , $Y$ integers 1 to 12 integers 1 to 31 integers 0100 to 9999 (but probably 1800 to 2100) $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) or missing
mdyhms $(M, D, Y,$ Description: Domain $M$ : Domain $D$ : Domain $Y$ : Domain $h$ : Domain $m$ : Domain $m$ : Domain $s$ : Range:	h, m, s) the $e_{tc}$ datetime (ms. since 01jan1960 00:00:00.000) corresponding to $M, D, Y, h, m, s$ integers 1 to 12 integers 1 to 31 integers 0100 to 9999 (but probably 1800 to 2100) integers 0 to 23 integers 0 to 59 reals 0.000 to 59.999 $e_{tc}$ datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999 (integers -58,695,840,000,000 to 253,717,919,999,999) or missing
minutes( <i>ms</i> ) Description: Domain <i>ms</i> : Range:	ms/60,000 real; milliseconds real or <i>missing</i>
$mm(e_{tc})$ Description: Domain $e_{tc}$ : Range:	the minute corresponding to date time $e_{tc}$ (ms. since 01jan1960 00:00:00.000) $e_{tc}$ date times 01jan0100 00:00:00.000 to 31de c9999 23:59:59.999 (integers -58,695,840,000,000 to 253,717,919,999,999) integers 0 through 59 or missing
$mmC(e_{tC})$ Description: Domain $e_{tC}$ : Range:	the minute corresponding to date time $e_{tC}$ (ms. with leap seconds since 01jan1960 00:00:00.000) $e_{tC}$ date times 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999 (integers –58,695,840,000,000 to 253,717,919,999,999 + number of leap seconds) integers 0 through 59 or missing

mofd( $e_d$ ) Description: Domain $e_d$ : Range:	the $e_m$ monthly date (months since 1960m1) containing date $e_d$ $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) $e_m$ dates 0100m1 to 9999m12 (integers -22,320 to 96,479)				
$month(e_d)$ Description: Domain $e_d$ : Range:	the numeric month corresponding to date $e_d$ $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) integers 1 to 12 or <i>missing</i>				
monthly $(s_1, s_2)$ , Description: Domain $s_1$ : Domain $s_2$ : Domain $Y$ : Range:	Y]) the $e_m$ monthly date (months since 1960m1) corresponding to $s_1$ based on $s_2$ and Y; Y specifies <i>topyear</i> ; see date() strings strings "MY" and "YM"; Y may be prefixed with ## integers 1000 to 9998 (but probably 2001 to 2099) $e_m$ dates 0100m1 to 9999m12 (integers -22,320 to 96,479) or missing				
msofhours(h) Description: Domain h: Range:	$h \times 3,600,000$ real; hours real or <i>missing</i> ; milliseconds				
msofminutes(m) Description: Domain m: Range:	$m \times 60,000$ real; minutes real or <i>missing</i> ; milliseconds				
msofseconds(s) Description: Domain s: Range:	$s \times 1,000$ real; seconds real or <i>missing</i> ; milliseconds				
nextbirthday( $e_d$ Description:	$_{\text{DOB}}$ , $e_d[, s_{nl}]$ ) the $e_d$ date of the first birthday after $e_d$ for date of birth $e_{d \text{ DOB}}$ with $s_{nl}$ the nonleap-year birthday for 29feb birthdates $s_{nl}$ specifies when someone born on 29feb becomes another year older in nonleap				
Domain $e_{d \text{ DOB}}$ : Domain $e_d$ : Domain $s_{nl}$ : Range:	years. $s_{nl} = "01mar"$ (the default) means the birthday is taken to be 01mar. $s_{nl} = "28feb"$ means the birthday is taken to be 28feb. See Methods and formulas. $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) strings "28feb", "feb28", "01mar", "1mar", "mar01", and "mar1" (case insensitive) $e_d$ dates 01jan0101 to 31dec9999 (integers -678,985 to 2,936,549) or missing				

$nextdow(e_d, d)$ Description:	a synonym for $\texttt{nextweekday}(e_d, d)$			
nextleapyear(Y) Description: Domain Y: Range:	the first leap year after year $Y$ integers 0100 to 9999 (but probably 1800 to 2100) integers 1584 to 9996 or <i>missing</i>			
nextweekday( $e_d$ , Description: Domain $e_d$ : Domain $d$ : Range:	d) the $e_d$ date of the first day-of-week $d$ after $e_d$ $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) integers 0 to 6 (0=Sunday, 1=Monday,, 6=Saturday); alternatively, strings with the first two or more letters of the day of week (case insensitive) $e_d$ dates 02jan0100 to 31dec9999 (integers -679,349 to 2,936,549) or missing			
now() Description: Range:	the current $e_{tc}$ date time $e_{tc}$ date times 01jan0100 00:00:00.000 to 31de c9999 23:59:59.999 (integers -58,695,840,000,000 to 253,717,919,999,999)			
previousbirthday $(e_{d \text{ DOB}}, e_d[, s_{nl}])$ Description: the $e_d$ date of the birthday immediately before $e_d$ for date of birth $e_{d \text{ DOB}}$ with $s_{nl}$ the nonleap-year birthday for 29feb birthdates				
Domain $e_{d \text{ DOB}}$ : Domain $e_d$ : Domain $s_{nl}$ : Range:	$s_{nl}$ specifies when someone born on 29feb becomes another year older in nonleap years. $s_{nl} = "01mar"$ (the default) means the birthday is taken to be 01mar. $s_{nl} = "28feb"$ means the birthday is taken to be 28feb. See Methods and formulas. $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549) strings "28feb", "feb28", "01mar", "1mar", "mar01", and "mar1" (case insensitive) $e_d$ dates 01jan0100 to 31dec9998 (integers -679,350 to 2,936,184) or missing			
$previousdow(e_d, Description)$	d) a synonym for previousweekday ( $e_d$ , $d$ )			
previousleapyea Description: Domain Y: Range:	the leap year immediately before year $Y$ integers 0100 to 9999 (but probably 1800 to 2100) integers 1584 to 9996 or <i>missing</i>			

previousweekday	$(e_d, d)$			
Description:	the $e_d$ date of the last day-of-week d before $e_d$			
Domain $e_d$ :	$e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)			
Domain d:	integers 0 to 6 (0=Sunday, 1=Monday,, 6=Saturday); alternatively, strings			
Range:	with the first two or more letters of the day of week (case insensitive) $e_d$ dates 01jan0100 to 30dec9999 (integers -679,350 to 2,936,548) or missing			
$qofd(e_d)$				
Description:	the $e_q$ quarterly date (quarters since 1960q1) containing date $e_d$			
Domain $e_d$ :	$e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)			
Range:	$e_q^u$ dates 0100q1 to 9999q4 (integers -7,440 to 32,159)			
$quarter(e_d)$				
Description:	the numeric quarter of the year corresponding to date $e_d$			
Domain $e_d$ :	$e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)			
Range:	integers 1 to 4 or missing			
i un ger				
quarterly( $s_1$ , $s_2$ [	Y			
Description:	the $e_q$ quarterly date (quarters since 1960q1) corresponding to $s_1$ based on $s_2$ and			
Description	Y; Y specifies topyear; see date()			
Domain $s_1$ :	strings			
Domain $s_2$ :	strings "QY" and "YQ"; Y may be prefixed with ##			
Domain Y:	integers 1000 to 9998 (but probably 2001 to 2099)			
Range:	$e_q$ dates 0100q1 to 9999q4 (integers -7,440 to 32,159) or missing			
Runge.	$e_q$ and so to q1 to yyy q1 (megers $\gamma$ , 10 to $y_2$ , 15) or missing			
seconds(ms)				
Description:	ms/1,000			
Domain ms:	real; milliseconds			
Range:	real or missing			
Kange.				
$ss(e_{tc})$				
	the second corresponding to detetime c. (mg. since 01ion1060.00.00.000.000)			
Description:	the second corresponding to date time $e_{tc}$ (ms. since 01jan1960 00:00:00.000)			
Domain $e_{tc}$ :	$e_{tc}$ date times 01jan0100 00:00:000 to 31dec9999 23:59:59.999			
Danga	(integers -58,695,840,000,000 to 253,717,919,999,999)			
Range:	real 0.000 through 59.999 or missing			
aaC(a)				
$ssC(e_{tC})$	the second corresponding to detetime a (ms. with loss seconds since 01 ion 1060)			
Description:	the second corresponding to date time $e_{tC}$ (ms. with leap seconds since 01jan1960 00:00:00.000)			
Domain $e_{tC}$ :	$e_{tC}$ datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999			
$\mathcal{L}_{tC}$	(integers - 58,695,840,000,000 to 253,717,919,999,999 + number of leap seconds)			
Range:	real 0.000 through 60.999 or missing real 0.000 through 60.999 or missing			
8				

tC(l)	
Description:	convenience function to make typing dates and times in expressions easier
Domain <i>l</i> : Range:	Same as tc(), except returns leap second-adjusted values; for example, typing tc(29nov2007 9:15) is equivalent to typing 1511946900000, whereas tC(29nov2007 9:15) is 1511946923000. datetime literal strings 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999 $e_{tC}$ datetimes 01jan0100 00:00:000 to 31dec9999 23:59:59.999 (integers -58,695,840,000,000 to 253,717,919,999,999 + number of leap seconds)
tc(l) Description:	convenience function to make typing dates and times in expressions easier
Domain <i>l</i> : Range:	For example, typing tc(2jan1960 13:42) is equivalent to typing 135720000; the date but not the time may be omitted, and then 01jan1960 is assumed; the seconds portion of the time may be omitted and is assumed to be 0.000; tc(11:02) is equivalent to typing 39720000. datetime literal strings 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999 $e_{tc}$ datetimes 01jan0100 00:00:00.000 to 31dec9999 23:59:59.999 (integers -58,695,840,000,000 to 253,717,919,999,999)
td(l)	
Description:	convenience function to make typing dates in expressions easier
	For example, typing td(2jan1960) is equivalent to typing 1.
Domain <i>l</i> : Range:	date literal strings 01jan0100 to 31dec9999 $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)
th(l) Description:	convenience function to make typing half-yearly dates in expressions easier
Description.	
Domain <i>l</i> : Range:	For example, typing th(1960h2) is equivalent to typing 1. half-year literal strings 0100h1 to 9999h2 $e_h$ dates 0100h1 to 9999h2 (integers -3,720 to 16,079)
tm(l)	
Description:	convenience function to make typing monthly dates in expressions easier
	For example, typing tm(1960m2) is equivalent to typing 1.
Domain <i>l</i> : Range:	month literal strings 0100m1 to 9999m12 $e_m$ dates 0100m1 to 9999m12 (integers -22,320 to 96,479)
today() Description: Range:	today's $e_d$ date $e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)

tq(l)	convenience function to make tuning quarterly detecting expressions easier
Description:	convenience function to make typing quarterly dates in expressions easier
	For example, typing tq(1960q2) is equivalent to typing 1.
Domain <i>l</i> :	quarter literal strings 0100q1 to 9999q4
Range:	$e_q$ dates 0100q1 to 9999q4 (integers -7,440 to 32,159)
tw(l)	
Description:	convenience function to make typing weekly dates in expressions easier
	For example, typing $tw(1960w2)$ is equivalent to typing 1.
Domain <i>l</i> :	week literal strings 0100w1 to 9999w52
Range:	$e_w$ dates 0100w1 to 9999w52 (integers $-96{,}720$ to 418,079)
week( $e_d$ ) Description:	the numeric week of the year corresponding to date $e_d$ , the %td encoded date (days
Desemption	since $01jan1960$ )
	Note: The first week of a year is the first 7-day period of the year.
Domain $e_d$ :	$e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)
Range	integers 1 to 52 or missing
weekly( $s_1$ , $s_2$ [, $Y$ ]	
Description:	the $e_w$ weekly date (weeks since 1960w1) corresponding to $s_1$ based on $s_2$ and Y;
-	Y specifies topyear; see date()
Domain $s_1$ :	strings
Domain $s_2$ : Domain Y:	strings "WY" and "YW"; Y may be prefixed with ## integers 1000 to 9998 (but probably 2001 to 2099)
Range:	$e_w$ dates 0100w1 to 99999w52 (integers -96,720 to 418,079) or missing
0	
$wofd(e_d)$	
Description:	the $e_w$ weekly date (weeks since 1960w1) containing date $e_d$
Domain $e_d$ :	$e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)
Range:	$e_w$ dates 0100w1 to 9999w52 (integers $-96{,}720$ to 418{,}079)
$year(e_d)$	
Description:	the numeric year corresponding to date $e_d$
Domain $e_d$ :	$e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)
Range:	integers 0100 to 9999 (but probably 1800 to 2100)

$\texttt{yearly}(s_1, s_2[\ \textbf{,} Y]$	
Description:	the $e_y$ yearly date (year) corresponding to $s_1$ based on $s_2$ and Y; Y specifies
Domain $s_1$ :	topyear, see date() strings
Domain $s_2$ :	string "Y"; Y may be prefixed with ##
Domain $Y$ :	integers 1000 to 9998 (but probably 2001 to 2099)
Range:	$e_y$ dates 0100 to 9999 (integers 0100 to 9999) or ${\it missing}$
yh $(Y, H)$ Description:	the $e_h$ half-yearly date (half-years since 1960h1) corresponding to year Y,
Description.	half-year $H$
Domain Y:	integers 1000 to 9999 (but probably 1800 to 2100)
Domain <i>H</i> :	integers 1, 2
Range:	$e_h$ dates 1000h1 to 9999h2 (integers -1,920 to 16,079)
ym(Y, M)	
Description:	the $e_m$ monthly date (months since 1960m1) corresponding to year Y, month M
Domain Y:	integers 1000 to 9999 (but probably 1800 to 2100)
Domain M:	integers 1 to 12
Range:	$e_m$ dates 1000m1 to 9999m12 (integers $-11,520$ to 96,479)
$yofd(e_d)$	
Description:	the $e_y$ yearly date (year) containing date $e_d$
Domain $e_d$ :	$e_d$ dates 01jan0100 to 31dec9999 (integers -679,350 to 2,936,549)
Range:	$e_y$ dates 0100 to 9999 (integers 0100 to 9999)
yq(Y,Q)	
Description:	the $e_q$ quarterly date (quarters since 1960q1) corresponding to year Y, quarter Q
Domain Y:	integers 1000 to 9999 (but probably 1800 to 2100)
Domain Q:	integers 1 to 4
Range:	$e_q$ dates 1000q1 to 9999q4 (integers $-3,840$ to $32,159$ )
уw(Y,W)	
Description:	the $e_w$ weekly date (weeks since 1960w1) corresponding to year Y, week W
Domain Y:	integers 1000 to 9999 (but probably 1800 to 2100)
Domain W:	integers 1 to 52
Range:	$e_w$ dates 1000w1 to 9999w52 (integers $-49,920$ to $418,079$ )

#### **Remarks and examples**

Stata's date and time functions are described with examples in [U] 25 Working with dates and times, [D] Datetime, [D] Datetime durations, and [D] Datetime relative dates.

#### Video example

How to create a date variable from a date stored as a string

## Methods and formulas

The functions age() and age\_frac() are based on datediff() and datediff\_frac(), respectively,

 $age(e_{d \text{ DOB}}, e_d, s_{nl}) = datediff(e_{d \text{ DOB}}, e_d, "year", s_{nl})$ 

and

age\_frac(
$$e_{d \text{ DOB}}, e_d, s_{nl}$$
) = datediff\_frac( $e_{d \text{ DOB}}, e_d$ , "year",  $s_{nl}$ )

when  $e_d \ge e_{d \text{ DOB}}$ . When  $e_d < e_{d \text{ DOB}}$ , age() and age\_frac() return missing(.).

datediff  $(e_{d1}, e_{d2}, "year", s_{nl})$  returns an integer that is the number of years between  $e_{d1}$  and  $e_{d2}$ . Assume  $e_{d2} \ge e_{d1}$ . If the month and day of  $e_{d2}$  are the same or after the month and day of  $e_{d1}$ , it returns year  $(e_{d2}) - year (e_{d1})$ . If the month and day of  $e_{d2}$  are before the month and day of  $e_{d1}$ , it returns year  $(e_{d2}) - year (e_{d1}) - 1$ .

If  $e_{d2} < e_{d1}$ , the result is calculated using

$$datediff(e_{d1}, e_{d2}, "year", s_{nl}) = -datediff(e_{d2}, e_{d1}, "year", s_{nl})$$

This formula also holds for units of "month" and "day" and for datediff\_frac().

datediff  $(e_{d1}, e_{d2}, "year", s_{nl})$  has an optional fourth argument,  $s_{nl}$ , that applies only to a starting date  $e_{d1}$  on 29feb when the ending date  $e_{d2}$  is not in a leap year. There are two possible values for  $s_{nl}$ : either "01mar" (with equivalents "1mar", "mar01", "mar1") or "28feb" ("feb28"). When "01mar" is specified and  $e_{d1}$  is on 29feb, datediff() increases by one in nonleap years when  $e_{d2}$  goes to 01mar. When "28feb" is specified and  $e_{d1}$  is on 29feb, it increases by one in nonleap years when  $e_{d2}$  goes to 28feb.

In other words,  $s_{nl}$  sets the anniversary date (or birthday) in nonleap years for starting dates (or dates of birth) on 29feb. When the fourth argument is omitted, it is as if "01mar" was specified.

Regardless of the value of  $s_{nl}$ , when  $e_{d1}$  is on 29feb, datediff(..., "year",...) increases by one in leap years when  $e_{d2}$  goes to 29feb.

datediff\_frac( $e_{d1}$ ,  $e_{d2}$ , "year",  $s_{nl}$ ) is defined similarly. datediff\_frac(..., "year",...) is exactly an integer and equal to datediff(..., "year",...) for days  $e_{d2}$  on which datediff() increases by one from the day previous to  $e_{d2}$ .

The fractional part of datediff\_frac( $e_{d1}$ ,  $e_{d2}$ , "year",  $s_{nl}$ ) is calculated by first counting the number of days,  $d_1$ , from the closest date prior to  $e_{d2}$  that has an exact integer value of datediff\_frac(..., "year",...) to  $e_{d2}$ . Then number of the days,  $d_2$ , from  $e_{d2}$  to the closest following date that has an exact integer value of datediff\_frac() is determined. The fractional part is  $d_1/(d_1 + d_2)$ , and  $d_1 + d_2$  is either 365 or 366.

For examples, see example 1 and example 3 in [D] Datetime durations.

datediff( $e_{d1}$ ,  $e_{d2}$ , "month",  $s_{nl}$ ) and datediff\_frac( $e_{d1}$ ,  $e_{d2}$ , "month",  $s_{nl}$ ) follow the corresponding definitions with "year". datediff(..., "month",...) increases to an integer multiple of 12 when datediff(..., "year",...) increases by one from the day previous to  $e_{d2}$ . datediff\_frac(..., "month",...) is exactly 12 times datediff\_frac(..., "year",...) when datediff\_frac(..., "year",...) is an integer.

datediff  $(e_{d1}, e_{d2}, "month", s_{nl})$  increases by one from the day previous to  $e_{d2}$  when day  $(e_{d2}) = day(e_{d1})$ . If there is no day  $(e_{d1})$  in the month, then it increases by one on the first day of the next month. For example, if  $e_{d1}$  is on 30aug, then datediff $(\ldots, "month", \ldots)$  increases by one when  $e_{d2}$  goes to 30sep. If  $e_{d1}$  is on 31aug, then datediff $(\ldots, "month", \ldots)$  increases by one when  $e_{d2}$  goes to 01oct.

The optional fourth argument,  $s_{nl}$ , again sets the date, either "01mar" or "28feb", when datediff(..., "month",...) increases by one when  $e_{d1}$  is on 29feb.

datediff\_frac(..., "month",...) is defined like datediff\_frac(..., "year",...). Days on which datediff\_frac(..., "month",...) is an exact integer are determined, and the fractional part for other days is determined by interpolating between these days. The denominator of the fractional part is 28, 29, 30, or 31.

See example 2 of datediff() and datediff\_frac() for months in [D] Datetime durations.

datediff  $(e_{d1}, e_{d2}, "day", s_{nl})$  and datediff\_frac  $(e_{d1}, e_{d2}, "day", s_{nl})$  have no such complications. Both are equal to  $e_{d2} - e_{d1}$  and are always integers. The optional fourth argument has no bearing on the calculation and is ignored.

clockdiff  $(e_{tc1}, e_{tc2}, s_u)$  and clockdiff\_frac  $(e_{tc1}, e_{tc2}, s_u)$  take the difference  $e_{tc2} - e_{tc1}$ , which is in milliseconds, and converts the difference to the units specified by  $s_u$ , days  $(24 \times 60 \times 60 \times 1000 \text{ milliseconds})$ , hours  $(60 \times 60 \times 1000 \text{ milliseconds})$ , minutes  $(60 \times 1000 \text{ milliseconds})$ , or seconds (1000 milliseconds). clockdiff() rounds the result down to an integer, whereas clockdiff\_frac() retains the fractional part of the difference.

 $\label{eq:clockdiff} (e_{tC1}, e_{tC2}, s_u) \mbox{ and } \mbox{Clockdiff}_frac(e_{tC1}, e_{tC2}, s_u) \mbox{ are similar to clockdiff}) \mbox{ and } \mbox{clockdiff}_frac() \mbox{ except they are used with datetime/C values (times with leap seconds) rather than datetime/c values (times without leap seconds). In almost all cases, \mbox{Clockdiff}) \mbox{ and } \mbox{Clockdiff}_frac() \mbox{ give the same results as clockdiff}) \mbox{ and clockdiff}_frac() \mbox{ with the datetime/C values converted to datetime/c values. They only differ when either or both of times $e_{tC1}$ and $e_{tC2}$ are close to a leap second and the units are days, hours, or minutes. By "close", we mean within a day, hour, or minute of the leap second, respectively, for the chosen unit, and less than or equal to the leap second.$ 

Stata system file leapseconds.maint lists the dates on which leap seconds occurred. To view the file, type

. viewsource leapseconds.maint

For times close to leap seconds or times that are leap seconds, Clockdiff() and Clockdiff\_frac() base their calculations on there being a minute consisting of 61 seconds, an hour of  $60 \times 60 + 1 = 3,601$  seconds, and a day of  $24 \times 60 \times 60 + 1 = 86,401$  seconds before the leap second (and including the leap second).

For example, 31dec2016 23:59:60 is a leap second, so the time difference between 31dec2016 23:59:00 and 01jan2017 00:00:00 is a minute that consists of 61 seconds. The time difference between  $e_{tC1} =$  31dec2016 23:59:00 and  $e_{tC2} =$  31dec2016 23:59:59 is 59 seconds. So Clockdiff\_frac( $e_{tC1}$ ,  $e_{tC2}$ , "minute") = 59/61 = 0.9672 minute.

For times further away from the leap second, say,  $e_{tC1} = 31 \text{dec2016} 23:58:00$  and  $e_{tC2} = 01 \text{jan2017} 00:02:01$ , having a leap second between these times has no effect on the result. In this case, Clockdiff\_frac( $e_{tC1}$ ,  $e_{tC2}$ , "minute") = 4 + 1/60 = 4.0167 minutes. 01 jan2017 00:02:00 is considered the "anniversary" minute of 31 dec2016 23:58:00, so the difference between

these times is exactly 4 minutes. Increasing the ending time by a second gives the result 4 + 1/60 minutes. This is, of course, the same result produced by clockdiff\_frac(..., "minute") with the datetime/C values converted to datetime/c.

For units of days or hours, the logic of the calculation is similar. For units of seconds or milliseconds, the results are straightforward. The arguments  $e_{tC1}$  and  $e_{tC2}$  are numbers of milliseconds, so

$$Clockdiff_frac(e_{tC1}, e_{tC2}, "millisecond") = e_{tC2} - e_{tC1}$$

and

$$Clockdiff_frac(e_{tC1}, e_{tC2}, "second") = (e_{tC2} - e_{tC1})/1000$$

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#### Also see

- [FN] Functions by category
- [D] Datetime Date and time values and variables
- [D] Datetime durations Obtaining and working with durations
- [D] Datetime relative dates Obtaining dates and date information from other dates
- [D] egen Extensions to generate
- [D] generate Create or change contents of variable
- [M-5] date() Date and time manipulation
- [U] 13.3 Functions
- [U] 25 Working with dates and times

# Mathematical functions

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ceil(x)					$\leq n$ ; x (not ".") if x is
			g, meaning that ce		
cloglog(x)			nplementary log-lo		
comb(n,k)			nbinatorial function	,	!}
digamma(x)		-	gamma() function,		
$\exp(x)$		-	onential function $\epsilon$		
expm1(x)					-1 for small values of $ x $
<pre>floor(x)</pre>			que integer $n$ such g, meaning that flo		+1; x (not ".") if x is
int(x)		and in			d 0 (thus, $int(5.2) = 5$ s missing, meaning that
invcloglog(	[x)		erse of the complet	nentary log-log	function of $x$
invlogit(x)	1	the inv	erse of the logit fur	nction of $x$	
ln(x)		the nat	ural logarithm, ln(a	c)	
ln1m(x)			ural logarithm of 1 all values of $ x $	-x with higher	precision than $ln(1-x)$
ln1p(x)		the nat		+ x with higher	precision than $ln(1 + x)$
lnfactorial	<i>(n)</i>		ural log of $n$ factor	ial = ln(n!)	
lngamma(x)		$\ln{\Gamma(x)}$	-		
$\log(x)$			nym for $ln(x)$		
$\log 10(x)$		-	e-10 logarithm of a	c	
$\log 1m(x)$			nym for $ln1m(x)$		
$\log 1p(x)$		-	hym for $ln1p(x)$		
logit(x)		-	of the odds ratio o	fx, logit(x) =	$= \ln \{x/(1-x)\}$
$\max(x_1, x_2,$	$\ldots, x_n$ )	-	ximum value of $x_1$	-	
$\min(x_1, x_2,$			nimum value of $x_1$		
mod(x,y)	- 10		dulus of $x$ with res	2	
reldif(x,y)					; 0 if both arguments are
round(x,y)		the sam argume of <i>miss</i>	ne type of extended ent is missing or if sing	l missing value; the two argumen	missing if only one ts are two different types e nearest integer if the
1000000,97		argume round	ent $y$ is omitted; $x$ (	(not".") if x is 1 tround(.a,y)	missing (meaning that = . a if $y$ is not missing)

sign(x)	the sign of $x$ : $-1$ if $x < 0, 0$ if $x = 0, 1$ if $x > 0$ , or missing if $x$ is
	missing
sqrt(x)	the square root of $x$
sum(x)	the running sum of $x$ , treating missing values as zero
trigamma(x)	the second derivative of lngamma(x) = $d^2 \ln \Gamma(x)/dx^2$
trunc(x)	a synonym for int(x)

## **Functions**

abs (x) Description: Domain: Range:	the absolute value of $x$ -8e+307 to 8e+307 0 to 8e+307
ceil(x) Description: Domain:	the unique integer n such that $n - 1 < x \le n$ ; x (not ".") if x is missing, meaning that ceil(.a) = .a Also see floor(x), int(x), and round(x). -8e+307 to $8e+307$
Range:	integers in -8e+307 to 8e+307
cloglog(x) Description: Domain: Range:	the complementary log-log of x $cloglog(x) = ln\{-ln(1-x)\}$ 0 to 1 -8e+307 to $8e+307$
comb(n,k) Description: Domain $n$ : Domain $k$ : Range:	the combinatorial function $n!/\{k!(n-k)!\}$ integers 1 to 1e+305 integers 0 to $n$ 0 to 8e+307 or missing
digamma(x) Description:	the digamma () function, $d\ln\Gamma(x)/dx$
Domain: Range:	This is the derivative of lngamma(x). The digamma(x) function is sometimes called the psi function, $\psi(x)$ . -1e+15 to $8e+307-8e+307$ to $8e+307$ or missing

```
exp(x)
Description:
                the exponential function e^x
                This function is the inverse of ln(x). To compute e^x - 1 with high precision for
                small values of |x|, use expm1(x).
Domain:
                -8e+307 to 709
                0 to 8e+307
Range:
expm1(x)
Description:
                e^x - 1 with higher precision than \exp(x) - 1 for small values of |x|
Domain:
                -8e+307 to 709
Range:
                -1 to 8e+307
floor(x)
Description:
                the unique integer n such that n \le x \le n+1; x (not ".") if x is missing, meaning
                that floor(.a) = .a
                Also see ceil(x), int(x), and round(x).
                -8e+307 to 8e+307
Domain:
Range:
                integers in -8e+307 to 8e+307
int(x)
Description:
                the integer obtained by truncating x toward 0 (thus, int(5.2) = 5 and
                int(-5.8) = -5; x (not ".") if x is missing, meaning that int(.a) = .a
                One way to obtain the closest integer to x is int(x+sign(x)/2), which simplifies to
                int (x+0.5) for x \ge 0. However, use of the round() function is preferred. Also see
                round(x), ceil(x), and floor(x).
Domain:
                -8e+307 to 8e+307
Range:
                integers in -8e+307 to 8e+307
invcloglog(x)
Description:
                the inverse of the complementary log-log function of x
                  invcloglog(x) = 1 - exp\{-exp(x)\}
Domain:
                -8e+307 to 8e+307
Range:
                0 to 1 or missing
invlogit(x)
Description:
                the inverse of the logit function of x
                  \operatorname{invlogit}(x) = \exp(x)/\{1 + \exp(x)\}\
                -8e+307 to 8e+307
Domain.
                0 to 1 or missing
Range:
```

ln(x)	
Description:	the natural logarithm, $\ln(x)$
	This function is the inverse of $\exp(x)$ . The logarithm of $x$ in base $b$ can be calculated via $\log_b(x) = \log_a(x)/\log_a(b)$ . Hence, $\log_5(x) = \ln(x)/\ln(5) = \log(x)/\log(5) = \log(10)/\log(10)/\log(10)$ $\log_2(x) = \ln(x)/\ln(2) = \log(x)/\log(2) = \log(10)/\log(10)/\log(10)$
Domain: Range:	You can calculate $\log_b(x)$ by using the formula that best suits your needs. To compute $\ln(1-x)$ and $\ln(1+x)$ with high precision for small values of $ x $ , use $\ln \ln(x)$ and $\ln \ln(x)$ , respectively. 1e-323 to 8e+307 -744 to 709
ln1m(x) Description: Domain: Range:	the natural logarithm of $1 - x$ with higher precision than $ln(1 - x)$ for small values of $ x $ -8e+307 to 1 - c(epsdouble) -37 to 709
ln1p(x) Description: Domain: Range:	the natural logarithm of $1 + x$ with higher precision than $ln(1 + x)$ for small values of $ x $ -1 + c(epsdouble) to 8e+307 -37 to 709
lnfactorial(	<i>n</i> )
Description:	the natural log of $n$ factorial = $\ln(n!)$
Domain: Range:	To calculate $n!$ , use round(exp(lnfactorial( $n$ )), 1) to ensure that the result is an integer. Logs of factorials are generally more useful than the factorials themselves because of overflow problems. integers 0 to 1e+305 0 to 8e+307
lngamma(x) Description:	$\ln\{\Gamma(x)\}$
2 computer	Here the gamma function, $\Gamma(x)$ , is defined by $\Gamma(x) = \int_0^\infty t^{x-1} e^{-t} dt$ . For integer values of $x > 0$ , this is $\ln((x-1)!)$ . lngamma(x) for $x < 0$ returns a number such that $\exp(\ln \operatorname{gamma}(x))$ is equal to the absolute value of the gamma function, $\Gamma(x)$ . That is, $\ln \operatorname{gamma}(x)$ always returns a
Domain: Range:	real (not complex) result. -2,147,483,648 to 1e+305 (excluding negative integers) -8e+307 to 8e+307

log(x) Description:	a synonym for $ln(x)$
log10(x) Description: Domain: Range:	the base-10 logarithm of $x$ 1e-323 to 8e+307 -323 to 308
log1m(x) Description:	a synonym for ln1m(x)
log1p(x) Description:	a synonym for $ln1p(x)$
logit(x) Description: Domain: Range:	the log of the odds ratio of x, logit(x) = $\ln \{x/(1-x)\}$ 0 to 1 (exclusive) -8e+307 to 8e+307 or missing
$\max(x_1, x_2,$ Description:	., $x_n$ ) the maximum value of $x_1, x_2, \ldots, x_n$
	Unless all arguments are <i>missing</i> , missing values are ignored. max(2,10,,7) = 10
Domain $x_1$ : Domain $x_2$ :	max(.,.,.) = . -8e+307 to 8e+307 or missing -8e+307 to 8e+307 or missing
 Domain <i>x<sub>n</sub></i> : Range:	-8e+307 to 8e+307 or missing -8e+307 to 8e+307 or missing
	-8e+307 to $8e+307$ or missing -8e+307 to $8e+307$ or missing ., $x_n$ )
Range: min( $x_1, x_2, \dots$	-8e+307 to $8e+307$ or missing -8e+307 to $8e+307$ or missing ., $x_n$ )
Range: min( $x_1, x_2, \dots$	-8e+307 to $8e+307$ or missing -8e+307 to $8e+307$ or missing $.,x_n$ ) the minimum value of $x_1, x_2, \dots, x_n$ Unless all arguments are missing, missing values are ignored.

mod(x, y) Description: Domain x: Domain y: Range:	the modulus of x with respect to y mod(x,y) = x - y floor(x/y) mod(x,0) = . -8e+307 to 8e+307 0 to 8e+307 0 to 8e+307
reldif(x,y) Description:	the "relative" difference $ x - y /( y  + 1)$ ; 0 if both arguments are the same type of extended missing value; <i>missing</i> if only one argument is missing or if the two arguments are two different types of <i>missing</i>
Domain <i>x</i> : Domain <i>y</i> : Range:	-8e+307 to 8e+307 or missing -8e+307 to 8e+307 or missing 0 to 8e+307 or missing
round $(x, y)$ of Description:	r round(x) x rounded in units of y or x rounded to the nearest integer if the argument y is omitted; x (not ".") if x is missing (meaning that round(.a) = .a and that round(.a, y) = .a if y is not missing) and if y is missing, then "." is returned
	For $y = 1$ , or with y omitted, this amounts to the closest integer to x; round(5.2,1) is 5, as is round(4.8,1); round(-5.2,1) is -5, as is round(-4.8,1). The rounding definition is generalized for $y \neq 1$ . With $y = 0.01$ , for instance, x is rounded to two decimal places; round(sqrt(2),.01) is 1.41. y may also be larger than 1; round(28,5) is 30, which is 28 rounded to the closest multiple of 5. For $y = 0$ , the function is defined as returning x unmodified.
	For values of x exactly at midpoints, where it may not be clear whether to round up or down, x is always rounded up to the larger value. For example, round (4.5) is 5 and round (-4.5) is -4. Note that rounding a number is based on the floating-point number representation of the number instead of the number itself. So round() is sensitive to representation errors and precision limits. For example, 0.15 has no exact floating-point number representation. Therefore, round (0.15,0.1) is 0.1 instead of 0.2. See [U] <b>13.12 Precision and problems therein</b> for details.
Domain <i>x</i> : Domain <i>y</i> : Range:	Also see int(x), ceil(x), and floor(x). -8e+307 to 8e+307 -8e+307 to 8e+307 -8e+307 to 8e+307 -8e+307 to 8e+307
sign(x) Description: Domain: Range:	the sign of $x$ : $-1$ if $x < 0$ , 0 if $x = 0$ , 1 if $x > 0$ , or missing if $x$ is missing $-8e+307$ to $8e+307$ or missing $-1$ , 0, 1 or missing

sqrt(x) Description: Domain: Range:	the square root of $x$ 0 to 8e+307 0 to 1e+154
sum(x)	the munine over of a tractice missing volves as some
Description:	the running sum of $x$ , treating missing values as zero
Domain: Range:	For example, following the command generate $y=sum(x)$ , the <i>j</i> th observation on y contains the sum of the first through <i>j</i> th observations on x. See [D] <b>egen</b> for an alternative sum function, total(), that produces a constant equal to the overall sum. all real numbers or <i>missing</i> $-8e+307$ to $8e+307$ (excluding <i>missing</i> )
trigamma(x)	
Description:	the second derivative of lngamma( $x$ ) = $d^2 \ln \Gamma(x)/dx^2$
Domain: Range:	The trigamma() function is the derivative of digamma( $x$ ). -1e+15 to 8e+307 0 to 8e+307 or missing
trunc(x) Description:	a synonym for int(x)

## Video example

How to round a continuous variable

## References

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# Also see

- [FN] Functions by category
- [D] egen Extensions to generate
- [D] generate Create or change contents of variable
- [M-4] Intro Categorical guide to Mata functions
- [U] 13.3 Functions

## **Matrix functions**

	Contents	Functions	Reference	Also see
Contents				
cholesky(M)	the	e Cholesky de then $RR^T =$		S the matrix: if $R = \text{cholesky}(S)$ ,
coleqnumb(M,s)	the	equation num		iated with column equation <i>s</i> ; <i>missing</i> of be found
colnfreeparms(M)	the	e number of fr	ee parameters i	n columns of $M$
colnumb(M,s)	the		ber of <i>M</i> assoc annot be found	iated with column name s; missing if
colsof(M)	the	e number of co	olumns of $M$	
$\operatorname{corr}(M)$	the	e correlation m	natrix of the var	riance matrix
$\det(M)$	the	e determinant o	of matrix $M$	
diag(M)	the	e square, diago	onal matrix crea	ted from the row or column vector
diagOcnt(M)	the	e number of ze	eros on the diag	onal of $M$
el(s,i,j)		missing if $i$ of	r j are out of ra	i, j element of the matrix named $s$ ; nge or if matrix $s$ does not exist
<pre>get(systemname)</pre>	a c	opy of Stata in	nternal system	matrix systemname
hadamard(M,N)	a r			$I[i, j] \cdot N[i, j]$ (if $M$ and $N$ are not the rts a conformability error)
I(n)	an	$n \times n$ identity round(n) ide		an integer; otherwise, a round $(n) \times$
inv(M)	the	e inverse of the	e matrix $M$	
invsym(M)	the	e inverse of $M$	if $M$ is positiv	e definite
invvech(M)	a s		rix formed by f row or column	illing in the columns of the lower trivector
invvecp(M)	a s	-	rix formed by f row or column	illing in the columns of the upper trivector
issymmetric(M)	1 i	f the matrix is	symmetric; oth	nerwise, 0
J(r,c,z)	the	$r \times c$ matrix	containing eler	nents z
matmissing(M)	1 i	f any elements	s of the matrix	are missing; otherwise, 0
<pre>matuniform(r,c)</pre>	the		ces containing he interval (0, 1	uniformly distributed pseudorandom
mreldif(X, Y)	the		erence of $X$ an $ax_{i,j} \{  x_{ij} - y_i \}$	d Y, where the relative difference is $  /( y_{ij} +1) $
<pre>nullmat(matname)</pre>	us	e with the row	-join (,) and co	olumn-join (\\) operators
roweqnumb(M,s)	the	1	the of $M$ association cannot be f	ciated with row equation <i>s</i> ; <i>missing</i> if found
rownfreeparms(M)	the	e number of fr	ee parameters i	n rows of $M$
rownumb(M,s)		cannot be fou	ind	with row name s; missing if the row
rowsof(M)	the	e number of ro	ws of $M$	

sweep(M,i)	matrix M with ith row/column swept
trace(M)	the trace of matrix $M$
vec(M)	a column vector formed by listing the elements of $M$ , starting with the first column and proceeding column by column
vecdiag(M)	the row vector containing the diagonal of matrix $M$
vech(M)	a column vector formed by listing the lower triangle elements of ${\cal M}$
vecp(M)	a column vector formed by listing the upper triangle elements of ${\cal M}$

# **Functions**

We divide the basic matrix functions into two groups, according to whether they return a matrix or a scalar:

Matrix functions returning a matrix Matrix functions returning a scalar

## Matrix functions returning a matrix

In addition to the functions listed below, see [P] **matrix svd** for singular value decomposition, [P] **matrix symeigen** for eigenvalues and eigenvectors of symmetric matrices, and [P] **matrix eigenvalues** for eigenvalues of nonsymmetric matrices.

cholesky(M)

Description:	the Cholesky decomposition of the matrix: if $R = \text{cholesky}(S)$ , then $RR^T = S$
Domain: Range:	$R^T$ indicates the transpose of $R$ . Row and column names are obtained from $M$ . $n \times n$ , positive-definite, symmetric matrices $n \times n$ lower-triangular matrices
corr(M)	
Description:	the correlation matrix of the variance matrix
Domain: Range:	Row and column names are obtained from $M$ . $n \times n$ symmetric variance matrices $n \times n$ symmetric correlation matrices
diag(M)	
Description:	the square, diagonal matrix created from the row or column vector
Domain: Range:	Row and column names are obtained from the column names of $M$ if $M$ is a row vector or from the row names of $M$ if $M$ is a column vector. $1 \times n$ and $n \times 1$ vectors $n \times n$ diagonal matrices
get(systemnam	ne)
Description:	a copy of Stata internal system matrix systemname
Domain: Range:	This function is included for backward compatibility with previous versions of Stata. existing names of system matrices matrices

hadamard $(M, N)$
-------------------

Description: a matrix whose i, j element is  $M[i, j] \cdot N[i, j]$  (if M and N are not the same size, this function reports a conformability error) Domain M:  $m \times n$  matrices

Domain M:	$m \times n$ matrices
Domain N:	$m \times n$ matrices
Range:	$m \times n$ matrices

### I(n)

Description:	an $n \times n$ identity matrix if n is an integer; otherwise, a round (n) $\times$ round (n) identity
	matrix real scalars 1 to c(max_matdim) identity matrices

# inv(M)

Description	the inverse of the matrix $M$	
Description.	the inverse of the matrix m	

If M is singular, this will result in an error.

The function invsym() should be used in preference to inv() because invsym() is more accurate. The row names of the result are obtained from the column names of M, and the column names of the result are obtained from the row names of M. Domain:  $n \times n$  nonsingular matrices Range:  $n \times n$  matrices

#### invsym(M)

Description: the inverse of M if M is positive definite

	If $M$ is not positive definite, rows will be inverted until the diagonal terms are zero or
	negative; the rows and columns corresponding to these terms will be set to 0, producing
	a g2 inverse. The row names of the result are obtained from the column names of $M$ ,
р <sup>.</sup>	and the column names of the result are obtained from the row names of $M$ .
Domain:	$n \times n$ symmetric matrices
Range:	$n \times n$ symmetric matrices

#### invvech(M)

Description: a symmetric matrix formed by filling in the columns of the lower triangle from a row or column vector

Domain:  $n(n+1)/2 \times 1$  and  $1 \times n(n+1)/2$  vectors Range:  $n \times n$  matrices

### invvecp(M)

Description:	a symmetric matrix formed by filling in the columns of the upper triangle from a row
	or column vector
Domain:	$n(n+1)/2 \times 1$ and $1 \times n(n+1)/2$ vectors
Range:	$n \times n$ matrices

J(r,c,z)

Description:the  $r \times c$  matrix containing elements zDomain r:integer scalars 1 to c(max\_matdim)Domain c:integer scalars 1 to c(max\_matdim)Domain z:scalars -8e+307 to 8e+307Range: $r \times c$  matrices

matuniform(r,c)

Description: the  $r \times c$  matrices containing uniformly distributed pseudorandom numbers on the interval (0, 1)Domain r: integer scalars 1 to c(max\_matdim)

Domain c: integer scalars 1 to c(max\_matdim)

Range:  $r \times c$  matrices

nullmat(matname)

Description: use with the row-join (,) and column-join (\\) operators

Consider the following code fragment, which is an attempt to create the vector (1, 2, 3, 4):

The above program will not work because, the first time through the loop, v will not yet exist, and thus forming (v, 'i') makes no sense. nullmat() relaxes that restriction:

The nullmat() function informs Stata that if v does not exist, the function row-join is to be generalized. Joining nothing with 'i' results in ('i'). Thus the first time through the loop, v = (1) is formed. The second time through, v does exist, so v = (1, 2) is formed, and so on.

nullmat() can be used only with the , and  $\ operators$ .

Domain: matrix names, existing and nonexisting

Range: matrices including null if *matname* does not exist

sweep(M,i)

Description: matrix M with ith row/column swept

The row and column names of the resultant matrix are obtained from M, except that the *n*th row and column names are interchanged. If B = sweep(A, k), then

$$\begin{split} B_{kk} &= \frac{1}{A_{kk}} \\ B_{ik} &= -\frac{A_{ik}}{A_{kk}}, \qquad i \neq k \\ B_{kj} &= \frac{A_{kj}}{A_{kk}}, \qquad j \neq k \\ B_{ij} &= A_{ij} - \frac{A_{ik}A_{kj}}{A_{kk}}, \qquad i \neq k, j \neq k \end{split}$$

Domain M:	$n \times n$ matrices
Domain <i>i</i> :	integer scalars 1 to $n$
Range:	$n \times n$ matrices

#### vec(M)

Description:	a column vector formed by listing the elements of M, starting with the first column and
	proceeding column by column
Domain:	matrices
Range:	column vectors ( $n \times 1$ matrices)

### vecdiag(M)

Description: the row vector containing the diagonal of matrix M

	vecdiag() is the opposite of diag(). The row name is set to r1; the column names
_	are obtained from the column names of M.
Domain:	$n \times n$ matrices
Range:	$1 \times n$ vectors

#### vech(M)

Description:	a column vector formed by listing the lower triangle elements of $M$
Domain:	$n \times n$ matrices
Range:	$n(n+1)/2 \times 1$ vectors

### vecp(M)

Description:	a column vector formed by listing the upper triangle elements of $M$
Domain:	$n \times n$ matrices
Range:	$n(n+1)/2 \times 1$ vectors

# Matrix functions returning a scalar

coleqnumb(M Description: Domain M: Domain s: Range:	the equation number of $M$ associated with column equation $s$ ; <i>missing</i> if the column equation cannot be found
Domain: Range:	the number of free parameters in columns of M matrices integer scalars 0 to c(max_matdim)
colnumb (M, s) Description: Domain M: Domain s: Range:	the column number of $M$ associated with column name $s$ ; missing if the column cannot be found
colsof ( <i>M</i> ) Description: Domain: Range:	the number of columns of M matrices integer scalars 1 to c(max_matdim)
det ( <i>M</i> ) Description: Domain: Range:	the determinant of matrix $M$ $n \times n$ (square) matrices scalars $-8e+307$ to $8e+307$
diag0cnt(M) Description: Domain: Range:	the number of zeros on the diagonal of $M$ $n \times n$ (square) matrices integer scalars 0 to $n$
el (s, i, j) Description: Domain s: Domain i: Domain j: Range:	<pre>s[floor(i),floor(j)], the i, j element of the matrix named s; missing if i or j are out of range or if matrix s does not exist strings containing matrix name scalars 1 to c(max_matdim) scalars 1 to c(max_matdim) scalars -8e+307 to 8e+307 or missing</pre>

Domain M:	1 if the matrix is symmetric; otherwise, 0
Domain M:	1 if any elements of the matrix are missing; otherwise, 0
Domain X: Domain Y:	the relative difference of X and Y, where the relative difference is defined as $\max_{i,j}\{ x_{ij}-y_{ij} /( y_{ij} +1)\}$
roweqnumb(M Description: Domain M: Domain s: Range:	the equation number of $M$ associated with row equation $s$ ; missing if the row equation cannot be found matrices
Domain:	s(M) the number of free parameters in rows of M matrices integer scalars 0 to c(max_matdim)
rownumb(M,s) Description: Domain M: Domain s: Range:	the row number of $M$ associated with row name $s$ ; missing if the row cannot be found matrices
rowsof ( <i>M</i> ) Description: Domain: Range:	the number of rows of M matrices integer scalars 1 to c(max_matdim)
trace(M) Description: Domain: Range:	the trace of matrix $M$ $n \times n$ (square) matrices scalars $-8e+307$ to $8e+307$

Jacques Salomon Hadamard (1865–1963) was born in Versailles, France. He had a tumultuous childhood, eating elephant meat to survive and enduring the premature deaths of two younger sisters. Hadamard taught while working on his doctorate, which he obtained in 1892 from École Normale Supérieure. His dissertation is recognized as the first examination of singularities. Hadamard published a paper on the Riemann zeta function, for which he was awarded the Grand Prix des Sciences Mathématiques in 1892. Shortly after, he became a professor at the University of Bordeaux and made many significant contributions over the course of four years. For example, in 1893 he published a paper on determinant inequalities, giving rise to Hadamard matrices. Then in 1896, he used complex analysis to prove the prime number theorem, and he was awarded the Bordin Prize by the Academy of Sciences for his work on dynamic trajectories. In the following years, he published books on two-dimensional and three-dimensional geometry, as well as an influential paper on functional analysis. He was elected to presidency of the French Mathematical Society in 1906 and as chair of mechanics at the Collège de France in 1909. Faced with the tragic deaths of two of his sons during World War I, Hadamard buried himself in his work. He continued to publish outstanding work in new areas, including probability theory, education, and psychology. In 1956, he was awarded the CNRS Gold Medal for his many contributions.

## Reference

Mazýa, V. G., and T. O. Shaposhnikova. 1998. Jacques Hadamard, A Universal mathematician. Providence, RI: American Mathematical Society.

## Also see

- [FN] Functions by category
- [D] egen Extensions to generate
- [D] generate Create or change contents of variable
- [M-4] Intro Categorical guide to Mata functions
- [U] 13.3 Functions
- [U] 14.8 Matrix functions

# **Programming functions**

	Contents	Functions	References	Also see
Contents				
$autocode(x,n,x_0,x_1)$	re	eturns the uppe	r bound of the in	$x_1$ into $n$ equal-length intervals and interval that contains $x$ or the upper if $x < x_0$ or $x > x_1$ , respectively
byteorder()	1 e	if your compu	ter stores numbe	ers by using a hilo byte order and stores numbers by using a lohi byte
c( <i>name</i> )			system or consta	ant result c( <i>name</i> ) (see [P] creturn)
_caller()			•	ion that invoked the currently
			n; see [P] version	-
$chop(x, \epsilon)$		ound(x) if ab missing	s(x - round(x	)) $< \epsilon$ ; otherwise, x; or x if x is
clip(x,a,b)		if $a < x < b$ , > b; x if x is i		$\leq a$ , or <i>missing</i> if x is missing or if
cond(x,a,b[,c])			I nonmissing, $b$ is and $x$ evaluates	f $x$ is false, and $c$ if $x$ is missing; $a$ if s to missing
e(name)			ed result e ( <i>nam</i> ther programs	e); see [U] 18.8 Accessing results
e(sample)	1	if the observat	ion is in the estin	mation sample and 0 otherwise
epsdouble()	tł	ne machine pre	cision of a doub	le-precision number
<pre>epsfloat()</pre>	tł	ne machine pre	cision of a floati	ng-point number
fileexists(f)	1	if the file spec	ified by <i>f</i> exists	; otherwise, 0
<pre>fileread(f)</pre>	tł	ne contents of t	he file specified	by f
filereaderror(s)		or positive inte	eger, said value l	having the interpretation of a return
filewrite(f,s[,r])		-	specified by s to ytes in the result	the file specified by $f$ and returns ing file
float(x)	tł	ne value of $x$ ro	ounded to float	precision
<pre>fmtwidth(fmtstr)</pre>		ne output lengtl oes not contain		ntained in <i>fmtstr</i> ; <i>missing</i> if <i>fmtstr</i>
frval()	re	eturns values of	f variables stored	l in other frames
_frval()	р	rogrammer's v	ersion of frval	()
has_eprop( <i>name</i> )	1	if name appear	rs as a word in e	(properties); otherwise, 0
$inlist(z,a,b,\ldots)$	1	if $z$ is a memb	er of the remaini	ing arguments; otherwise, 0
inrange(z,a,b)	1	if it is known	that $a \leq z \leq b$ ; of	otherwise, 0
$irecode(x, x_1, \ldots, x_n)$				, $x_n$ is not weakly increasing; 0 if $x_2 < x \le x_3; \ldots; n$ if $x > x_n$
<pre>matrix(exp)</pre>				calars and matrices; see scalar()
<pre>maxbyte()</pre>	tł	ne largest value	that can be store	ed in storage type byte
<pre>maxdouble()</pre>	tł	ne largest value	that can be store	ed in storage type double

maxfloat()	the largest value that can be stored in storage type float
maxint()	the largest value that can be stored in storage type int
maxlong()	the largest value that can be stored in storage type long
$\min(x_1, x_2, \ldots, x_n)$	a synonym for missing $(x_1, x_2, \ldots, x_n)$
minbyte()	the smallest value that can be stored in storage type byte
mindouble()	the smallest value that can be stored in storage type double
minfloat()	the smallest value that can be stored in storage type float
<pre>minint()</pre>	the smallest value that can be stored in storage type int
minlong()	the smallest value that can be stored in storage type long
$missing(x_1, x_2, \dots, x_n)$	1 if any $x_i$ evaluates to <i>missing</i> ; otherwise, 0
r(name)	the value of the stored result r (name); see [U] 18.8 Accessing
	results calculated by other programs
$recode(x, x_1, \ldots, x_n)$	missing if $x_1, x_2, \ldots, x_n$ is not weakly increasing; x if x is missing;
	$x_1$ if $x \le x_1$ ; $x_2$ if $x \le x_2$ ,; otherwise, $x_n$ if $x > x_1, x_2,,$
	$x_{n-1}$ . $x_i \ge$ . is interpreted as $x_i = +\infty$
replay()	1 if the first nonblank character of local macro '0' is a comma, or if
	'0' is empty
return( <i>name</i> )	the value of the to-be-stored result r (name); see [P] return
s(name)	the value of stored result s (name); see [U] 18.8 Accessing results
	calculated by other programs
<pre>scalar(exp)</pre>	restricts name interpretation to scalars and matrices
<pre>smallestdouble()</pre>	the smallest double-precision number greater than zero

# Functions

autocode ( $x$ , $n$ , $x$ Description:	$x_0, x_1$ ) partitions the interval from $x_0$ to $x_1$ into $n$ equal-length intervals and returns the upper bound of the interval that contains $x$ or the upper bound of the first or last interval if $x < x_0$ or $x > x_1$ , respectively	
	This function is an automated version of recode(). See [U] 26 Working with categorical data and factor variables for an example.	
	The algorithm for autocode() is	
	if $(n \ge .   x_0 \ge .   x_1 \ge .   n \le 0   x_0 \ge x_1)$ then return <i>missing</i>	
	if $x \ge .$ , then return $x$ otherwise	
	for $i = 1$ to $n - 1$	
	$xmap = x_0 + i * (x_1 - x_0)/n$	
	if $x \leq xmap$ then return $xmap$	
	end	
	otherwise	
Domain x:	-8e+307  to  8e+307	
Domain <i>n</i> :	integers 1 to 10,000	
Domain $x_0$ :	-8e+307 to $8e+307$	
Domain $x_1$ :	$x_0$ to 8e+307	
Range:	$x_0$ to $x_1$	
<pre>byteorder()</pre>		
Description:	1 if your computer stores numbers by using a hilo byte order and evaluates to 2 if your computer stores numbers by using a lohi byte order	
	Consider the number 1 written as a 2-byte integer. On some computers (called hilo), it is written as "00 01", and on other computers (called lohi), it is written as "01 00" (with the least significant byte written first). There are similar issues for 4-byte integers, 4-byte floats, and 8-byte floats. Stata automatically handles byte-order differences for Stata-created files. Users need not be concerned about this issue. Programmers producing custom binary files can use byteorder() to determine the native byte ordering; see [P] file.	
Range:	1 and 2	
c( <i>name</i> ) Description:	the value of the system or constant result $c(name)$ (see [P] creturn)	
Description.		
Domain:	Referencing c( <i>name</i> ) will return an error if the result does not exist. names	
Range:	real values, strings, or missing	

<pre>_caller() Description:</pre>	version of the program or session that invoked the currently running program; see [P] <b>version</b>
Range:	This is a function for use by programmers. 1 to 19.0 (or 1 to 19.5 for StataNow)
chop $(x, \epsilon)$ Description: Domain $x$ : Domain $\epsilon$ : Range:	round(x) if $abs(x - round(x)) < \epsilon$ ; otherwise, x; or x if x is missing -8e+307 to 8e+307 -8e+307 to 8e+307 -8e+307 to 8e+307
clip(x,a,b) Description:	$x$ if $a < x < b$ , $b$ if $x \ge b$ , $a$ if $x \le a$ , or missing if $x$ is missing or if $a > b$ ; $x$ if $x$ is missing
Domain <i>x</i> : Domain <i>a</i> : Domain <i>b</i> : Range:	If a or b is missing, this is interpreted as $a = -\infty$ or $b = +\infty$ , respectively. -8e+307 to 8e+307 -8e+307 to 8e+307 -8e+307 to 8e+307 -8e+307 to 8e+307

cond(x,a,b[,c])	
Description:	a if $x$ is true and nonmissing, $b$ if $x$ is false, and $c$ if $x$ is missing; $a$ if $c$ is not specified and $x$ evaluates to missing
	Note that expressions such as $x > 2$ will never evaluate to <i>missing</i> .
	cond(x>2,50,70) returns 50 if x $>$ 2 (includes x $\geq$ .) cond(x>2,50,70) returns 70 if x $\leq$ 2
	If you need a case for missing values in the above examples, try
	cond(missing(x), ., cond(x>2,50,70)) returns . if x is missing, returns 50 if x $>$ 2, and returns 70 if x $\leq$ 2
	If the first argument is a scalar that may contain a missing value or a variable containing missing values, the fourth argument has an effect.
	<pre>cond(wage,1,0,.) returns 1 if wage is not zero and not missing cond(wage,1,0,.) returns 0 if wage is zero cond(wage,1,0,.) returns . if wage is missing</pre>
Domain x: Domain a: Domain b: Domain c: Range:	Caution: If the first argument to cond() is a logical expression, that is, cond(x>2,50,70,.), the fourth argument is never reached. $-8e+307$ to $8e+307$ or <i>missing</i> ; $0 \Rightarrow false$ , otherwise interpreted as <i>true</i> numbers and strings numbers if a is a number; strings if a is a string numbers if a is a number; strings if a is a string a, b, and c
e ( <i>name</i> ) Description:	the value of stored result e ( <i>name</i> ); see [U] <b>18.8 Accessing results calculated by other programs</b>
Domain: Range:	<ul> <li>e(name) = scalar missing if the stored result does not exist</li> <li>e(name) = specified matrix if the stored result is a matrix</li> <li>e(name) = scalar numeric value if the stored result is a scalar names</li> <li>strings, scalars, matrices, or missing</li> </ul>
e(sample) Description: Range:	1 if the observation is in the estimation sample and 0 otherwise 0 and 1
epsdouble() Description:	the machine precision of a double-precision number
Range:	If $d < epsdouble()$ and (double) $x = 1$ , then $x + d = (double) 1$ . This function takes no arguments, but the parentheses must be included. a double-precision number close to 0

epsfloat() Description:	the machine precision of a floating-point number		
Range:	If $d < \texttt{epsfloat}()$ and (float) $x = 1$ , then $x + d = (\texttt{float}) 1$ . This function takes no arguments, but the parentheses must be included. a floating-point number close to 0		
<pre>fileexists(f) Description:</pre>	1 if the file specified by $f$ exists; otherwise, 0		
Domain: Range:	If the file exists but is not readable, fileexists() will still return 1, because it does exist. If the "file" is a directory, fileexists() will return 0. filenames 0 and 1		
fileread( <i>f</i> )			
Description:	the contents of the file specified by $f$		
Domain: Range:	If the file does not exist or an I/O error occurs while reading the file, then "fileread() error #" is returned, where # is a standard Stata error return code. filenames strings		
filereaderror(s	3)		
Description:	0 or positive integer, said value having the interpretation of a return code		
	It is used like this		
	<pre>. generate strL s = fileread(filename) if fileexists(filename) . assert filereaderror(s)==0</pre>		
	or this		
	<pre>. generate strL s = fileread(filename) if fileexists(filename) . generate rc = filereaderror(s)</pre>		
	That is, filereaderror( $s$ ) is used on the result returned by fileread( <i>filename</i> ) to determine whether an I/O error occurred.		
	In the example, we only fileread() files that fileexists(). That is not required. If the file does not exist, that will be detected by filereaderror() as an error. The way we showed the example, we did not want to read missing files as errors. If we wanted to treat missing files as errors, we would have coded		
	<pre>. generate strL s = fileread(filename) . assert filereaderror(s)==0</pre>		
	or		
	<pre>. generate strL s = fileread(filename) . generate rc = filereaderror(s)</pre>		
Domain: Range:	strings integers		

filewrite( $f, s[, r]$ )			
Description:	writes the string specified by $s$ to the file specified by $f$ and returns the number of bytes in the resulting file		
	If the optional argument $r$ is specified as 1, the file specified by $f$ will be replaced if it exists. If $r$ is specified as 2, the file specified by $f$ will be appended to if it exists. Any other values of $r$ are treated as if $r$ were not specified; that is, $f$ will only be written to if it does not already exist.		
	When the file f is freshly created or is replaced, the value returned by filewrite() is the number of bytes written to the file, strlen(s). If r is specified as 2, and thus filewrite() is appending to an existing file, the value returned is the total number of bytes in the resulting file; that is, the value is the sum of the number of the bytes in the file as it existed before filewrite() was called and the number of bytes newly written to it, strlen(s).		
Domain <i>f</i> :	If the file exists and $r$ is not specified as 1 or 2, or an error occurs while writing to the file, then a negative number (#) is returned, where $abs(#)$ is a standard Stata error return code. filenames		
Domain s:	strings		
Domain <i>r</i> : Range:	integers 1 or 2 integers		
Tunger	in opens		
float(x)			
Description:	the value of $x$ rounded to float precision		
	Although you may store your numeric variables as byte, int, long, float, or double, Stata converts all numbers to double before performing any calculations. Consequently, difficulties can arise in comparing numbers that have no finite binary representation.		
	For example, if the variable x is stored as a float and contains the value 1.1 (a repeating "decimal" in binary), the expression $x==1.1$ will evaluate to false because the literal 1.1 is the double representation of 1.1, which is different from the float representation stored in x. (They differ by $2.384 \times 10^{-8}$ .) The expression $x==$ float(1.1) will evaluate to true because the float() function converts the literal 1.1 to its float representation before it is compared with x.		
Domain:	(See [U] <b>13.12 Precision and problems therein</b> for more information.) -1e+38 to 1e+38		
Range:	-1e+38 to $1e+38$		
fortani del (fortato)			
fmtwidth( <i>fmtstr</i> ) Description:	the output length of the % <i>fmt</i> contained in <i>fmtstr</i> ; <i>missing</i> if <i>fmtstr</i> does not contain a valid % <i>fmt</i>		
	For example, fmtwidth("%9.2f") returns 9 and fmtwidth("%tc") returns 18.		
Range:	strings		

<pre>frval(lvar,var) Description:</pre>	returns values of variables stored in other frames				
2.000.prom	The frame functions frval() and _frval() access values of variables in frames outside the current frame. If you do not know what a frame is, see [D] frames intro.				
	The two functions do the same thing, but frval() is easier to use, and it is safer. _frval() is a programmer's function.				
	<i>lvar</i> is the name of a variable created by frlink that links the current frame to another frame.				
	<i>var</i> is the name of a variable in the other frame.				
	Returned is the value of <i>var</i> from the observation in the other frame that matches the observation in the current frame.				
Example 1:	The current frame contains data on persons. Among the variables in the current frame is countyid containing the county in which each person lives.				
	Frame frcounty contains data on counties. In these data, variable countyid also records the county's ID, and the other variables record county characteristics.				
	In the current frame, you have previously created variable linkcnty that links the current frame to frcounty. You did this by typing				
	.frlinkm:1 countyid, frame(frcounty) generate(linkcnty)				
	Thus, you can now type				
	.generate rel_income = income / frval(linkcnty, median_income)				
Example 2:	income is an existing variable in the current frame. median_income is an existing variable in frcounty. rel_income will be a new variable in the current frame, containing the income of each person divided by the median income of the county in which they live.				
	It is usual to name frames after dataset names and to name link variables after frame names. Here is an example of this, following the names used above:				
	<pre>. use persons, clear . frame create county . frame county: use county . frlink m:1 countyid, frame(county) . generate rel_income = income / frval(county, median_income)</pre>				
Domain <i>lvar</i> :	the name of a variable created by frlink that links the current frame to another				
Domain var:	frame any variable (string or numeric) in the frame to which <i>lvar</i> links; varname				
Range:	abbreviation is allowed range of <i>var</i> , plus missing value (missing value is defined as . when <i>var</i> contains numeric data and "" when <i>var</i> contains string data; missing value is returned for observations in the current frame that are unmatched in the other frame)				

frval(lvar,var,unm)			
Description:	the frval() function described above but with a third argument <i>unm</i>		
	frval() returns the value of <i>var</i> from the observation in the frame linked using <i>lvar</i> that matches the observation in the current frame and the value in <i>unm</i> if there is no matching observation.		
	For example, type		
	.generate median_inc = frval(county, median_income, .a)		
	to create new variable median_inc in the current frame, containing median_income from the other frame, or .a when there is no matched observation in the other frame.		
Domain <i>lvar</i> :	the name of a variable created by frlink that links the current frame to another		
Domain var:	frame any variable (string or numeric) in the frame to which <i>lvar</i> links; varname abbreviation is allowed		
Domain unm:	any numeric value if <i>var</i> is numeric; any string value when <i>var</i> is string		
Range:	range of <i>var</i> , plus <i>unm</i>		
_frval( <i>frm</i> , <i>var</i>	<i>,i</i> )		
Description:	programmer's version of frval()		
	It is useful for those wishing to write their own frlink and create special (or at least different) effects.		
	_frval() returns values of variables stored in other frames. It returns <i>var</i> 's <i>i</i> th observation $(var[i])$ from the frame <i>frm</i> ; see [D] <b>frames intro</b> .		
	If <i>i</i> is outside the valid range of observations for the frame, _frval() returns missing.		
	For example, you have two datasets in memory. The current frame is named default and contains 57 observations. The other dataset, we will assume, is stored in frame xdata. It contains different variables but on the same 57 observations. The		

observation 1 in xdata, observation 2 to observation 2, and so on. You can type

. generate hrlywage = income / \_frval(xdata, hrswrked, \_n)

This will divide values of income stored in default by values of hrswrked stored in xdata.

two datasets are in the same order so that observation 1 in default corresponds to

The first thing to notice is that \_frval()'s first two arguments are not expressions. You just type the name of the frame and the name of the variable without embedding them in quotes. We specified xdata for the frame name and and hrswrked for the variable name.

The second thing to notice is that the third argument is an expression. To emphasize that, let's change the example. Assume that xdata contains 58 instead of 57 observations. Assume that observation 1 in default corresponds to observation 2 in xdata, observation 2 corresponds to observation 3, and so on. There is no observation in default that corresponds to observation 1 in xdata. In this case, you type

. generate hrlywage = income / \_frval(xdata, hrswrked, \_n+1)

These examples are artificial. You will normally use \_frval() by creating a variable in default that contains the corresponding observation numbers in xdata. If the variable were called xobsno, then in the first example, xobsno would contain 1, 2, ..., 57.

In the second example, xobsno would contain 2, 3, ..., 58.

In another example, xobsno might contain 9, 6, ..., 32, which is to say, the numbers 2, 3, ..., 58, but permuted to reflect the datasets' jumbled order.

In yet another example, xobsno might contain 9, 6, 9, ..., 32, which is to say, observation 1 and 3 in default both correspond to observation 9 in xdata. xdata in this example might record geographic location and in default, persons in observations 1 and 3 live in the same locale.

And in a final example, xobsno might contain all the above and missing values (.). The missing values would indicate observations in default that have no corresponding observation in xdata. If observations 7 and 11 contained missing, that means there would be no observations in xdata corresponding to observations 7 and 11 in default. (\_frval() has a second syntax that allows you to specify the value returned when there are no corresponding observations; see below.)

Regardless of the complexity of the example, the value of xobsno in observation *i* is the corresponding observation number *i* in xdata. Regardless of complexity, to create new variable hrlywage in default, you would type

```
. generate hrlywage = income / _frval(xdata, hrswrked, xobsno)
```

That leaves only the question of how to generate xobsno in all the above situations, and it is easy to do. See [D] frlink.

There are two more things to know.

First, variables across frames are distinct. If the variable we have been calling income in default were named x, and the variable hrswrked in xdata were also named x, you would type

. generate hrlywage = x / \_frval(xdata, x, xobsno)

Second, although we have demonstrated the use of \_frval() with numeric variables, it works with string variables too. If var is a string variable name, \_frval() returns a string result.

Domain *frm*: Domain var:

any existing framename

Domain *i*:

any existing variable name in *frm*; varname abbreviation is allowed any numeric values including missing values even though the nonmissing values should be integers in the range 1 to frm's \_N; nonintegers will be interpreted as the corresponding integer obtained by truncation, and values outside the range will be treated as if they were missing value

range of var in frm plus missing value; numeric missing value (.) when var is Range: numeric, and string missing value ("") when var is string

_frval( <i>frm</i> ,var,	<i>i</i> , <i>v</i> )			
Description:				
	frval() returns values of variables stored in other frames. It returns var's <i>i</i> th observation (var[i]) from the frame <i>frm</i> .			
	When v is specified, $\_frval()$ returns v if $var[i]$ is missing or if i is outside the valid range of observations.			
	.generate hwage = income / _frval(xdata, hrswrked, xobsno, .z) .generate hwage = income / _frval(xdata, hrswrked, xobsno, avg)			
	In the first case, .z is returned for observations in which xobsno contains values that are out of range. In the second case, the value recorded in variable avg is returned.			
Domain <i>frm</i> : Domain <i>var</i> : Domain <i>i</i> :	any existing framename any existing variable name in <i>frm</i> ; varname abbreviation is allowed any numeric values including missing values even though the nonmissing values should be integers in the range 1 to <i>frm</i> 's $\_N$ ; nonintegers will be interpreted as the corresponding integer obtained by truncation, and values outside the range will be treated as if they were missing value			
Domain <i>v</i> :	treated as if they were missing value any numeric value when <i>var</i> is numeric; any string value when <i>var</i> is string (can be a constant or vary observation by observation)			
Range:	range of <i>var</i> in <i>frm</i> plus <i>v</i>			
has_eprop(name)				
Description:	1 if <i>name</i> appears as a word in e(properties); otherwise, 0			
Domain:	names 0 or 1			
Range:	0 or 1			
<pre>inlist(z,a,b,</pre>				
Description:	1 if z is a member of the remaining arguments; otherwise, 0			
Domain: Range:	All arguments must be reals or all must be strings. The number of arguments is between 2 and 250 for reals and between 2 and 10 for strings. all reals or all strings 0 or 1			
inrange(z,a,b) Description:	1 if it is known that $a \le z \le b$ ; otherwise, 0			
1	The following ordered rules apply: $z \ge .$ returns 0. $a \ge .$ and $b = .$ returns 1. $a \ge .$ returns 1 if $z \le b$ ; otherwise, it returns 0. $b \ge .$ returns 1 if $a \le z$ ; otherwise, it returns 0. Otherwise, 1 is returned if $a \le z \le b$ . If the arguments are strings, "." is interpreted as "".			
Domain:	all reals or all strings			
Range:	0 or 1			

$irecode(x, x_1, x_2)$ Description:	missing if x is missing or $x_1, \ldots, x_n$ is not weakly increasing; 0 if $x \le x_1$ ; 1 if $x_1 < x \le x_2$ ; 2 if $x_2 < x \le x_3$ ;; n if $x > x_n$
	Also see autocode() and recode() for other styles of recode functions.
Domain $x$ : Domain $x_i$ : Range:	irecode(3, -10, -5, -3, -3, 0, 15, .) = 5 -8e+307 to 8e+307 -8e+307 to 8e+307 nonnegative integers
matrix( <i>exp</i> ) Description: Domain: Range:	restricts name interpretation to scalars and matrices; see scalar() any valid expression evaluation of <i>exp</i>
<pre>maxbyte()</pre>	
Description:	the largest value that can be stored in storage type byte
Range:	This function takes no arguments, but the parentheses must be included. one integer number
maxdouble() Description:	the largest value that can be stored in storage type double
Range:	This function takes no arguments, but the parentheses must be included. one double-precision number
maxfloat() Description:	the largest value that can be stored in storage type float
Range:	This function takes no arguments, but the parentheses must be included. one floating-point number
maxint() Description:	the largest value that can be stored in storage type int
×	This function takes no arguments, but the parentheses must be included.
Range:	one integer number
maxlong()	the langest very short each he stored in stars a true 2
Description:	the largest value that can be stored in storage type long
Range:	This function takes no arguments, but the parentheses must be included. one integer number

mi $(x_1, x_2, \ldots, x_n)$ Description:	a synonym for missing $(x_1, x_2, \ldots, x_n)$		
minbyte() Description:	the smallest value that can be stored in storage type byte This function takes no arguments, but the parentheses must be included.		
Range:	one integer number		
mindouble() Description:	the smallest value that can be stored in storage type double		
Range:	This function takes no arguments, but the parentheses must be included. one double-precision number		
minfloat() Description:	the smallest value that can be stored in storage type float		
Range:	This function takes no arguments, but the parentheses must be included. one floating-point number		
minint()			
Description:	the smallest value that can be stored in storage type int		
Range:	This function takes no arguments, but the parentheses must be included. one integer number		
minlong() Description:	the smallest value that can be stored in storage type long		
Range:	This function takes no arguments, but the parentheses must be included. one integer number		
missing( $x_1$ , $x_2$ ,. Description:	$(x_i, x_n)$ 1 if any $x_i$ evaluates to <i>missing</i> ; otherwise, 0		
Domain $x_i$ :	Stata has two concepts of missing values: a numeric missing value (., .a, .b,, .z) and a string missing value (""). missing() returns 1 (meaning true) if any expression $x_i$ evaluates to missing. If x is numeric, missing(x) is equivalent to $x \ge$ If x is string, missing(x) is equivalent to $x==$ "". any string or numeric expression		
Range:	0 and 1		

r ( <i>name</i> ) Description:	the value of the stored result r ( <i>name</i> ); see [U] <b>18.8 Accessing results calculated by other programs</b>
	r(name) = scalar missing if the stored result does not exist r(name) = specified matrix if the stored result is a matrix r(name) = scalar numeric value if the stored result is a scalar that can be interpreted as a number
Domain: Range:	names strings, scalars, matrices, or <i>missing</i>
recode $(x, x_1, x_2)$ Description:	$\begin{array}{l} (\ldots,x_n) \\ \text{missing if } x_1, x_2, \ldots, x_n \text{ is not weakly increasing; } x \text{ if } x \text{ is missing; } x_1 \text{ if } x \leq x_1; \\ x_2 \text{ if } x \leq x_2, \ldots; \text{ otherwise, } x_n \text{ if } x > x_1, x_2, \ldots, x_{n-1}. \ x_i \geq . \text{ is interpreted as} \\ x_i = +\infty \end{array}$
Domain $x$ : Domain $x_1$ : Domain $x_2$ :	Also see autocode() and irecode() for other styles of recode functions. -8e+307 to $8e+307$ or missing -8e+307 to $8e+307x_1 to 8e+307$
 Domain $x_n$ : Range:	$x_{n-1}$ to 8e+307 $x_1, x_2, \dots, x_n$ or missing
replay() Description:	1 if the first nonblank character of local macro '0' is a comma, or if '0' is empty
Range:	This is a function for use by programmers writing estimation commands; see [P] <b>ereturn</b> . integers 0 and 1, meaning <i>false</i> and <i>true</i> , respectively
return( <i>name</i> ) Description:	the value of the to-be-stored result r ( <i>name</i> ); see [P] return
Domain: Range:	<pre>return(name) = scalar missing if the stored result does not exist return(name) = specified matrix if the stored result is a matrix return(name) = scalar numeric value if the stored result is a scalar names strings, scalars, matrices, or missing</pre>

s ( <i>name</i> ) Description: Domain: Range:	the value of stored result s( <i>name</i> ); see [U] <b>18.8 Accessing results calculated by</b> other programs s( <i>name</i> ) = . if the stored result does not exist names strings or <i>missing</i>	
scalar( <i>exp</i> ) Description:	restricts name interpretation to scalars and matrices	
Domain: Range:	Names in expressions can refer to names of variables in the dataset, names of matrices, or names of scalars. Matrices and scalars can have the same names as variables in the dataset. If names conflict, Stata assumes that you are referring to the name of the variable in the dataset. matrix() and scalar() explicitly state that you are referring to matrices and scalars. matrix() and scalar() are the same function; scalars and matrices may not have the same names and so cannot be confused. Typing scalar(x) makes it clear that you are referring to the scalar or matrix named x and not the variable named x, should there happen to be a variable of that name. any valid expression evaluation of <i>exp</i>	
<pre>smallestdouble()</pre>		
Description:	the smallest double-precision number greater than zero	
Range:	If $0 < d < \texttt{smallestdouble()}$ , then $d$ does not have full double precision; these are called the denormalized numbers. This function takes no arguments, but the parentheses must be included. a double-precision number close to $0$	

## References

Kantor, D., and N. J. Cox. 2005. Depending on conditions: A tutorial on the cond() function. *Stata Journal* 5: 413–420. Rising, W. R. 2010. Stata tip 86: The missing() function. *Stata Journal* 10: 303–304.

## Also see

- [FN] Functions by category
- [D] egen Extensions to generate
- [D] generate Create or change contents of variable
- [M-4] Programming Programming functions
- [U] 13.3 Functions

# **Random-number functions**

	Contents Acknowledgments	Functions References	Remarks and examples Also see	Methods and formulas
Conte	ents			
rbeta	(a,b)	beta( <i>a</i> , <i>b</i> ) shape par		nd $b$ are the beta distribution
rbino	mial(n,p)		(n,p) random variates, wher cess probability	e $n$ is the number of trials and $p$
rcauc	hy(a,b)	• •	(a,b) random variates, where cale parameter	<i>a</i> is the location parameter and
rchi2	(df)	$\chi^2$ , with $a$	df degrees of freedom, rand	lom variates
rexpo	nential(b)	exponent	ial random variates with sca	lle b
rgamm	a( <i>a</i> , <i>b</i> )		<i>b)</i> random variates, where the scale parameter	a is the gamma shape parameter
rhype	rgeometric(N, K, n	) hypergeo	metric random variates	
rigau	ssian(m,a)	inverse G parameter	aussian random variates wir $a$	th mean $m$ and shape
rlapl	ace(m,b)	Laplace( <i>r</i>	n,b) random variates with n	nean $m$ and scale parameter $b$
rlogi	stic()	logistic v	ariates with mean 0 and star	ndard deviation $\pi/\sqrt{3}$
rlogi	<pre>stic(s)</pre>	logistic v	ariates with mean 0, scale $s$	, and standard deviation $s\pi/\sqrt{3}$
rlogi	stic(m,s)	logistic v $s\pi/\sqrt{3}$	ariates with mean $m$ , scale .	s, and standard deviation
rnbin	omial(n,p)	negative	binomial random variates	
rnorm	al()		· · · · · · · · · · · · · · · · · · ·	variates, that is, variates from a and a standard deviation of 1
rnorm	al(m)	the standa	ard deviation is 1	ates, where $m$ is the mean and
	al( <i>m</i> , <i>s</i> )	s is the st	andard deviation	ates, where $m$ is the mean and
	$\operatorname{son}(m)$		n) random variates, where n	
rt(df			t random variates, where $d$	
runif		-	distributed random variate	
	$\operatorname{orm}(a, b)$	•	v distributed random variate	
runif	ormint(a,b)	uniformly	distributed random integer	variates on the interval $[a, b]$

<pre>rweibull(a,b)</pre>	Weibull variates with shape $a$ and scale $b$
rweibull(a, b, g)	Weibull variates with shape $a$ , scale $b$ , and location $g$
<pre>rweibullph(a,b)</pre>	Weibull (proportional hazards) variates with shape $a$ and scale $b$
<pre>rweibullph(a,b,g)</pre>	Weibull (proportional hazards) variates with shape $a$ , scale $b$ , and location $g$

# **Functions**

The term "pseudorandom number" is used to emphasize that the numbers are generated by formulas and are thus not truly random. From now on, we will drop the "pseudo" and just say random numbers.

For information on setting the random-number seed, see [R] set seed.

runiform()	uniformly distributed random variates over the interval $(0, 1)$		
Description:	runiform() can be seeded with the set seed command; see [R] set seed.		
Range:	c(epsdouble) to $1 - c(epsdouble)$		
runiform(a,b	)		
Description:	uniformly distributed random variates over the interval $(a, b)$		
Domain a:	c(mindouble) to c(maxdouble)		
Domain b:	c(mindouble) to c(maxdouble)		
Range:	a + c(epsdouble) to $b - c(epsdouble)$		
runiformint(	runiformint $(a, b)$		
Description:	Description: uniformly distributed random integer variates on the interval $[a, b]$		
Domain <i>a</i> : Domain <i>b</i> : Range:	If a or b is nonintegral, runiformint $(a, b)$ returns runiformint (floor $(a)$ , floor $(b)$ ). $-2^{53}$ to $2^{53}$ (may be nonintegral) $-2^{53}$ to $2^{53}$ (may be nonintegral) $-2^{53}$ to $2^{53}$		
rbeta( <i>a</i> , <i>b</i> ) Description:	beta $(a,b)$ random variates, where $a$ and $b$ are the beta distribution shape parameters		
Description.	Besides using the standard methodology for generating random variates from a given distribution, rbeta() uses the specialized algorithms of Johnk (Gentle 2003), Atkinson and Whittaker (1970, 1976), Devroye (1986), and Schmeiser and Babu (1980).		
Domain <i>a</i> :	0.05 to 1e+5		
Domain <i>b</i> :	0.15 to 1e+5		
Range:	0 to 1 (exclusive)		

rbinomial $(n, p)$ Description: binomial $(n, p)$ random variates, where n is the number of trials and p is the success			
Description	probability		
Domain <i>n</i> : Domain <i>p</i> : Range:	Besides using the standard methodology for generating random variates from a given distribution, rbinomial() uses the specialized algorithms of Kachitvichyanukul (1982), Kachitvichyanukul and Schmeiser (1988), and Kemp (1986). 1 to 1e+11 1e-8 to 1-1e-8 0 to n		
rcauchy (a,b) Description: Domain a: Domain b: Range:	Cauchy $(a,b)$ random variates, where $a$ is the location parameter and $b$ is the scale parameter -1e+300 to 1e+300 1e-100 to 1e+300 c(mindouble) to c(maxdouble)		
rchi2( <i>df</i> ) Description: Domain <i>df</i> : Range:	$\chi^2$ , with $df$ degrees of freedom, random variates 2e-4 to 2e+8 0 to c(maxdouble)		
rexponential Description: Domain <i>b</i> : Range:	(b) exponential random variates with scale b 1e-323 to 8e+307 1e-323 to 8e+307		
rgamma(a,b) Description:	gamma $(a,b)$ random variates, where $a$ is the gamma shape parameter and $b$ is the scale parameter Methods for generating gamma variates are taken from Ahrens and Dieter (1974), Best (1983), and Schmeiser and Lal (1980).		
Domain <i>a</i> : Domain <i>b</i> : Range:	<pre>(1765), and Semilerser and Ear(1960). 1e-4 to 1e+8 c(smallestdouble) to c(maxdouble) 0 to c(maxdouble)</pre>		

rhypergeometric(N,K,n)			
Description:	hypergeometric random variates		
	The distribution parameters are integer valued, where $N$ is the population size, $K$ is the number of elements in the population that have the attribute of interest, and $n$ is the sample size.		
	Besides using the standard methodology for generating random variates from a given distribution, rhypergeometric() uses the specialized algorithms of Kachitvichyanukul (1982) and Kachitvichyanukul and Schmeiser (1985).		
Domain <i>N</i> : Domain <i>K</i> :	2 to 1e+6 1 to $N-1$		
Domain $n$ :	1 to $N-1$		
Range:	$\max(0, n - N + K)$ to $\min(K, n)$		
rigaussian(m,a)			
Description:	inverse Gaussian random variates with mean $m$ and shape parameter $a$		
	rigaussian() is based on a method proposed by Michael, Schucany, and Haas (1976).		
Domain m:	1e-10 to 1000		
Domain <i>a</i> : Range:	0.001 to 1e+10 0 to c(maxdouble)		
Range.			
<pre>rlaplace(m,b)</pre>			
Description:	Laplace $(m,b)$ random variates with mean m and scale parameter b		
Domain <i>m</i> :	-1e+300 to 1e+300		
Domain <i>b</i> : Range:	1e-300 to 1e+300 c(mindouble) to c(maxdouble)		
Range.			
rlogistic()			
Description:	logistic variates with mean 0 and standard deviation $\pi/\sqrt{3}$		
	The variates x are generated by $x = invlogistic(0,1,u)$ , where u is a random uniform(0,1) variate.		
Range:	c(mindouble) to c(maxdouble)		
<pre>rlogistic(s)</pre>			
Description:	logistic variates with mean 0, scale s, and standard deviation $s\pi/\sqrt{3}$		
	The variates x are generated by $x = invlogistic(0, s, u)$ , where u is a random uniform(0,1) variate.		
Domain s:	0 to c(maxdouble)		
Range:	c(mindouble) to c(maxdouble)		

rlogistic( $m, s$ ) Description: logistic variates with mean $m$ , scale $s$ , and standard deviation $s\pi/\sqrt{3}$		
Domain <i>m</i> :	The variates x are generated by $x = invlogistic(m, s, u)$ , where u is a random uniform(0,1) variate. c(mindouble) to c(maxdouble)	
Domain <i>s</i> : Range:	0 to c(maxdouble) c(mindouble) to c(maxdouble)	
rnbinomial(n,p) Description: negative binomial random variates		
Detemption	If $n$ is integer valued, rnbinomial() returns the number of failures before the $n$ th success, where the probability of success on a single trial is $p$ . $n$ can also be nonintegral.	
Domain <i>n</i> : Domain <i>p</i> : Range:	$1e-4 \text{ to } 1e+5$ $1e-4 \text{ to } 1-1e-4$ $0 \text{ to } 2^{53}-1$	
rnormal()		
Description: Range:	standard normal (Gaussian) random variates, that is, variates from a normal distribution with a mean of 0 and a standard deviation of 1 c(mindouble) to c(maxdouble)	
rnormal(m) Description:	normal $(m,1)$ (Gaussian) random variates, where $m$ is the mean and the standard deviation is 1	
Domain <i>m</i> : Range:	c(mindouble) to c(maxdouble) c(mindouble) to c(maxdouble)	
rnormal( <i>m</i> , <i>s</i> ) Description:	normal $(m,s)$ (Gaussian) random variates, where $m$ is the mean and $s$ is the standard deviation	
Domain m:	The methods for generating normal (Gaussian) random variates are taken from Knuth (1998, 122–128); Marsaglia, MacLaren, and Bray (1964); and Walker (1977). c(mindouble) to c(maxdouble)	
Domain s: Range:	0 to c(maxdouble) c(mindouble) to c(maxdouble)	
rpoisson(m) Description:	Poisson $(m)$ random variates, where $m$ is the distribution mean	
Domain <i>m</i> : Range:	Poisson variates are generated using the probability integral transform methods of Kemp and Kemp (1990, 1991) and the method of Kachitvichyanukul (1982). 1e-6 to 1e+11 0 to $2^{53} - 1$	

rt( <i>df</i> ) Description:	Student's $t$ random variates, where $df$ is the degrees of freedom Student's $t$ variates are generated using the method of Kinderman and Monahan (1977, 1980).	
Domain <i>df</i> : Range:	1 to $2^{53} - 1$ c(mindouble) to c(maxdouble)	
rweibull(a,b) Description: Weibull variates with shape a and scale b		
Domain <i>a</i> : Domain <i>b</i> : Range:	The variates x are generated by $x = invweibulltail(a, b, 0, u)$ , where u is a random uniform(0,1) variate. 0.01 to 1e+6 1e-323 to 8e+307 1e-323 to 8e+307	
rweibull $(a, b, g)$ Description: Weibull variates with shape $a$ , scale $b$ , and location $g$		
Domain <i>a</i> : Domain <i>b</i> : Domain <i>g</i> : Range:	The variates x are generated by $x = invweibulltail(a, b, g, u)$ , where u is a random uniform(0,1) variate. 0.01 to 1e+6 1e-323 to 8e+307 -8e+307 to 8e+307 g + c(epsdouble) to 8e+307	
rweibullph(a,b) Description: Weibull (proportional hazards) variates with shape a and scale b		
Domain <i>a</i> : Domain <i>b</i> : Range:	The variates x are generated by $x = invweibullphtail(a,b,0,u)$ , where u is a random uniform(0,1) variate. 0.01 to 1e+6 1e-323 to 8e+307 1e-323 to 8e+307	
rweibullph(a Description:	Weibull (proportional hazards) variates with shape $a$ , scale $b$ , and location $g$	
Domain <i>a</i> : Domain <i>b</i> : Domain <i>g</i> : Range:	The variates x are generated by $x = invweibullphtail(a, b, g, u)$ , where u is a random uniform(0,1) variate. 0.01 to 1e+6 1e-323 to 8e+307 -8e+307 to 8e+307 g + c(epsdouble) to 8e+307	

# **Remarks and examples**

It is ironic that the first thing to note about random numbers is how to make them reproducible. Before using a random-number function, type

### set seed #

where # is any integer between 0 and  $2^{31} - 1$ , inclusive, to draw the same sequence of random numbers. It does not matter which integer you choose as your seed; they are all equally good. See [R] set seed.

runiform() is the basis for all the other random-number functions because all the other random-number functions transform uniform (0, 1) random numbers to the specified distribution.

runiform() implements the 64-bit Mersenne Twister (mt64), the stream 64-bit Mersenne Twister (mt64s), and the 32-bit "keep it simple stupid" (kiss32) random-number generators (RNGs) for generating uniform (0, 1) random numbers. runiform() uses the mt64 RNG by default.

runiform() uses the kiss32 RNG only when the user version is less than 14 or when the RNG has been set to kiss32; see [P] version for details about setting the user version. We recommend that you do not change the default RNG, but see [R] set rng for details.

## Technical note

Although we recommend that you use runiform(), we made generator-specific versions of runiform() available for advanced users who want to hardcode their generator choice. The function runiform\_mt64() always uses the mt64 RNG to generate uniform (0, 1) random numbers, the function runiform\_mt64s() always uses the mt64s RNG to generate uniform (0, 1) random numbers, the function runiform\_kiss32() always uses the kiss32 RNG to generate uniform (0, 1) random numbers. In fact, generator-specific versions are available for all the implemented distributions. For example, rnormal\_mt64(), rnormal\_mt64s, and rnormal\_kiss32() use transforms of mt64, mt64s, and kiss32 uniform variates, respectively, to generate standard normal variates.

## Technical note

Both the mt64 and the kiss32 RNGs produce uniform variates that pass many tests for randomness. Many researchers prefer the mt64 to the kiss32 RNG because the mt64 generator has a longer period and a finer resolution and requires a higher dimension before patterns appear; see Matsumoto and Nishimura (1998).

The mt64 RNG has a period of  $2^{19937} - 1$  and a resolution of  $2^{-53}$ ; see Matsumoto and Nishimura (1998). Each stream of the mt64s RNG contains  $2^{128}$  random numbers, and mt64s has a resolution of  $2^{-53}$ ; see Haramoto et al. (2008). The kiss32 RNG has a period of about  $2^{126}$  and a resolution of  $2^{-32}$ ; see Methods and formulas below.

## Technical note

This technical note explains how to restart a RNG from its current spot.

The current spot in the sequence of a RNG is part of the state of a RNG. If you tell me the state of a RNG, I know where it is in its sequence, and I can compute the next random number. The state of a RNG is a complicated object that requires more space than the integers used to seed a generator. For instance, an mt64 state is a 5011-digit, base-16 number preceded by three letters.

If you want to restart a RNG from where it left off, you should store the current state in a macro and then set the state of the RNG when you want to restart it. For example, suppose we set a seed and draw some random numbers.

```
. set obs 3
Number of observations (_N) was 0, now 3.
. set seed 12345
. generate x = runiform()
. list x
1. .3576297
2. .4004426
3. .6893833
```

We store the state of the RNG so that we can pick up right here in the sequence.

```
. local rngstate "'c(rngstate)'"
```

We draw some more random numbers.

```
. replace x = runiform()
(3 real changes made)
. list x
1. .5597356
2. .5744513
3. .2076905
```

Now, we set the state of the RNG to where it was and draw those same random numbers again.

```
. set rngstate 'rngstate'

. replace x = runiform()

(0 real changes made)

. list x

1. .5597356

2. .5744513

3. .2076905
```

# Methods and formulas

All the nonuniform generators are based on the uniform mt64, mt64s, and kiss32 RNGs.

The mt64 RNG is well documented in Matsumoto and Nishimura (1998) and on their website http://www.math.sci.hiroshima-u.ac.jp/~m-mat/MT/emt.html. The mt64 RNG implements the 64-bit version discussed at http://www.math.sci.hiroshima-u.ac.jp/~m-mat/MT/emt64.html. The mt64s RNG is based on a method proposed by Haramoto et al. (2008). The default seed of all three RNGs is 123456789.

### kiss32 generator

The kiss32 uniform RNG implemented in runiform() is based on George Marsaglia's (G. Marsaglia, 1994, pers. comm.) 32-bit pseudorandom-integer generator kiss32. The integer kiss32 RNG is composed of two 32-bit pseudorandom-integer generators and two 16-bit integer generators (combined

to make one 32-bit integer generator). The four generators are defined by the recursions

$$x_n = 69069 x_{n-1} + 1234567 \mod 2^{32} \tag{1}$$

$$y_n = y_{n-1}(I + L^{13})(I + R^{17})(I + L^5)$$
(2)

$$z_n = 65184(z_{n-1} \bmod 2^{16}) + \operatorname{int}(z_{n-1}/2^{16}) \tag{3}$$

$$w_n = 63663(w_{n-1} \bmod 2^{16}) + \operatorname{int}(w_{n-1}/2^{16}) \tag{4}$$

In (2), the 32-bit word  $y_n$  is viewed as a 1 × 32 binary vector; L is the 32 × 32 matrix that produces a left shift of one (L has 1s on the first left subdiagonal, 0s elsewhere); and R is L transpose, affecting a right shift by one. In (3) and (4), int(x) is the integer part of x.

The integer kiss32 RNG produces the 32-bit random integer

$$R_n = x_n + y_n + z_n + 2^{16} w_n \mod 2^{32}$$

The kiss32 uniform RNG implemented in runiform() takes the output from the integer kiss32 RNG and divides it by  $2^{32}$  to produce a real number on the interval (0, 1). (Zeros are discarded, and the first nonzero result is returned.)

The recursion (5)-(8) have, respectively, the periods

$$2^{32}$$
 (5)

$$2^{32} - 1$$
 (6)

$$(65184 \cdot 2^{16} - 2)/2 \approx 2^{31} \tag{7}$$

$$(63663 \cdot 2^{16} - 2)/2 \approx 2^{31}$$
(8)

Thus the overall period for the integer kiss32 RNG is

$$2^{32} \cdot (2^{32} - 1) \cdot (65184 \cdot 2^{15} - 1) \cdot (63663 \cdot 2^{15} - 1) \approx 2^{126}$$

When Stata first comes up, it initializes the four recursions in kiss32 by using the seeds

$$\begin{array}{l} x_0 = 123456789 \\ y_0 = 521288629 \\ z_0 = 362436069 \\ w_0 = 2262615 \end{array}$$

Successive calls to the kiss32 uniform RNG implemented in runiform() then produce the sequence

$$\frac{R_1}{2^{32}}, \frac{R_2}{2^{32}}, \frac{R_3}{2^{32}}, \dots$$

Hence, the kiss32 uniform RNG implemented in runiform() gives the same sequence of random numbers in every Stata session (measured from the start of the session) unless you reinitialize the seed. The full seed is the set of four numbers (x, y, z, w), but you can reinitialize the seed by simply issuing the command

. set seed #

where # is any integer between 0 and  $2^{31} - 1$ , inclusive. When this command is issued, the initial value  $x_0$  is set equal to #, and the other three recursions are restarted at the seeds  $y_0$ ,  $z_0$ , and  $w_0$  given above. The first 100 random numbers are discarded, and successive calls to the kiss32 uniform RNG implemented in runiform() give the sequence

$$\frac{R'_{101}}{2^{32}}, \frac{R'_{102}}{2^{32}}, \frac{R'_{103}}{2^{32}}, \dots$$

However, if the command

. set seed 123456789

is given, the first 100 random numbers are not discarded, and you get the same sequence of random numbers that the kiss32 RNG produces when Stata restarts; also see [R] set seed.

## Acknowledgments

We thank the late George Marsaglia, formerly of Florida State University, for providing his kiss32 RNG.

We thank John R. Gleason (retired) of Syracuse University for directing our attention to Wichura (1988) for calculating the cumulative normal density accurately, for sharing his experiences about techniques with us, and for providing C code to make the calculations.

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### Also see

- [FN] Functions by category
- [D] egen Extensions to generate
- [D] generate Create or change contents of variable
- [R] set rng Set which random-number generator (RNG) to use
- [R] set rngstream Specify the stream for the stream random-number generator
- [R] set seed Specify random-number seed and state
- [M-5] runiform() Uniform and nonuniform pseudorandom variates
- [U] 13.3 Functions

# Selecting time-span functions

Contents Functions Also see

## Contents

$tin(d_1, d_2)$	true if $d_1 \leq t \leq d_2$ , where t is the time variable previously tsset
$\texttt{twithin}(d_1, d_2)$	true if $d_1 < t < d_2$ , where t is the time variable previously tsset

# **Functions**

$tin(d_1, d_2)$ Description:	true if $d_1 \leq t \leq d_2$ , where t is the time variable previously tsset
Decomption	You must have previously tsset the data to use tin(); see [TS] <b>tsset</b> . When you tsset the data, you specify a time variable, $t$ , and the format on $t$ states how it is recorded. You type $d_1$ and $d_2$ according to that format.
	If $t$ has a %tc format, you could type tin(5jan1992 11:15, 14apr2002 12:25).
	If $t$ has a %td format, you could type tin(5jan1992, 14apr2002).
	If t has a %tw format, you could type tin(1985w1, 2002w15).
	If t has a %tm format, you could type tin(1985m1, 2002m4).
	If t has a %tq format, you could type tin(1985q1, 2002q2).
	If t has a %th format, you could type tin(1985h1, 2002h1).
	If t has a %ty format, you could type tin(1985, 2002).
	If $t$ has a %tb format, you could type tin(5jan1992, 14apr2002). This will work as expected even if the arguments of tin() are not business days.
	Otherwise, $t$ is just a set of integers, and you could type tin(12, 38).
	The details of the $t$ format do not matter. If your $t$ is formatted $t dmm/dd/yy$ so that 5jan1992 displays as 1/5/92, you would still type the date in day-month-year order: tin(5jan1992, 14apr2002).
$\text{Domain}\ d_1:$	date or time literals or strings recorded in units of $t$ previously tsset or blank to
Domain $d_2$ :	indicate no minimum date date or time literals or strings recorded in units of $t$ previously tsset or blank to
Range:	indicate no maximum date 0 and 1, $1 \Rightarrow true$

<code>twithin(<math>d_1</math>,<math>d</math></code>	2)
Description:	true if $d_1 < t < d_2$ , where t is the time variable previously <code>tsset</code>
	See tin() above; twithin() is similar, except the range is exclusive.
Domain $d_1$ :	date or time literals or strings recorded in units of $t$ previously tsset or blank to
	indicate no minimum date
Domain $d_2$ :	date or time literals or strings recorded in units of $t$ previously tsset or blank to
	indicate no maximum date
Range:	0 and 1, 1 $\Rightarrow$ true

# Also see

- [FN] Functions by category
- [D] egen Extensions to generate
- [D] generate Create or change contents of variable
- [U] 13.3 Functions

## **Statistical functions**

	Contents	Functions	References	Also see
Contents				
betaden(a,b,x)			lensity of the bet rs; 0 if $x < 0$ or a	ta distribution, where $a$ and $b$ are the $r > 1$
$binomial(n,k,\theta)$	th fl	e probability of	of observing flo when the proba	or (k) or fewer successes in bility of a success on one trial is $\theta$ ; 0
binomialp(n,k,p)	th	e probability o	of observing flo	or (k) successes in floor (n) trials s on one trial is $p$
binomialtail( $n, k, \theta$ )	th fl	e probability o	of observing flo when the proba	or $(k)$ or more successes in bility of a success on one trial is $\theta$ ; 1
$binormal(h,k,\rho)$	th			$\Phi(h,k,\rho)$ of bivariate normal with
cauchy(a,b,x)	th			ion with location parameter $a$ and
cauchyden(a,b,x)	th	e probability d		uchy distribution with location $b$
cauchytail(a,b,x)	th	e reverse cum	-	il or survivor) Cauchy distribution
chi2(df, x)	the	-		with $df$ degrees of freedom; 0 if
chi2den(df, x)	th		•	distribution with $df$ degrees of
chi2tail(df,x)	the	e reverse cum		il or survivor) $\chi^2$ distribution with 0
dgammapda(a,x)	$\frac{\partial I}{\partial t}$	$\frac{P(a,x)}{\partial a}$ , where $a$	P(a,x) = gamma	ap(a, x); 0  if  x < 0
dgammapdada(a,x)	$\frac{\partial^2}{\partial t}$	$\frac{P(a,x)}{\partial a^2}$ , where	P(a,x) = gamm	$ap(a,x); 0  ext{ if } x < 0$
dgammapdadx(a,x)	$\frac{\partial^2}{\partial t}$	$\frac{P(a,x)}{\partial a \partial x}$ , where	P(a,x) = gamm	$ap(a,x); 0  ext{ if } x < 0$
dgammapdx(a,x)				$ap(a, x); 0  ext{ if } x < 0$
dgammapdxdx(a,x)	$\frac{\partial^2}{\partial t}$	$\frac{P(a,x)}{\partial x^2}$ , where	P(a, x) = gamm	$ap(a,x); 0  ext{ if } x < 0$
dunnettprob( $k, df, x$ )	th m	e cumulative 1	nultiple range di rison method wi	stribution that is used in Dunnett's th $k$ ranges and $df$ degrees of
exponential(b, x)				ibution with scale b
exponentialden(b, x)			lensity function	of the exponential distribution with
exponentialtail(b,x		ale <i>b</i> e reverse cum	ulative exponent	tial distribution with scale b
$F(df_1, df_2, f)$	th de	nominator deg	grees of freedom	th $df_1$ numerator and $df_2$ a: , $df_2$ ,t) $dt$ ; 0 if $f < 0$
	1 (		$J_0$	, wj2, 0, w0, 0 m j < 0

$\mathtt{Fden}(df_1, df_2, f)$	the probability density function of the F distribution with $df_1$
$\texttt{Ftail}(df_1, df_2, f)$	numerator and $df_2$ denominator degrees of freedom; 0 if $f < 0$ the reverse cumulative (upper tail or survivor) $F$ distribution with $df_1$ numerator and $df_2$ denominator degrees of freedom; 1 if $f < 0$
gammaden(a, b, g, x)	the probability density function of the gamma distribution; 0 if $x < g$
gammap(a, x)	the cumulative gamma distribution with shape parameter $a$ ; 0 if
<pre>gammaptail(a,x)</pre>	x < 0 the reverse cumulative (upper tail or survivor) gamma distribution with shape parameter <i>a</i> ; 1 if $x < 0$
hypergeometric( $N, K, n, k$ )	the cumulative probability of the hypergeometric distribution
hypergeometricp $(N, K, n, k)$	the hypergeometric probability of $k$ successes out of a sample of size $n$ , from a population of size $N$ containing $K$ elements that have the
ibeta(a,b,x)	attribute of interest the cumulative beta distribution with shape parameters $a$ and $b$ ; 0 if x < 0; or 1 if $x > 1$
<pre>ibetatail(a,b,x)</pre>	the reverse cumulative (upper tail or survivor) beta distribution with shape parameters $a$ and $b$ ; 1 if $x < 0$ ; or 0 if $x > 1$
igaussian(m,a,x)	the cumulative inverse Gaussian distribution with mean $m$ and shape parameter $a$ ; 0 if $x \le 0$
igaussianden(m,a,x)	the probability density of the inverse Gaussian distribution with mean $m$ and shape parameter $a$ ; 0 if $x \le 0$
<pre>igaussiantail(m,a,x)</pre>	the reverse cumulative (upper tail or survivor) inverse Gaussian distribution with mean $m$ and shape parameter $a$ ; 1 if $x \le 0$
invbinomial(n,k,p)	the inverse of the cumulative binomial; that is, $\theta$ ( $\theta$ = probability of success on one trial) such that the probability of observing floor(k) or fewer successes in floor(n) trials is p
<pre>invbinomialtail(n,k,p)</pre>	the inverse of the right cumulative binomial; that is, $\theta$ ( $\theta$ = probability of success on one trial) such that the probability of observing floor(k) or more successes in floor(n) trials is p
invcauchy(a,b,p)	the inverse of cauchy(): if cauchy( $a, b, x$ ) = $p$ , then invcauchy( $a, b, p$ ) = $x$
<pre>invcauchytail(a,b,p)</pre>	the inverse of cauchytail(): if cauchytail( $a, b, x$ ) = $p$ , then invcauchytail( $a, b, p$ ) = $x$
<pre>invchi2(df,p)</pre>	the inverse of chi2(): if chi2( $df, x$ ) = $p$ , then invchi2( $df, p$ ) = $x$
invchi2tail(df,p)	the inverse of chi2tail(): if chi2tail( $df, x$ ) = $p$ , then invchi2tail( $df, p$ ) = $x$
invdunnettprob(k, df, p)	the inverse cumulative multiple range distribution that is used in Dunnett's multiple-comparison method with $k$ ranges and $df$ degrees of freedom
invexponential(b,p)	the inverse cumulative exponential distribution with scale b: if exponential $(b, x) = p$ , then invexponential $(b, p) = x$
<pre>invexponentialtail(b,p)</pre>	the inverse reverse cumulative exponential distribution with scale $b$ : if exponentialtail( $b, x$ ) = $p$ , then
$\texttt{invF}(df_1, df_2, p)$	invexponentialtail( $b, p$ ) = $x$ the inverse cumulative $F$ distribution: if $F(df_1, df_2, f) = p$ , then inv $F(df_1, df_2, p) = f$

 $invFtail(df_1, df_2, p)$ the inverse reverse cumulative (upper tail or survivor) F distribution: if Ftail( $df_1$ ,  $df_2$ , f) = p, then invFtail( $df_1$ ,  $df_2$ , p) = fthe inverse cumulative gamma distribution: if gammap(a, x) = p, invgammap(a,p) then invgammap(a, p) = xthe inverse reverse cumulative (upper tail or survivor) gamma invgammaptail(a,p) distribution: if gammaptail (a, x) = p, then invgammaptail (a, p)= xinvibeta(a, b, p)the inverse cumulative beta distribution: if ibeta(a, b, x) = p, then invibeta(a, b, p) = xinvibetatail(*a*,*b*,*p*) the inverse reverse cumulative (upper tail or survivor) beta distribution: if ibetatail(a, b, x) = p, then invibetatail(a,b,p) = xthe inverse of igaussian(): if invigaussian(m,a,p)igaussian(m,a,x) = p, then invigaussian(m,a,p) = xinvigaussiantail(m,a,p) the inverse of igaussiantail(): if igaussiantail(m, a, x) = p, then invigaussiantail(m,a,p) = xinvlaplace(m,b,p)the inverse of laplace(): if laplace(m, b, x) = p, then invlaplace(m, b, p) = xinvlaplacetail(m, b, p)the inverse of laplacetail(): if laplacetail(m, b, x) = p, then invlaplacetail(m, b, p) = xinvlogistic(p) the inverse cumulative logistic distribution: if logistic(x) = p, then invlogistic(p) = xthe inverse cumulative logistic distribution: if logistic(s, x) = p, invlogistic(s,p)then invlogistic(s, p) = xinvlogistic(m,s,p)the inverse cumulative logistic distribution: if logistic(m, s, x)= p, then invlogistic(m, s, p) = xinvlogistictail(p) the inverse reverse cumulative logistic distribution: if logistictail(x) = p, then invlogistictail(p) = xthe inverse reverse cumulative logistic distribution: if invlogistictail(s,p) logistictail(s, x) = p, then invlogistictail(s, p) = xthe inverse reverse cumulative logistic distribution: if invlogistictail(m,s,p) logistictail(m,s,x) = p, then invlogistictail(m,s,p) = xinvnbinomial(n,k,q)the value of the negative binomial parameter, p, such that q = nbinomial(n, k, p)the value of the negative binomial parameter, p, such that invnbinomialtail(n,k,q)q = nbinomialtail(n, k, p)the inverse cumulative noncentral  $\chi^2$  distribution: if invnchi2(df, np, p)nchi2(df, np, x) = p, then invnchi2(df, np, p) = xthe inverse reverse cumulative (upper tail or survivor) noncentral  $\chi^2$ invnchi2tail(df, np, p)distribution: if nchi2tail(df, np, x) = p, then invnchi2tail(df, np, p) = x $invnF(df_1, df_2, np, p)$ the inverse cumulative noncentral F distribution: if  $nF(df_1, df_2, np, f) = p$ , then  $invnF(df_1, df_2, np, p) = f$  $invnFtail(df_1, df_2, np, p)$ the inverse reverse cumulative (upper tail or survivor) noncentral Fdistribution: if nFtail( $df_1$ ,  $df_2$ , np, f) = p, then  $invnFtail(df_1, df_2, np, p) = f$ 

<pre>invnibeta(a,b,np,p)</pre>	the inverse cumulative noncentral beta distribution: if
	$\mathtt{nibeta}(a,b,np,x) = p, \mathtt{then invibeta}(a,b,np,p) = x$
<pre>invnormal(p)</pre>	the inverse cumulative standard normal distribution: if normal(z) = $p$ , then invnormal( $p$ ) = $z$
invnt(df, np, p)	the inverse cumulative noncentral Student's $t$ distribution: if
0 - 1 - 1	nt(df, np, t) = p, then $invnt(df, np, p) = t$
invnttail(df, np, p)	the inverse reverse cumulative (upper tail or survivor) noncentral Student's t distribution: if $nttail(df, np, t) = p$ , then
	invnttail(df, np, p) = t
invpoisson(k,p)	the Poisson mean such that the cumulative Poisson distribution
	evaluated at k is p: if $poisson(m,k) = p$ , then $invpoisson(k,p) = m$
invpoissontail(k,q)	the Poisson mean such that the reverse cumulative Poisson
	distribution evaluated at $k$ is $q$ : if poissontail( $m, k$ ) = $q$ , then invpoissontail( $k, q$ ) = $m$
invt(df,p)	the inverse cumulative Student's t distribution: if $t(df, t) = p$ , then
	invt(df,p) = t
invttail(df,p)	the inverse reverse cumulative (upper tail or survivor) Student's
	t distribution: if ttail( $df$ , $t$ ) = $p$ , then invttail( $df$ , $p$ ) = $t$
invtukeyprob(k, df, p)	the inverse cumulative Tukey's Studentized range distribution with $k$
	ranges and $df$ degrees of freedom
<pre>invweibull(a,b,p)</pre>	the inverse cumulative Weibull distribution with shape <i>a</i> and scale <i>b</i> :
	if weibull( $a, b, x$ ) = $p$ , then invweibull( $a, b, p$ ) = $x$
<pre>invweibull(a,b,g,p)</pre>	the inverse cumulative Weibull distribution with shape $a$ , scale $b$ ,
	and location g: if weibull $(a, b, g, x) = p$ , then
	invweibull $(a,b,g,p) = x$
<pre>invweibullph(a,b,p)</pre>	the inverse cumulative Weibull (proportional hazards) distribution
* · · · *	with shape a and scale b: if weibullph( $a, b, x$ ) = p, then
	invweibullph(a,b,p) = x
<pre>invweibullph(a,b,g,p)</pre>	the inverse cumulative Weibull (proportional hazards) distribution
	with shape a, scale b, and location g: if weibullph( $a, b, g, x$ ) = p,
	then invweibullph( $a, b, g, p$ ) = $x$
<pre>invweibullphtail(a,b,p)</pre>	the inverse reverse cumulative Weibull (proportional hazards)
	distribution with shape $a$ and scale $b$ : if
	weibullphtail( $a, b, x$ ) = $p$ , then
	invweibullphtail(a,b,p) = x
<pre>invweibullphtail(a,b,g,p)</pre>	the inverse reverse cumulative Weibull (proportional hazards)
	distribution with shape $a$ , scale $b$ , and location $g$ : if
	weibullphtail( $a, b, g, x$ ) = $p$ , then
	invweibullphtail(a, b, g, p) = x
invweibulltail(a,b,p)	the inverse reverse cumulative Weibull distribution with shape $a$ and
	scale b: if weibulltail( $a, b, x$ ) = $p$ , then
	invweibulltail(a,b,p) = x
<pre>invweibulltail(a,b,g,p)</pre>	the inverse reverse cumulative Weibull distribution with shape $a$ ,
	scale $b$ , and location $g$ : if weibulltail( $a$ , $b$ , $g$ , $x$ ) = $p$ , then
	invweibulltail( $a, b, g, p$ ) = $x$
laplace(m,b,x)	the cumulative Laplace distribution with mean $m$ and scale
	parameter b

laplaceden(m,b,x)	the probability density of the Laplace distribution with mean $m$ and scale parameter $b$
<pre>laplacetail(m,b,x)</pre>	the reverse cumulative (upper tail or survivor) Laplace distribution with mean $m$ and scale parameter $b$
lncauchyden(a,b,x)	the natural logarithm of the density of the Cauchy distribution with location parameter $a$ and scale parameter $b$
lnigammaden(a,b,x)	the natural logarithm of the inverse gamma density, where $a$ is the shape parameter and $b$ is the scale parameter
lnigaussianden(m,a,x)	the natural logarithm of the inverse Gaussian density with mean $m$ and shape parameter $a$
lniwishartden(df, V, X)	the natural logarithm of the density of the inverse Wishart distribution; missing if $df \le n-1$
lnlaplaceden(m,b,x)	the natural logarithm of the density of the Laplace distribution with mean $m$ and scale parameter $b$
lnmvnormalden(M,V,X)	the natural logarithm of the multivariate normal density
lnnormal(z)	the natural logarithm of the cumulative standard normal distribution
lnnormalden(z)	the natural logarithm of the standard normal density, $N(0, 1)$
$lnnormalden(x,\sigma)$	the natural logarithm of the normal density with mean 0 and standard deviation $\sigma$
lnnormalden( $x, \mu, \sigma$ )	the natural logarithm of the normal density with mean $\mu$ and standard deviation $\sigma, N(\mu, \sigma^2)$
lnwishartden(df,V,X)	the natural logarithm of the density of the Wishart distribution; missing if $df \le n-1$
<pre>logistic(x)</pre>	the cumulative logistic distribution with mean 0 and standard deviation $\pi/\sqrt{3}$
<pre>logistic(s,x)</pre>	the cumulative logistic distribution with mean 0, scale s, and standard deviation $s\pi/\sqrt{3}$
logistic(m,s,x)	the cumulative logistic distribution with mean m, scale s, and standard deviation $s\pi/\sqrt{3}$
logisticden(x)	the density of the logistic distribution with mean 0 and standard deviation $\pi/\sqrt{3}$
<pre>logisticden(s,x)</pre>	the density of the logistic distribution with mean 0, scale s, and standard deviation $s\pi/\sqrt{3}$
<pre>logisticden(m,s,x)</pre>	the density of the logistic distribution with mean m, scale s, and standard deviation $s\pi/\sqrt{3}$
<pre>logistictail(x)</pre>	the reverse cumulative logistic distribution with mean 0 and standard deviation $\pi/\sqrt{3}$
<pre>logistictail(s,x)</pre>	the reverse cumulative logistic distribution with mean 0, scale s, and standard deviation $s\pi/\sqrt{3}$
<pre>logistictail(m,s,x)</pre>	the reverse cumulative logistic distribution with mean $m$ , scale $s$ , and standard deviation $s\pi/\sqrt{3}$
nbetaden(a,b,np,x)	the probability density function of the noncentral beta distribution; 0 if $x<0 \mbox{ or } x>1$
nbinomial(n,k,p)	the cumulative probability of the negative binomial distribution
nbinomialp(n,k,p)	the negative binomial probability
nbinomialtail(n,k,p)	the reverse cumulative probability of the negative binomial distribution

nchi2(df, np, x)
nchi2den(df, np, x)
nchi2tail(df, np, x)
$\texttt{nF}(df_1, df_2, np, f)$
$\texttt{nFden}(df_1, df_2, np, f)$
$\texttt{nFtail}(df_1, df_2, np, f)$
nibeta(a,b,np,x)
normal(z)
normalden( $z$ )
normalden $(x,\sigma)$
normalden $(x, \mu, \sigma)$ npnchi2 $(df, x, p)$
nphemiz(aj, a, p)
$\texttt{npnF}(df_1, df_2, f, p)$
$\mathtt{npnt}(df,t,p)$
$\mathtt{nt}(df, np, t)$
ntden(df, np, t)
<pre>nttail(df,np,t)</pre>
<pre>poisson(m,k)</pre>
poissonp(m,k)
poissontail(m,k)
t(df,t)
tden(df,t)
ttail(df,t)
tukeyprob(k, df, x)
weibull(a,b,x)
weibull( $a, b, g, x$ )

the sumulative concentral $a^2$ distributions 0 if $a < 0$
the cumulative noncentral $\chi^2$ distribution; 0 if $x < 0$
the probability density of the noncentral $\chi^2$ distribution; 0 if $x < 0$
the reverse cumulative (upper tail or survivor) noncentral $\chi^2$ distribution; 1 if $x < 0$
the cumulative noncentral $F$ distribution with $df_1$ numerator and
$df_2$ denominator degrees of freedom and noncentrality parameter $np$ ; 0 if $f < 0$
the probability density function of the noncentral $F$ distribution with
$df_1$ numerator and $df_2$ denominator degrees of freedom and noncentrality parameter $np$ ; 0 if $f < 0$
the reverse cumulative (upper tail or survivor) noncentral $F$
distribution with $df_1$ numerator and $df_2$ denominator degrees of
freedom and noncentrality parameter $np$ ; 1 if $f < 0$
the cumulative noncentral beta distribution; 0 if $x < 0$ ; or 1 if $x > 1$
the cumulative standard normal distribution
the standard normal density, $N(0, 1)$
the normal density with mean 0 and standard deviation $\sigma$
the normal density with mean $\mu$ and standard deviation $\sigma, N(\mu, \sigma^2)$
the noncentrality parameter, $np$ , for noncentral $\chi^2$ : if
nchi2(df, np, x) = p, then $npnchi2(df, x, p) = np$
the noncentrality parameter, $np$ , for the noncentral $F$ : if
$nF(df_1, df_2, np, f) = p$ , then $npnF(df_1, df_2, f, p) = np$
the noncentrality parameter, $np$ , for the noncentral Student's
t distribution: if $nt(df, np, t) = p$ , then $npnt(df, t, p) = np$
the cumulative noncentral Student's $t$ distribution with $df$ degrees of
freedom and noncentrality parameter np
the probability density function of the noncentral Student's
t distribution with $df$ degrees of freedom and noncentrality
parameter np
the reverse cumulative (upper tail or survivor) noncentral Student's $t$ distribution with $df$ degrees of freedom and noncentrality
parameter <i>np</i>
the probability of observing $floor(k)$ or fewer outcomes that are
distributed as Poisson with mean $m$ the probability of observing floor(k) outcomes that are distributed
as Poisson with mean $m$ the probability of observing floor (k) or more outcomes that are
distributed as Poisson with mean $m$
the cumulative Student's $t$ distribution with $df$ degrees of freedom
the probability density function of Student's $t$ distribution
the reverse cumulative (upper tail or survivor) Student's $t$ distribution; the probability $T > t$
the cumulative Tukey's Studentized range distribution with $k$ ranges
and $df$ degrees of freedom; 0 if $x < 0$
the cumulative Weibull distribution with shape $a$ and scale $b$
the cumulative Weibull distribution with shape $a$ , scale $b$ , and location $g$
5

weibullden $(a, b, x)$	the probability density function of the Weibull distribution with shape $a$ and scale $b$
weibullden(a,b,g,x)	the probability density function of the Weibull distribution with shape $a$ , scale $b$ , and location $g$
weibullph(a,b,x)	the cumulative Weibull (proportional hazards) distribution with shape $a$ and scale $b$
<pre>weibullph(a,b,g,x)</pre>	the cumulative Weibull (proportional hazards) distribution with shape $a$ , scale $b$ , and location $g$
weibullphden( $a, b, x$ )	the probability density function of the Weibull (proportional hazards) distribution with shape $a$ and scale $b$
weibullphden( $a, b, g, x$ )	the probability density function of the Weibull (proportional hazards) distribution with shape $a$ , scale $b$ , and location $g$
<pre>weibullphtail(a,b,x)</pre>	the reverse cumulative Weibull (proportional hazards) distribution with shape $a$ and scale $b$
<pre>weibullphtail(a,b,g,x)</pre>	the reverse cumulative Weibull (proportional hazards) distribution with shape $a$ , scale $b$ , and location $g$
weibulltail( $a, b, x$ )	the reverse cumulative Weibull distribution with shape $a$ and scale $b$
weibulltail( $a, b, g, x$ )	the reverse cumulative Weibull distribution with shape $a$ , scale $b$ , and location $g$

### **Functions**

Statistical functions are listed alphabetically under the following headings:

Beta and noncentral beta distributions **Binomial distribution** Cauchy distribution  $\chi^2$  and noncentral  $\chi^2$  distributions Dunnett's multiple range distribution Exponential distribution F and noncentral F distributions Gamma distribution Hypergeometric distribution Inverse Gaussian distribution Laplace distribution Logistic distribution Negative binomial distribution Normal (Gaussian), binormal, and multivariate normal distributions Poisson distribution Student's t and noncentral Student's t distributions Tukey's Studentized range distribution Weibull distribution Weibull (proportional hazards) distribution Wishart distribution

### Beta and noncentral beta distributions

betaden(a,b,x)

Description:

the probability density of the beta distribution, where a and b are the shape parameters; 0 if x < 0 or x > 1

The probability density of the beta distribution is

$$\texttt{betaden}(a,b,x) = \frac{x^{a-1}(1-x)^{b-1}}{\int_0^\infty t^{a-1}(1-t)^{b-1}dt} = \frac{\Gamma(a+b)}{\Gamma(a)\Gamma(b)}x^{a-1}(1-x)^{b-1}dt$$

Domain a:	1e-323 to 8e+307
Domain b:	1e-323 to 8e+307
Domain x:	$-8e+307$ to $8e+307$ ; interesting domain is $0 \le x \le 1$
Range:	0 to 8e+307

ibeta(a,b,x)

Description: the cumulative beta distribution with shape parameters a and b; 0 if x < 0; or 1 if x > 1

The cumulative beta distribution with shape parameters a and b is defined by

$$I_x(a,b)=\frac{\Gamma(a+b)}{\Gamma(a)\Gamma(b)}\int_0^x t^{a-1}(1-t)^{b-1}\,dt$$

ibeta() returns the regularized incomplete beta function, also known as the incomplete beta function ratio. The incomplete beta function without regularization is given by (gamma(a)\*gamma(b)/gamma(a+b))\*ibeta(a,b,x) or, better when a or b might be large, exp(lngamma(a)+lngamma(b)-lngamma(a+b))\*ibeta(a,b,x).

Here is an example of the use of the regularized incomplete beta function. Although Stata has a cumulative binomial function (see binomial()), the probability that an event occurs k or fewer times in n trials, when the probability of one event is p, can be evaluated as cond(k==n,1,1-ibeta(k+1,n-k,p)). The reverse cumulative binomial (the probability that an event occurs k or more times) can be evaluated as cond(k==0,1,ibeta(k,n-k+1,p)). See Press et al. (2007, 270–273) for a more complete description and for suggested uses for this function.

Domain a:	1e-10 to $1e+17$
Domain b:	1e-10 to 1e+17
Domain x:	$-8e+307$ to $8e+307$ ; interesting domain is $0 \le x \le 1$
Range:	0 to 1

ibetatail(a,b,x)

Description: the reverse cumulative (upper tail or survivor) beta distribution with shape parameters a and b; 1 if x < 0; or 0 if x > 1

The reverse cumulative (upper tail or survivor) beta distribution with shape parameters a and b is defined by

$$\texttt{ibetatail}(a,b,x) = 1 - \texttt{ibeta}(a,b,x) = \int_x^1 \texttt{betaden}(a,b,t) \, dt$$

invibeta( <i>a</i> , <i>b</i> , <i>p</i> )		
Description:	the inverse cumulative beta distribution: if $ibeta(a,b,x) = p$ ,	
	then invibeta( $a, b, p$ ) = $x$	
Domain <i>a</i> :	1e-10 to 1e+17	
Domain b:	1e-10 to 1e+17	
Domain <i>p</i> :	0 to 1	
Range:	0 to 1	

<pre>invibetatail(a,b,p)</pre>		
Description:	the inverse reverse cumulative (upper tail or survivor) beta distribution: if	
Domain <i>a</i> :	ibetatail( $a, b, x$ ) = $p$ , then invibetatail( $a, b, p$ ) = $x$ le-10 to le+17	
Domain <i>b</i> :	1e-10 to 1e+17	
Domain <i>p</i> :	0 to 1	
Range:	0 to 1	

nbetaden(a, b, np, x)

Description: the probability density function of the noncentral beta distribution; 0 if x < 0 or x > 1

The probability density function of the noncentral beta distribution is defined as

$$\sum_{j=0}^{\infty} \frac{e^{-np/2} (np/2)^j}{\Gamma(j+1)} \left\{ \frac{\Gamma(a+b+j)}{\Gamma(a+j)\Gamma(b)} x^{a+j-1} (1-x)^{b-1} \right\}$$

where a and b are shape parameters, np is the noncentrality parameter, and x is the value of a beta random variable.

nbetaden(a, b, 0, x) = betaden(a, b, x), but betaden() is the preferred function to use for the central beta distribution. nbetaden() is computed using an algorithm described in Johnson, Kotz, and Balakrishnan (1995).

Domain <i>a</i> :	1e-323 to $8e+307$
Domain <i>b</i> :	1e-323 to 8e+307
Domain np:	0 to 1,000
Domain $x$ :	$-8e+307$ to $8e+307$ ; interesting domain is $0 \le x \le 1$
Range:	0 to 8e+307

nibeta (a, b, np, x)Description: the cumulative noncentral beta distribution; 0 if x < 0; or 1 if x > 1

The cumulative noncentral beta distribution is defined as

$$I_x(a,b,np) = \sum_{j=0}^{\infty} \frac{e^{-np/2}(np/2)^j}{\Gamma(j+1)} I_x(a+j,b)$$

	where $a$ and $b$ are shape parameters, $np$ is the noncentrality parameter, $x$ is the value of a beta random variable, and $I_x(a, b)$ is the cumulative beta distribution, ibeta().
	nibeta(a,b,0,x) = ibeta(a,b,x), but $ibeta()$ is the preferred function to use for
	the central beta distribution. nibeta() is computed using an algorithm described in
	Johnson, Kotz, and Balakrishnan (1995).
Domain a:	1e-323 to 8e+307
Domain <i>b</i> :	1e-323 to 8e+307
Domain np:	0 to 10,000
Domain x:	$-8e+307$ to $8e+307$ ; interesting domain is $0 \le x \le 1$
Range:	0 to 1

## **Binomial distribution**

<pre>binomialp(n, Description: Domain n: Domain k: Domain p: Range:</pre>	<pre>k,p) the probability of observing floor(k) successes in floor(n) trials when the probability of a success on one trial is p 1 to 1e+6 0 to n 0 to 1 0 to 1</pre>		
binomial(n,k Description:	the probability of observing $floor(k)$ or fewer successes in $floor(n)$ trials when		
Domain <i>n</i> :	the probability of a success on one trial is $\theta$ ; 0 if $k < 0$ ; or 1 if $k > n$ 0 to 1e+17		
Domain $h$ :	$-8e+307$ to $8e+307$ ; interesting domain is $0 \le k < n$		
Domain $\theta$ :	0 to 1		
Range:	0 to 1		
binomialtail Description: Domain $n$ : Domain $k$ : Domain $\theta$ : Range:	$(n, k, \theta)$ the probability of observing floor $(k)$ or more successes in floor $(n)$ trials when the probability of a success on one trial is $\theta$ ; 1 if $k < 0$ ; or 0 if $k > n$ 0 to 1e+17 -8e+307 to 8e+307; interesting domain is $0 \le k < n$ 0 to 1 0 to 1		
invbinomial(	invbinomial(n,k,p)		
Description:	the inverse of the cumulative binomial; that is, $\theta$ ( $\theta$ = probability of success on one trial) such that the probability of observing floor(k) or fewer successes in floor(n) trials is p		
Domain <i>n</i> :	1 to $1e+17$		
Domain k:	0 to $n-1$		
Domain <i>p</i> :	0 to 1 (exclusive)		
Range:	0 to 1		

invbinomialtail(n, k, p)Description:the inverse of the right cumulative binomial; that is,  $\theta$  ( $\theta$  = probability of success on<br/>one trial) such that the probability of observing floor(k) or more successes in<br/>floor(n) trials is pDomain n:1 to 1e+17Domain k:1 to nDomain p:0 to 1 (exclusive)Range:0 to 1

### **Cauchy distribution**

Cauchy distri	button
cauchyden(a,	
Description:	the probability density of the Cauchy distribution with location parameter $a$ and scale parameter $b$
Domain a:	-1e+300 to $1e+300$
Domain <i>b</i> :	1e-100 to 1e+300
Domain x:	-8e+307 to $8e+307$
Range:	0 to 8e+307
<pre>cauchy(a,b,a)</pre>	.)
Description:	the cumulative Cauchy distribution with location parameter $a$ and scale parameter $b$
Domain a:	-1e+300 to $1e+300$
Domain <i>b</i> :	1e-100 to 1e+300
Domain <i>x</i> :	-8e+307 to $8e+307$
Range:	0 to 1
cauchytail(d	
Description:	the reverse cumulative (upper tail or survivor) Cauchy distribution with location
	parameter a and scale parameter b
Domain <i>a</i> :	cauchytail(a,b,x) = 1 - cauchy(a,b,x) $-1e+300  to  1e+300$
Domain $a$ : Domain $b$ :	1e-100 to $1e+300$
Domain $v$ :	-8e+307 to $8e+307$
Range:	0 to 1
Runge.	
invcauchy(a,	-
Description:	the inverse of cauchy(): if cauchy( $a, b, x$ ) = $p$ , then
Domain <i>a</i> :	invcauchy(a,b,p) = x -1e+300 to $1e+300$
Domain $a$ : Domain $b$ :	-1e+300 to $1e+3001e-100$ to $1e+300$
Domain $p$ :	0  to  1  (exclusive)
Range:	-8e+307 to $8e+307$
itunge.	

<pre>invcauchytail(a,b,p)</pre>		
Description:	the inverse of cauchytail(): if cauchytail( $a, b, x$ ) = $p$ , then	
- ·	invcauchytail(a,b,p) = x	
Domain <i>a</i> :	-1e+300 to $1e+300$	
Domain <i>b</i> :	1e-100 to 1e+300	
Domain <i>p</i> :	0 to 1 (exclusive)	
Range:	-8e+307 to 8e+307	
lncauchyden $(a, b, x)$ Description: the natural logarithm of the density of the Cauchy distribution with location parameter		
Domain <i>a</i> :	a and scale parameter $b-1e+300 to 1e+300$	
Domain <i>b</i> :	1e-100 to 1e+300	
Domain <i>x</i> :	-8e+307 to $8e+307$	
Range:	-1650 to 230	

Augustin-Louis Cauchy (1789–1857) was born in Paris, France. He obtained a degree in engineering with honors from École Polytechnique, where he would later teach mathematics. While working as a military engineer, he published two papers on polyhedra, one of which was a solution to a problem presented to him by Joseph-Louis Lagrange. In 1816, he won the Grand Prix for his work on wave propagation.

Cauchy's contributions were numerous and far reaching, as evident by the many concepts and theorems named after him. Some examples include the Cauchy criterion for convergence, Cauchy's theorem for finite groups, the Cauchy distribution, and the Cauchy stress tensor. His contributions were so vast that once all of his work was collected, it comprised 27 volumes. His name is engraved on the Eiffel Tower, along with 71 other scientists and mathematicians.

### $\chi^2$ and noncentral $\chi^2$ distributions

·)
the probability density of the $\chi^2$ distribution with $df$ degrees of freedom; 0 if $x < 0$
chi2den(df, x) = gammaden(df/2, 2, 0, x)
2e-10 to 2e+17 (may be nonintegral)
-8e+307 to $8e+307$
0 to 8e+307
the cumulative $\chi^2$ distribution with $df$ degrees of freedom; 0 if $x < 0$
chi2(df, x) = gammap(df/2, x/2)
2e-10 to 2e+17 (may be nonintegral)
$-8e+307$ to $8e+307$ ; interesting domain is $x \ge 0$
0 to 1

chi2tail(df, Description: Domain df: Domain x: Range:	(x) the reverse cumulative (upper tail or survivor) $\chi^2$ distribution with $df$ degrees of freedom; 1 if $x < 0$ chi2tail( $df, x$ ) = 1 - chi2( $df, x$ ) 2e-10 to 2e+17 (may be nonintegral) -8e+307 to 8e+307; interesting domain is $x \ge 0$ 0 to 1
invchi2(df, p Description: Domain df: Domain p: Range:	(p) the inverse of chi2(): if chi2(df,x) = p, then invchi2(df,p) = x 2e-10 to 2e+17 (may be nonintegral) 0 to 1 0 to 8e+307
invchi2tail( Description: Domain df: Domain p: Range:	<pre>(df,p) the inverse of chi2tail(): if chi2tail(df,x) = p, then invchi2tail(df,p) = x 2e-10 to 2e+17 (may be nonintegral) 0 to 1 0 to 8e+307</pre>
nchi2den( $df$ , Description: Domain $df$ : Domain $np$ : Domain $x$ : Range:	( <i>np</i> , <i>x</i> ) the probability density of the noncentral $\chi^2$ distribution; 0 if $x < 0$ df denotes the degrees of freedom, <i>np</i> is the noncentrality parameter, and <i>x</i> is the value of $\chi^2$ . nchi2den( $df$ , 0, <i>x</i> ) = chi2den( $df$ , <i>x</i> ), but chi2den() is the preferred function to use for the central $\chi^2$ distribution. 2e-10 to 1e+6 (may be nonintegral) 0 to 10,000 -8e+307 to 8e+307 0 to 8e+307

nchi2(df, np, x) Description: the cumulative noncentral  $\chi^2$  distribution; 0 if x < 0

The cumulative noncentral  $\chi^2$  distribution is defined as

$$\int_0^x \frac{e^{-t/2} e^{-np/2}}{2^{df/2}} \sum_{j=0}^\infty \frac{t^{df/2+j-1} np^j}{\Gamma(df/2+j) 2^{2j} j!} dt$$

 $\begin{array}{ll} \mbox{where } df \mbox{ denotes the degrees of freedom, } np \mbox{ is the noncentrality parameter, and } x \mbox{ is the value of } \chi^2. \\ \mbox{ nchi2}(df,0,x) = \mbox{chi2}(df,x), \mbox{ but chi2}() \mbox{ is the preferred function to use for the central } \chi^2 \mbox{ distribution.} \\ \mbox{ Domain } df: & 2e-10 \mbox{ to } 1e+6 \mbox{ (may be nonintegral)} \\ \mbox{ Domain } np: & 0 \mbox{ to } 10,000 \\ \mbox{ Domain } x: & -8e+307 \mbox{ to } 8e+307; \mbox{ interesting domain is } x \geq 0 \\ \mbox{ Range: } & 0 \mbox{ to } 1 \\ \end{array}$ 

nchi2tail(df, np, x)

Description:	the reverse cumulative (upper tail or survivor) noncentral $\chi^2$ distribution; 1 if $x < 0$
	df denotes the degrees of freedom, $np$ is the noncentrality parameter, and $x$ is the
	value of $\chi^2$ .
Domain <i>df</i> :	2e-10 to 1e+6 (may be nonintegral)
Domain np:	0 to 10,000
Domain $x$ :	-8e+307 to $8e+307$
Range:	0 to 1

<pre>invnchi2(df,np,p)</pre>		
Description:	the inverse cumulative noncentral $\chi^2$ distribution: if	
	nchi2(df, np, x) = p, then $invnchi2(df, np, p) = x$	
Domain <i>df</i> :	2e–10 to 1e+6 (may be nonintegral)	
Domain <i>np</i> :	0 to 10,000	
Domain <i>p</i> :	0 to 1	
Range:	0 to 8e+307	

#### invnchi2tail(df,np,p)

Description:	the inverse reverse cumulative (upper tail or survivor) noncentral $\chi^2$ distribution: if
	nchi2tail(df, np, x) = p, then invnchi2tail(df, np, p) = x
Domain <i>df</i> :	2e-10 to 1e+6 (may be nonintegral)
Domain np:	0 to 10,000
Domain <i>p</i> :	0 to 1
Range:	0 to 8e+307

npnchi2( $df$ , $x$	<i>,p</i> )
Description:	the noncentrality parameter, $np$ , for noncentral $\chi^2$ : if
	nchi2(df, np, x) = p, then $npnchi2(df, x, p) = np$
Domain <i>df</i> :	2e–10 to 1e+6 (may be nonintegral)
Domain x:	0 to 8e+307
Domain <i>p</i> :	0 to 1
Range:	0 to 10,000

#### Dunnett's multiple range distribution

dunnettprob( $k, df, x$ )Description:the cumulative multiple range distribution that is used in Dunnett's multiple-comparison method with $k$ ranges and $df$ degrees of freedom; 0 if $x < 0$		
Domain k: Domain df: Domain x: Range:	dunnettprob() is computed using an algorithm described in Miller (1981). 2 to 1e+6 2 to 1e+6 $-8e+307$ to 8e+307; interesting domain is $x \ge 0$ 0 to 1	
invdunnettprob $(k, df, p)$ Description: the inverse cumulative multiple range distribution that is used in Dunnett's multiple-comparison method with k ranges and df degrees of freedom If dunnettprob $(k, df, x) = p$ , then invdunnettprob $(k, df, p) = x$ .		
Domain k: Domain df: Domain p: Range:	<pre>invdunnettprob() is computed using an algorithm described in Miller (1981). 2 to 1e+6 2 to 1e+6 0 to 1 (right exclusive) 0 to 8e+307</pre>	

Charles William Dunnett (1921–2007) was a Canadian statistician best known for his work on multiple-comparison procedures. He was born in Windsor, Ontario, and graduated in mathematics and physics from McMaster University. After naval service in World War II, Dunnett's career included further graduate work, teaching, and research at Toronto, Columbia, the New York State Maritime College, the Department of National Health and Welfare in Ottawa, Cornell, Lederle Laboratories, and Aberdeen before he became Professor of Clinical Epidemiology and Biostatistics at McMaster University in 1974. He was President and Gold Medalist of the Statistical Society of Canada. Throughout his career, Dunnett took a keen interest in computing. According to Google Scholar, his 1955 paper on comparing treatments with a control has been cited over 4,000 times.

#### **Exponential distribution**

exponentialden(b, x)

Description: the probability density function of the exponential distribution with scale b

The probability density function of the exponential distribution is

$$\frac{1}{b}\exp(-x/b)$$

 $\begin{array}{ll} \mbox{where } b \mbox{ is the scale and } x \mbox{ is the value of an exponential variate.} \\ \mbox{Domain } b: & 1e-323 \mbox{ to } 8e+307 \\ \mbox{Domain } x: & -8e+307 \mbox{ to } 8e+307; \mbox{ interesting domain is } x \geq 0 \\ \mbox{Range:} & 1e-323 \mbox{ to } 8e+307 \\ \end{array}$ 

exponential(b,x)

Description: the cumulative exponential distribution with scale b

The cumulative distribution function of the exponential distribution is

 $1 - \exp(-x/b)$ 

	for $x \ge 0$ and 0 for $x < 0$ , where b is the scale and x is the value of an exponential
	variate.
	The mean of the exponential distribution is b and its variance is $b^2$ .
Domain b:	1e-323 to 8e+307
Domain x:	$-8e+307$ to $8e+307$ ; interesting domain is $x \ge 0$
Range:	0 to 1

exponentialtail(b, x)

Description: the reverse cumulative exponential distribution with scale b

The reverse cumulative distribution function of the exponential distribution is

 $\exp(-x/b)$ 

Domain <i>b</i> :	where <i>b</i> is the scale and <i>x</i> is the value of an exponential variate. 1e-323 to $8e+307$
Domain $0$ .	1e-323 to 8e+307
Domain $x$ :	$-8e+307$ to $8e+307$ ; interesting domain is $x \ge 0$
Range:	0 to 1

invexponential(b,p)		
Description:	the inverse cumulative exponential distribution with scale b: if	
	exponential(b, x) = p, then invexponential $(b, p) = x$	
Domain <i>b</i> :	1e-323 to 8e+307	
Domain <i>p</i> :	0 to 1	
Range:	1e-323 to 8e+307	
invexponentia	altail(b,p)	
Description:	the inverse reverse cumulative exponential distribution with scale <i>b</i> :	
	if exponential tail $(b, x) = p$ , then	
	invexponentialtail(b,p) = x	
Domain <i>b</i> :	1e-323 to 8e+307	
Domain <i>p</i> :	0 to 1	
Range:	1e-323 to 8e+307	

#### F and noncentral F distributions

Fden  $(df_1, df_2, f)$ Description: the probability density function of the *F* distribution with  $df_1$  numerator and  $df_2$ denominator degrees of freedom; 0 if f < 0

The probability density function of the F distribution with  $df_1$  numerator and  $df_2$  denominator degrees of freedom is defined as

$$\mathsf{Fden}(df_1, df_2, f) = \frac{\Gamma(\frac{df_1 + df_2}{2})}{\Gamma(\frac{df_1}{2})\Gamma(\frac{df_2}{2})} \left(\frac{df_1}{df_2}\right)^{\frac{df_1}{2}} \cdot f^{\frac{df_1}{2} - 1} \left(1 + \frac{df_1}{df_2}f\right)^{-\frac{1}{2}(df_1 + df_2)}$$

 $\begin{array}{ll} \mathsf{F}(df_1,df_2,f)\\ \text{Description:} & \text{the cumulative } F \, \text{distribution with } df_1 \, \text{numerator and } df_2 \, \text{denominator degrees of}\\ & \text{freedom: } \mathsf{F}(df_1,df_2,f) = \int_0^f \mathsf{Fden}(df_1,df_2,t) \, dt; \, 0 \, \text{if } f < 0\\ \text{Domain } df_1: & 2\mathrm{e}{-10} \text{ to } 2\mathrm{e}{+17} \, (\text{may be nonintegral})\\ \text{Domain } df_2: & 2\mathrm{e}{-10} \text{ to } 2\mathrm{e}{+17} \, (\text{may be nonintegral})\\ \text{Domain } f: & -8\mathrm{e}{+307} \, \text{to } 8\mathrm{e}{+307}; \, \text{interesting domain is } f \geq 0\\ \text{Range:} & 0 \, \text{to } 1 \end{array}$ 

Ftail( $df_1$ , $df$ ) Description:	$f_2, f$ ) the reverse cumulative (upper tail or survivor) $F$ distribution with $df_1$ numerator and $df_2$ denominator degrees of freedom; 1 if $f < 0$ Ftail( $df_1, df_2, f$ ) = 1 - F( $df_1, df_2, f$ ).
Domain $df_1$ : Domain $df_2$ : Domain $f$ : Range:	2e-10 to 2e+17 (may be nonintegral) 2e-10 to 2e+17 (may be nonintegral) -8e+307 to 8e+307; interesting domain is $f \ge 0$ 0 to 1
• 2	,p) the inverse cumulative F distribution: if $F(df_1, df_2, f) = p$ , then invF $(df_1, df_2, p) = f$ 2e-10 to 2e+17 (may be nonintegral) 2e-10 to 2e+17 (may be nonintegral) 0 to 1 0 to 8e+307
Domain $df_2$ :	$(df_2, p)$ the inverse reverse cumulative (upper tail or survivor) <i>F</i> distribution: if Ftail( $df_1, df_2, f$ ) = <i>p</i> , then invFtail( $df_1, df_2, p$ ) = <i>f</i> 2e-10 to 2e+17 (may be nonintegral) 2e-10 to 2e+17 (may be nonintegral) 0 to 1 0 to 8e+307

#### $nFden(df_1, df_2, np, f)$

Description: the probability density function of the noncentral F distribution with  $df_1$  numerator and  $df_2$  denominator degrees of freedom and noncentrality parameter np; 0 if f < 0nFden $(df_1, df_2, 0, f) = Fden(df_1, df_2, f)$ , but Fden() is the preferred function to use for the central F distribution.

Also, if F follows the noncentral F distribution with  $df_1$  and  $df_2$  degrees of freedom and noncentrality parameter np, then

$$\frac{df_1F}{df_2+df_1F}$$

follows a noncentral beta distribution with shape parameters  $a = df_1/2$ ,  $b = df_2/2$ , and noncentrality parameter np, as given in nbetaden(). nFden() is computed based on this relationship.

#### $nF(df_1, df_2, np, f)$ Description: the cumulative noncentral F distribution with $df_1$ numerator and $df_2$ denominator degrees of freedom and noncentrality parameter np; 0 if f < 0 $nF(df_1, df_2, 0, f) = F(df_1, df_2, f)$ nF() is computed using nibeta() based on the relationship between the noncentral beta and noncentral F distributions: $nF(df_1, df_2, np, f) =$ $\begin{array}{l} \texttt{nibeta}(df_{1}/2, df_{2}/2, np, df_{1} \times f/\{(df_{1} \times f) + df_{2}\}). \\ \texttt{2e-10 to 1e+8} \end{array}$ Domain $df_1$ : 2e-10 to 1e+8 Domain $df_2$ : Domain np: 0 to 10,000 Domain *f*: -8e+307 to 8e+307 Range: 0 to 1

#### $nFtail(df_1, df_2, np, f)$

Description:	the reverse cumulative (upper tail or survivor) noncentral $F$ distribution with $df_1$ numerator and $df_2$ denominator degrees of freedom and noncentrality parameter $np$ ; 1 if $f < 0$
	nFtail() is computed using nibeta() based on the relationship between the
	noncentral beta and F distributions. See Johnson, Kotz, and Balakrishnan (1995) for
Densin 16	more details.
Domain $df_1$ :	1e-323 to 8e+307 (may be nonintegral)
Domain $df_2$ :	1e-323 to 8e+307 (may be nonintegral)
Domain np:	0 to 1,000
Domain <i>f</i> :	$-8e+307$ to $8e+307$ ; interesting domain is $f \ge 0$
Range:	0 to 1

$invnF(df_1, df_2, np, p)$		
Description:	the inverse cumulative noncentral $F$ distribution: if	
	$nF(df_1, df_2, np, f) = p$ , then $invnF(df_1, df_2, np, p) = f$	
Domain $df_1$ :	1e–6 to 1e+6 (may be nonintegral)	
Domain $df_2$ :	1e–6 to 1e+6 (may be nonintegral)	
Domain np:	0 to 10,000	
Domain <i>p</i> :	0 to 1	
Range:	0 to 8e+307	

### $invnFtail(df_1, df_2, np, p)$

Description:	the inverse reverse cumulative (upper tail or survivor) noncentral F distribution: if
	$nFtail(df_1, df_2, np, f) = p$ , then invnFtail( $df_1, df_2, np, p$ ) = f
Domain $df_1$ :	1e-323 to 8e+307 (may be nonintegral)
Domain $df_2$ :	1e-323 to 8e+307 (may be nonintegral)
Domain np:	0 to 1,000
Domain <i>p</i> :	0 to 1
Range:	0 to 8e+307

 $\mathtt{npnF}(df_1, df_2, f, p)$ Description: the noncentrality parameter, np, for the noncentral F: if  $nF(df_1, df_2, np, f) = p$ , then  $npnF(df_1, df_2, f, p) = np$ 2e-10 to 1e+6 (may be nonintegral) Domain  $df_1$ : Domain  $df_2$ : 2e-10 to 1e+6 (may be nonintegral) 0 to 8e+307Domain *f*: 0 to 1 Domain *p*: 0 to 1,000 Range:

#### Gamma distribution

gammaden(a, b, q, x)Description: the probability density function of the gamma distribution; 0 if x < q

The probability density function of the gamma distribution is defined by

$$\frac{1}{\Gamma(a)b^a}(x-g)^{a-1}e^{-(x-g)/b}$$

	where <i>a</i> is the shape parameter, <i>b</i> is the scale parameter, and <i>q</i> is the location parameter.
Domain <i>a</i> :	1e-323 to 8e+307
Domain <i>b</i> :	1e-323 to 8e+307
Domain g:	-8e+307 to $8e+307$
Domain $x$ :	$-8e+307$ to $8e+307$ ; interesting domain is $x \ge g$
Range:	0 to 8e+307

gammap(a, x)Description: the cumulative gamma distribution with shape parameter a; 0 if x < 0The cumulative gamma distribution with shape parameter a is defined by

$$\frac{1}{\Gamma(a)} \int_0^x e^{-t} t^{a-1} dt$$

The cumulative Poisson (the probability of observing k or fewer events if the expected is x) can be evaluated as 1-gammap(k+1,x). The reverse cumulative (the probability of observing k or more events) can be evaluated as gammap(k, x). See Press et al. (2007, 259–266) for a more complete description and for suggested uses for this function. gammap() is also known as the incomplete gamma function (ratio). Probabilities for the three-parameter gamma distribution (see gammaden()) can be calculated by shifting and scaling x; that is, gammap (a, (x-q)/b). Domain *a*: 1e-10 to 1e+17

Domain x: -8e+307 to 8e+307; interesting domain is  $x \ge 0$ 0 to 1

Range:

gammaptail(a, x)

Description: the reverse cumulative (upper tail or survivor) gamma distribution with shape parameter a; 1 if x < 0

The reverse cumulative (upper tail or survivor) gamma distribution with shape parameter a is defined by

$$ext{gammaptail}(a,x) = 1 - ext{gammap}(a,x) = \int_x^\infty ext{gammaden}(a,t) \, dt$$

invgammap(a,p)Description: the inverse cumulative gamma distribution: if gammap(a,x) = p, then invgammap(a,p) = xDomain a: 1e-10 to 1e+17 Domain p: 0 to 1 Range: 0 to 8e+307

invgammaptail(a,p)

Description:the inverse reverse cumulative (upper tail or survivor) gamma distribution: if<br/>gammaptail(a, x) = p, then invgammaptail(a, p) = xDomain a:1e-10 to 1e+17Domain p:0 to 1Range:0 to 8e+307

dgammapda(a, x)

Description:	$\frac{\partial P(a,x)}{\partial a}$ , where $P(a,x) = \text{gammap}(a,x)$ ; 0 if $x < 0$
Domain <i>a</i> :	1e-7 to $1e+17$
Domain x:	$-8e+307$ to $8e+307$ ; interesting domain is $x \ge 0$
Range:	-16 to 0

dgammapdada(a,x)		
Description:	$\frac{\partial^2 P(a,x)}{\partial a^2},$ where $P(a,x) = \texttt{gammap}(a,x);$ 0 if $x < 0$	
Domain a:	1e-7 to $1e+17$	
Domain $x$ :	$-8e+307$ to $8e+307$ ; interesting domain is $x \ge 0$	
Range:	-0.02 to 4.77e+5	

dgammapdadx(a	
Description:	$\frac{\partial^2 P(a,x)}{\partial a \partial x}$ , where $P(a,x) = \text{gammap}(a,x)$ ; 0 if $x < 0$
Domain a:	1e-7 to 1e+17
Domain x:	$-8e+307$ to $8e+307$ ; interesting domain is $x \ge 0$
Range:	-0.04 to $8e+307$

dgammapdx(a,	x)
Description:	$\frac{\partial P(a,x)}{\partial x}$ , where $P(a,x) = \text{gammap}(a,x)$ ; 0 if $x < 0$
Domain <i>a</i> :	1e-10 to $1e+17$
Domain $x$ :	$-8e+307$ to $8e+307$ ; interesting domain is $x \ge 0$
Range:	0 to 8e+307

dgammapdxdx(	
Description:	$\frac{\partial^2 P(a,x)}{\partial x^2}$ , where $P(a,x) = \text{gammap}(a,x)$ ; 0 if $x < 0$
Domain <i>a</i> :	1e-10 to $1e+17$
Domain x:	$-8e+307$ to $8e+307$ ; interesting domain is $x \ge 0$
Range:	0 to 1e+40

```
lnigammaden(a,b,x)
```

Description:the natural logarithm of the inverse gamma density, where a is the shape parameter<br/>and b is the scale parameterDomain a:1e-300 to 1e+300Domain b:1e-300 to 1e+300Domain x:1e-300 to 8e+307Range:-8e+307 to 8e+307

### Hypergeometric distribution

hypergeometricp(N, K, n, k)

Description:	the hypergeometric probability of $k$ successes out of a sample of size $n$ , from a population of size $N$ containing $K$ elements that have the attribute of interest
	population of size iv containing it clements that have the attribute of interest
	Success is obtaining an element with the attribute of interest.
Domain N:	2 to 1e+5
Domain K:	1 to $N-1$
Domain <i>n</i> :	1 to $N-1$

Domain k:	$\max(0, n -$	N + K)	to $\min(K, n)$

Range: 0 to 1 (right exclusive)

hypergeometric (N, K, n, k)Description: the cumulative probability of the hypergeometric distribution N is the population size, K is the number of elements in the population that have the attribute of interest, and n is the sample size. Returned is the probability of observing k or fewer elements from a sample of size n that have the attribute of interest. Domain N: 2 to 1e+5Domain *K*: 1 to N-1Domain *n*: 1 to N-1Domain k:  $\max(0, n - N + K)$  to  $\min(K, n)$ 0 to 1 Range:

### **Inverse Gaussian distribution**

igaussianden(m,a,x)

Description: the probability density of the inverse Gaussian distribution with mean m and shape parameter a; 0 if  $x \le 0$ Domain m: 1e-323 to 8e+307

Domain a:	1e-323 to $8e+307$
Domain x:	-8e+307 to 8e+307
Range:	0 to 8e+307

igaussian(m,a,x)

Description:the cumulative inverse Gaussian distribution with mean m and shape parameter a; 0 if $x \leq 0$ 1e-323 to 8e+307Domain a:1e-323 to 8e+307Domain x:-8e+307 to 8e+307Range:0 to 1

igaussiantail(m,a,x)

Description:	the reverse cumulative (upper tail or survivor) inverse Gaussian distribution with
	mean $m$ and shape parameter $a$ ; 1 if $x \leq 0$
	igaussiantail(m,a,x) = 1 - igaussian(m,a,x)
Domain m:	1e-323 to 8e+307
Domain a:	1e-323 to 8e+307
Domain x:	-8e+307 to $8e+307$
Range:	0 to 1

invigaussian	( <i>m</i> , <i>a</i> , <i>p</i> )
Description:	the inverse of igaussian(): if
	igaussian(m,a,x) = p, then $invigaussian(m,a,p) = x$
Domain m:	1e-323 to 8e+307
Domain a:	1e-323 to 1e+8
Domain <i>p</i> :	0 to 1 (exclusive)
Range:	0 to 8e+307

```
invigaussiantail(m, a, p)

Description: the inverse of igaussiantail(): if

igaussiantail(m, a, x) = p, then

invigaussiantail(m, a, p) = x

Domain m: 1e-323 to 8e+307

Domain a: 1e-323 to 1e+8

Domain p: 0 to 1 (exclusive)

Range: 0 to 8e+307
```

Inigaussianden (m, a, x)Description:the natural logarithm of the inverse Gaussian density with mean m and shape<br/>parameter aDomain m:1e-323 to 8e+307Domain a:1e-323 to 8e+307Domain x:1e-323 to 8e+307Range:-8e+307 to 8e+307

#### Laplace distribution

laplaceden (m, b, x)Description:the probability density of the Laplace distribution with mean m and scale parameter bDomain m:-8e+307 to 8e+307Domain b:1e-307 to 8e+307Domain x:-8e+307 to 8e+307Range:0 to 8e+307

laplace (m, b, x)Description:the cumulative Laplace distribution with mean m and scale parameter bDomain m:-8e+307 to 8e+307Domain b:1e-307 to 8e+307Domain x:-8e+307 to 8e+307Range:0 to 1

laplacetail(m,b,x)

Description:the reverse cumulative (upper tail or survivor) Laplace distribution with mean m and<br/>scale parameter b<br/>laplacetail(m, b, x) = 1 - laplace(m, b, x)Domain m:-8e+307 to 8e+307Domain b:1e-307 to 8e+307Domain x:-8e+307 to 8e+307Domain x:-8e+307 to 8e+307Range:0 to 1

```
invlaplace(m,b,p)
Description:
               the inverse of laplace(): if laplace(m, b, x) = p, then
               invlaplace(m, b, p) = x
               -8e+307 to 8e+307
Domain m:
Domain b:
               1e-307 to 8e+307
Domain p:
               0 to 1 (exclusive)
Range:
               -8e+307 to 8e+307
invlaplacetail(m,b,p)
Description:
               the inverse of laplacetail(): if laplacetail(m, b, x) = p,
               then invlaplacetail(m, b, p) = x
Domain m:
               -8e+307 to 8e+307
Domain b:
               1e-307 to 8e+307
Domain p:
               0 to 1 (exclusive)
               -8e+307 to 8e+307
Range:
```

lnlaplaceden(m,b,x)

Description:the natural logarithm of the density of the Laplace distribution with mean m and scale<br/>parameter bDomain m:-8e+307 to 8e+307Domain b:1e-307 to 8e+307Domain x:-8e+307 to 8e+307Domain x:-8e+307 to 8e+307Range:-8e+307 to 707

### Logistic distribution

logisticden(	<i>x</i> )
Description:	the density of the logistic distribution with mean 0 and standard deviation $\pi/\sqrt{3}$
	logisticden(x) = logisticden(1, x) = logisticden(0, 1, x), where x is the value of a logistic random variable.
Domain x:	-8e+307 to $8e+307$
Range:	0 to 0.25
logisticden( Description:	the density of the logistic distribution with mean 0, scale s, and standard deviation $s\pi/\sqrt{3}$
	logisticden $(s, x)$ = logisticden $(0, s, x)$ , where s is the scale and x is the value of a logistic random variable.
Domain <i>s</i> : Domain <i>x</i> : Range:	1e-323 to 8e+307 -8e+307 to 8e+307 0 to 8e+307

logisticden(m,s,x)

Description: the density of the logistic distribution with mean m, scale s, and standard deviation  $s\pi/\sqrt{3}$ 

The density of the logistic distribution is defined as

$$\frac{\exp\{-(x-m)/s\}}{s[1+\exp\{-(x-m)/s\}]^2}$$

where m is the mean, s is the scale, and x is the value of a logistic random variable.

Domain <i>m</i> :	-8e+307 to 8e+307
Domain s:	1e-323 to 8e+307
Domain $x$ :	-8e+307 to 8e+307
Range:	0 to 8e+307

#### logistic(x)

Description: the cumulative logistic distribution with mean 0 and standard deviation  $\pi/\sqrt{3}$ logistic(x) = logistic(1,x) = logistic(0,1,x), where x is the value of a logistic random variable. Domain x: -8e+307 to 8e+307Range: 0 to 1

#### logistic(s, x)

Description: the cumulative logistic distribution with mean 0, scale s, and standard deviation  $s\pi/\sqrt{3}$ logistic(s, x) = logistic(0, s, x), where s is the scale and x is the value of a logistic random variable. Domain s: 1e-323 to 8e+307 Domain x: -8e+307 to 8e+307 Range: 0 to 1

logistic(m,s,x)

Description: the cumulative logistic distribution with mean m, scale s, and standard deviation  $s\pi/\sqrt{3}$ 

The cumulative logistic distribution is defined as

 $[1 + \exp\{-(x - m)/s\}]^{-1}$ 

where m is the mean, s is the scale, and x is the value of a logistic random variable.

Domain m:	-8e+307 to 8e+307
Domain s:	1e-323 to 8e+307
Domain x:	-8e+307 to 8e+307
Range:	0 to 1

logistictail	
Description:	the reverse cumulative logistic distribution with mean 0 and standard deviation $\pi/\sqrt{3}$
	logistictail( $x$ ) = logistictail(1, $x$ ) = logistictail(0,1, $x$ ), where $x$ is the value of a logistic random variable.
Domain x:	-8e+307 to 8e+307
Range:	0 to 1
logistictail	(s, x)
Description:	the reverse cumulative logistic distribution with mean 0, scale s, and standard deviation $s\pi/\sqrt{3}$
	logistictail(s, x) = logistictail(0, s, x), where s is the scale and x is the value of a logistic random variable.
Domain <i>s</i> :	1e-323 to 8e+307
Domain <i>x</i> : Range:	-8e+307 to 8e+307 0 to 1
-	
logistictail	
Description:	the reverse cumulative logistic distribution with mean m, scale s, and standard deviation $s\pi/\sqrt{3}$
	The reverse cumulative logistic distribution is defined as
	$[1+\exp\{(x-m)/s\}]^{-1}$
	$[1+\exp\{(x-m)/s\}]^{-1}$ where $m$ is the mean, $s$ is the scale, and $x$ is the value of a logistic random variable.
Domain <i>m</i> :	where $m$ is the mean, $s$ is the scale, and $x$ is the value of a logistic random variable. -8e+307 to 8e+307
Domain <i>m</i> : Domain <i>s</i> : Domain <i>x</i> :	where $m$ is the mean, $s$ is the scale, and $x$ is the value of a logistic random variable.
Domain s:	where $m$ is the mean, $s$ is the scale, and $x$ is the value of a logistic random variable. -8e+307 to 8e+307 1e-323 to 8e+307
Domain <i>s</i> : Domain <i>x</i> : Range:	where m is the mean, s is the scale, and x is the value of a logistic random variable. -8e+307 to $8e+3071e-323$ to $8e+307-8e+307$ to $8e+307-8e+307$ to $8e+3070$ to $1$
Domain <i>s</i> : Domain <i>x</i> :	where m is the mean, s is the scale, and x is the value of a logistic random variable. -8e+307 to $8e+3071e-323$ to $8e+307-8e+307$ to $8e+307-8e+307$ to $8e+3070$ to $1$
Domain s: Domain x: Range: invlogistic( Description:	where <i>m</i> is the mean, <i>s</i> is the scale, and <i>x</i> is the value of a logistic random variable. -8e+307 to $8e+3071e-323$ to $8e+307-8e+307$ to $8e+3070$ to 1 ( <i>p</i> ) the inverse cumulative logistic distribution: if logistic( <i>x</i> ) = <i>p</i> , then invlogistic( <i>p</i> ) = <i>x</i>
Domain s: Domain x: Range: invlogistic( Description: Domain p:	where <i>m</i> is the mean, <i>s</i> is the scale, and <i>x</i> is the value of a logistic random variable. -8e+307 to $8e+3071e-323$ to $8e+307-8e+307$ to $8e+3070$ to 1 ( <i>p</i> ) the inverse cumulative logistic distribution: if logistic( <i>x</i> ) = <i>p</i> ,
Domain s: Domain x: Range: invlogistic( Description:	where <i>m</i> is the mean, <i>s</i> is the scale, and <i>x</i> is the value of a logistic random variable. -8e+307 to $8e+3071e-323$ to $8e+307-8e+307$ to $8e+3070$ to 1 ( <i>p</i> ) the inverse cumulative logistic distribution: if logistic( <i>x</i> ) = <i>p</i> , then invlogistic( <i>p</i> ) = <i>x</i> 0 to 1
Domain s: Domain x: Range: invlogistic( Description: Domain p: Range: invlogistic(	where <i>m</i> is the mean, <i>s</i> is the scale, and <i>x</i> is the value of a logistic random variable. -8e+307 to $8e+3071e-323$ to $8e+307-8e+307$ to $8e+3070$ to 1 <i>p</i> ) the inverse cumulative logistic distribution: if $logistic(x) = p$ , then $invlogistic(p) = x$ 0 to $1-8e+307$ to $8e+307s,p)$
Domain s: Domain x: Range: invlogistic( Description: Domain p: Range:	where <i>m</i> is the mean, <i>s</i> is the scale, and <i>x</i> is the value of a logistic random variable. -8e+307 to $8e+3071e-323$ to $8e+307-8e+307$ to $8e+3070$ to 1 <i>p</i> ) the inverse cumulative logistic distribution: if $logistic(x) = p$ , then $invlogistic(p) = x$ 0 to $1-8e+307$ to $8e+307is,p)the inverse cumulative logistic distribution: if logistic(s,x) = p, then$
Domain s: Domain x: Range: invlogistic( Description: Domain p: Range: invlogistic(	where <i>m</i> is the mean, <i>s</i> is the scale, and <i>x</i> is the value of a logistic random variable. -8e+307 to $8e+3071e-323$ to $8e+307-8e+307$ to $8e+3070$ to 1 <i>p</i> ) the inverse cumulative logistic distribution: if $logistic(x) = p$ , then $invlogistic(p) = x$ 0 to $1-8e+307$ to $8e+307s,p)$
Domain s: Domain x: Range: invlogistic( Description: Domain p: Range: invlogistic( Description:	where <i>m</i> is the mean, <i>s</i> is the scale, and <i>x</i> is the value of a logistic random variable. -8e+307 to $8e+3071e-323$ to $8e+307-8e+307$ to $8e+3070$ to 1 ( <i>p</i> ) the inverse cumulative logistic distribution: if logistic( <i>x</i> ) = <i>p</i> , then invlogistic( <i>p</i> ) = <i>x</i> 0 to 1 -8e+307 to $8e+307(s,p)the inverse cumulative logistic distribution: if logistic(s,x) = p, then invlogistic(s,p) = x$

<pre>invlogistic(m,s,p)</pre>				
Description:	the inverse cumulative logistic distribution: if $logistic(m,s,x) = p$ , then $invlogistic(m,s,p) = x$			
Domain <i>m</i> :	-8e+307 to 8e+307			
Domain s:	1e-323 to 8e+307			
Domain <i>p</i> : Range:	0 to 1 -8e+307 to 8e+307			
Tunger				
invlogistictail(p)				
Description:	the inverse reverse cumulative logistic distribution: if			
- ·	logistictail(x) = p, then invlogistictail( $p$ ) = $x$			
Domain <i>p</i> : Range:	0 to 1 -8e+307 to 8e+307			
Kange.				
invlogistictail(s,p)				
Description:	the inverse reverse cumulative logistic distribution: if			
	logistictail(s,x) = p, then invlogistictail(s,p) = x			
Domain <i>s</i> :	1e-323 to 8e+307			
Domain <i>p</i> : Range:	0 to 1 -8e+307 to 8e+307			
Range.				
invlogistict	ail(m,s,p)			
Description:	the inverse reverse cumulative logistic distribution: if			
	logistictail(m,s,x) = p, then invlogistictail(m,s,p) = x			
Domain m:	-8e+307 to $8e+307$			
Domain $m$ : Domain $s$ :	-8e+307 to $8e+3071e-323 to 8e+307$			
Domain $p$ :	0 to 1			
Range:	-8e+307 to $8e+307$			

# Negative binomial distribution

nbinomialp( <i>n</i>	n,k,p)	
Description:	the negative binomial probability	
Domain <i>n</i> :	When n is an integer, nbinomialp() returns the probability of observing exactly $floor(k)$ failures before the nth success when the probability of a success on one trial is p. 1e-10 to 1e+6 (can be nonintegral)	
Domain k:	0 to 1e+10	
Domain <i>p</i> :	0 to 1 (left exclusive)	
Range:	0 to 1	

(k,p)		
the cumulative probability of the negative binomial distribution		
n can be nonintegral. When $n$ is an integer, nbinomial() returns the probability of observing $k$ or fewer failures before the $n$ th success, when the probability of a success on one trial is $p$ .		
The negative binomial distribution function is evaluated using ibeta(). 1e-10 to $1e+17$ (can be nonintegral) 0 to $2^{53} - 1$ 0 to 1 (left exclusive) 0 to 1		
nbinomialtail $(n, k, p)$ Description: the reverse cumulative probability of the negative binomial distribution		
When $n$ is an integer, nbinomialtail() returns the probability of observing $k$ or more failures before the $n$ th success, when the probability of a success on one trial is $p$ .		
The reverse negative binomial distribution function is evaluated using ibetatail(). 1e-10 to $1e+17$ (can be nonintegral) 0 to $2^{53} - 1$ 0 to 1 (left exclusive) 0 to 1		
invnbinomial $(n, k, q)$ Description: the value of the negative binomial parameter, p, such that $q = nbinomial(n, k, p)$		
the value of the negative binomial parameter, $p$ , such that $q = nbinomial(n, k, p)$		
<pre>invnbinomial() is evaluated using invibeta(). le-10 to le+17 (can be nonintegral) 0 to 2<sup>53</sup> - 1 0 to 1 (exclusive) 0 to 1</pre>		
tail(n,k,q)		
the value of the negative binomial parameter, $p$ , such that $q = nbinomialtail(n, k, p)$		
<pre>invnbinomialtail() is evaluated using invibetatail(). le-10 to le+17 (can be nonintegral) 1 to 2<sup>53</sup> - 1 0 to 1 (exclusive) 0 to 1 (exclusive)</pre>		

## Normal (Gaussian), binormal, and multivariate normal distributions

normalden(z)	
Description:	the standard normal density, $N(0, 1)$
Domain:	-8e+307 to 8e+307
Range:	0 to 0.39894

normalden( $x, \sigma$ ) Description: the normal density with mean 0 and standard deviation  $\sigma$ normalden(x, 1) = normalden(x) and normalden( $x, \sigma$ ) = normalden( $x/\sigma$ )/ $\sigma$ . Domain x: -8e+307 to 8e+307Domain  $\sigma$ : 1e-308 to 8e+307 0 to 8e+307 Range: normalden( $x, \mu, \sigma$ ) Description: the normal density with mean  $\mu$  and standard deviation  $\sigma$ ,  $N(\mu, \sigma^2)$ normalden(x,0,s) = normalden(x,s) and normalden $(x, \mu, \sigma)$  = normalden $((x - \mu)/\sigma)/\sigma$ . In general, normalden(z, $\mu$ , $\sigma$ ) =  $\frac{1}{\sigma\sqrt{2\pi}}e^{-\frac{1}{2}\left\{\frac{(z-\mu)}{\sigma}\right\}^2}$ Domain x: -8e+307 to 8e+307Domain  $\mu$ : -8e+307 to 8e+307 1e-308 to 8e+307 Domain  $\sigma$ : 0 to 8e+307 Range: normal(z)Description: the cumulative standard normal distribution normal(z) =  $\int_{-\infty}^{z} \frac{1}{\sqrt{2\pi}} e^{-x^2/2} dx$ -8e+307 to 8e+307 Domain: Range: 0 to 1 invnormal(p) Description: the inverse cumulative standard normal distribution: if normal(z) = p, then invnormal(p) = z1e-323 to  $1-2^{-53}$ Domain: Range: -38.449394 to 8.2095362 lnnormalden(z)Description: the natural logarithm of the standard normal density, N(0, 1)Domain: -1e+154 to 1e+154-5e+307 to -0.91893853 =lnnormalden(0) Range:

lnnormalden $(x, \sigma)$ Description: the natural logarithm of the normal density with mean 0 and standard deviation  $\sigma$ 

	lnnormalden(x, 1) = lnnormalden(x) and
	$lnnormalden(x,\sigma) = lnnormalden(x/\sigma) - ln(\sigma).$
Domain <i>x</i> :	-8e+307 to 8e+307
Domain $\sigma$ :	1e-323 to 8e+307
Range:	-5e+307 to 742.82799

lnnormalden( $x, \mu, \sigma$ )

Description:

the natural logarithm of the normal density with mean  $\mu$  and standard deviation  $\sigma,$   $N(\mu,\sigma^2)$ 

lnnormalden(x,0,s) = lnnormalden(x,s) and lnnormalden $(x,\mu,\sigma)$  = lnnormalden $((x-\mu)/\sigma) - \ln(\sigma)$ . In general,

$$\texttt{lnnormalden}(z,\mu,\sigma) = \ln\left[\frac{1}{\sigma\sqrt{2\pi}}e^{-\frac{1}{2}\left\{\frac{(z-\mu)}{\sigma}\right\}^2}\right]$$

Domain x:	-8e+307 to 8e+307
Domain $\mu$ :	-8e+307 to 8e+307
Domain $\sigma$ :	1e-323 to 8e+307
Range:	1e-323 to 8e+307

lnnormal(z)

Description: the natural logarithm of the cumulative standard normal distribution

$$\texttt{lnnormal}(z) = \ln\left(\int_{-\infty}^{z} \frac{1}{\sqrt{2\pi}} e^{-x^2/2} dx\right)$$

Domain: -1e+99 to 8e+307 Range: -5e+197 to 0

 $binormal(h, k, \rho)$ 

Description: the joint cumulative distribution  $\Phi(h, k, \rho)$  of bivariate normal with correlation  $\rho$ Cumulative over  $(-\infty, h] \times (-\infty, k]$ :

$$\Phi(h,k,\rho) = \frac{1}{2\pi\sqrt{1-\rho^2}} \int_{-\infty}^{h} \int_{-\infty}^{k} \exp\biggl\{-\frac{1}{2(1-\rho^2)} (x_1^2 - 2\rho x_1 x_2 + x_2^2) \biggr\} dx_1 \, dx_2 + \frac{1}{2\rho^2} dx_2 \, dx_2 + \frac{1}{2\rho^2} dx_1 \, dx_2 + \frac{1}{2\rho^2} dx_2 \, dx_2 + \frac{1}{2\rho^2} dx_1 \, dx_2 + \frac{1}{2\rho^2} dx_2 \, dx_2 \,$$

 Domain h:
 -8e+307 to 8e+307 

 Domain k:
 -8e+307 to 8e+307 

 Domain  $\rho$ :
 -1 to 1

 Range:
 0 to 1

lnmvnormalden(M,V,X)			
Description:	the natural logarithm of the multivariate normal density		
Domain <i>M</i> : Domain <i>V</i> : Domain <i>X</i> :	M is the mean vector, $V$ is the covariance matrix, and $X$ is the random vector. $1 \times n$ and $n \times 1$ vectors $n \times n$ , positive-definite, symmetric matrices $1 \times n$ and $n \times 1$ vectors -8e+307 to $8e+307$		

## **Poisson distribution**

poissonp( <i>m</i> , Description:	the probability of observing $floor(k)$ outcomes that are distributed as Poisson with mean $m$			
Domain <i>m</i> : Domain <i>k</i> : Range:	The Poisson probability function is evaluated using gammaden(). 1e-10 to 1e+8 0 to 1e+9 0 to 1			
poisson( $m$ , $k$	)			
Description:	the probability of observing $floor(k)$ or fewer outcomes that are distributed as Poisson with mean $m$			
Domain <i>m</i> : Domain <i>k</i> : Range:	The Poisson distribution function is evaluated using gammaptail(). $1e-10 \text{ to } 2^{53} - 1$ $0 \text{ to } 2^{53} - 1$ 0  to  1			
poissontail( Description:	the probability of observing $floor(k)$ or more outcomes that are distributed as			
	Poisson with mean $m$ The reverse cumulative Poisson distribution function is evaluated using gammap().			
Domain <i>m</i> :	$1e-10 \text{ to } 2^{53} - 1$			
Domain <i>k</i> : Range:	0 to $2^{53} - 1$ 0 to 1			
invpoisson(k,p)				
Description:	the Poisson mean such that the cumulative Poisson distribution evaluated at k is p: if $poisson(m,k) = p$ , then $invpoisson(k,p) = m$			
Domain h	The inverse Poisson distribution function is evaluated using invgammaptail(). 0 to $2^{53} - 1$			
Domain <i>k</i> : Domain <i>p</i> :	0 to 1 (exclusive)			
Range:	$1.110e-16 \text{ to } 2^{53}$			

invpoissonta	il(k,q)		
Description:	the Poisson mean such that the reverse cumulative Poisson distribution evaluated at $k$ is $q$ : if poissontail( $m, k$ ) = $q$ , then invpoissontail( $k, q$ ) = $m$		
	The inverse of the reverse cumulative Poisson distribution function is evaluated using invgammap().		
Domain k:	$0 \text{ to } 2^{53} - 1$		
Domain q:	0 to 1 (exclusive)		
Range:	0 to $2^{53}$ (left exclusive)		

### Student's t and noncentral Student's t distributions

tden(df,t)Description: the probability density function of Student's t distribution  $\mathsf{tden}(df,t) = \frac{\Gamma\{(df+1)/2\}}{\sqrt{\pi d f} \Gamma(df/2)} \cdot (1 + t^2/df)^{-(df+1)/2}$ Domain df: 1e-323 to 8e+307 (may be nonintegral) -8e+307 to 8e+307 Domain *t*: Range: 0 to 0.39894 ... t(df,t)Description: the cumulative Student's t distribution with df degrees of freedom Domain df: 2e-10 to 2e+17 (may be nonintegral) -8e+307 to 8e+307 Domain t; 0 to 1 Range: ttail(df,t)Description: the reverse cumulative (upper tail or survivor) Student's t distribution; the probability T > t $\texttt{ttail}(df,t) = \int_t^\infty \frac{\Gamma\{(df+1)/2\}}{\sqrt{\pi df} \Gamma(df/2)} \cdot (1+x^2/df)^{-(df+1)/2} \; dx$ Domain df: 2e-10 to 2e+17 (may be nonintegral) Domain *t*: -8e+307 to 8e+307 Range: 0 to 1 invt(df,p)Description: the inverse cumulative Student's t distribution: if t(df, t) = p, then invt(df, p) = tDomain df: 2e-10 to 2e+17 (may be nonintegral) Domain *p*: 0 to 1 Range: -8e+307 to 8e+307

invttail(df)	
Description:	the inverse reverse cumulative (upper tail or survivor) Student's $t$ distribution: if
	ttail(df,t) = p, then invttail( $df,p$ ) = t
Domain <i>df</i> :	2e-10 to 2e+17 (may be nonintegral)
Domain <i>p</i> :	0 to 1
Range:	-8e+307 to 8e+307
invnt(df, np	n)
Description:	the inverse cumulative noncentral Student's t distribution: if $nt(df, np, t) = p$ , then
Desemption	$\operatorname{invnt}(df, np, p) = t$
Domain <i>d f</i> :	1 to 1e+6 (may be nonintegral)
Domain $np$ :	-1,000 to 1,000
Domain <i>p</i> :	0 to 1
Range:	-8e+307 to 8e+307
invnttail(d	f,np,p)
Description:	the inverse reverse cumulative (upper tail or survivor) noncentral Student's
	t distribution: if $nttail(df, np, t) = p$ , then $invnttail(df, np, p) = t$
Domain <i>df</i> :	1 to 1e+6 (may be nonintegral)
Domain np:	-1,000 to 1,000
Domain <i>p</i> :	0 to 1
Range:	-8e+10 to $8e+10$
ntden(df, np	*)
Description:	the probability density function of the noncentral Student's
Description.	t distribution with $df$ degrees of freedom and noncentrality parameter $np$
Domain <i>d f</i> :	1e-100 to $1e+10$ (may be nonintegral)
Domain $np$ :	-1,000 to $1,000$
Domain $t$ :	-8e+307 to $8e+307$
Range:	0 to 0.39894
U	
nt(df, np, t)	
Description:	the cumulative noncentral Student's $t$ distribution with $df$ degrees of freedom and
- ····r	noncentrality parameter $np$
Domain df.	$\operatorname{nt}(df, 0, t) = \operatorname{t}(df, t).$
Domain <i>df</i> :	1e-100 to $1e+10$ (may be nonintegral)
Domain <i>np</i> : Domain <i>t</i> :	-1,000 to 1,000 -8e+307 to 8e+307
Domain t: Range:	-8e+307 to $8e+3070 to 1$
Kange.	

<pre>nttail(df, np Description: Domain df: Domain np: Domain t:</pre>	the reverse cumulative (upper tail or survivor) noncentral Student's t distribution with $df$ degrees of freedom and noncentrality parameter $np$ 1e-100 to 1e+10 (may be nonintegral) -1,000 to 1,000 -8e+307 to 8e+307
Range:	0 to 1
npnt (df,t,p) Description: Domain df: Domain t: Domain p: Range:	the noncentrality parameter, $np$ , for the noncentral Student's t distribution: if $nt(df, np, t) = p$ , then $npnt(df, t, p) = np1e-100$ to $1e+8$ (may be nonintegral) -8e+307 to $8e+3070$ to $1-1,000$ to $1,000$

# Tukey's Studentized range distribution

<pre>tukeyprob(k,</pre>	df, x)			
Description:	the cumulative Tukey's Studentized range distribution with k ranges and $df$ degree freedom; 0 if $x < 0$			
	If $df$ is a missing value, then the normal distribution is used instead of Student's $t$ .			
	tukeyprob() is computed using an algorithm described in Miller (1981).			
Domain k:	2 to 1e+6			
Domain <i>df</i> :	2 to 1e+6			
Domain x:	-8e+307 to 8e+307			
Range:	0 to 1			

invtukeyprob(k, df, p)

	be cumulative Tukey's Studentized range distribution with $k$ ranges and $df$ f freedom
	missing value, then the normal distribution is used instead of Student's t. If $bb(k, df, x) = p$ , then invtukeyprob $(k, df, p) = x$ .
invtukeDomain $k$ :2 to 1e+6Domain $df$ :2 to 1e+6Domain $p$ :0 to 1Range:0 to 8e+3	

#### Weibull distribution

weibullden(a, b, x)

Description: the probability density function of the Weibull distribution with shape a and scale b

weibullden(a, b, x) = weibullden(a, b, 0, x), where a is the shape, b is the scale, and x is the value of Weibull random variable.

Domain a:	1e-323 to 8e+307
Domain <i>b</i> :	1e-323 to 8e+307
Domain x:	1e-323 to 8e+307
Range:	0 to 8e+307

weibullden(a, b, g, x)

Description: the probability density function of the Weibull distribution with shape a, scale b, and location g

The probability density function of the generalized Weibull distribution is defined as

a	(x)	- :	$g \rangle^{a-1}$	exp {-	( 2	—	$g \gamma'$	<sup>2</sup>
$\overline{b}$	(-	b	-)	cxp∫_	( -	b	-)	ſ

for  $x \ge g$  and 0 for x < g, where a is the shape, b is the scale, g is the location parameter, and x is the value of a generalized Weibull random variable.

Domain a:	1e-323 to 8e+307
Domain <i>b</i> :	1e-323 to 8e+307
Domain g:	-8e+307 to $8e+307$
Domain $x$ :	$-8e+307$ to $8e+307$ ; interesting domain is $x \ge g$
Range:	0 to 8e+307

x)		
the cumulative Weibull distribution with shape $a$ and scale $b$		
weibull $(a, b, x) =$ weibull $(a, b, 0, x)$ , where a is the shape, b is the scale, and x is the value of Weibull random variable.		
1e-323 to 8e+307		
1e-323 to 8e+307		
1e-323 to 8e+307		
0 to 1		

weibull(a,b,g,x)

Description: the cumulative Weibull distribution with shape a, scale b, and location g

The cumulative Weibull distribution is defined as

$$1 - \exp\left[-\left(\frac{x-g}{b}\right)^a\right]$$

for  $x \ge g$  and 0 for x < g, where a is the shape, b is the scale, g is the location parameter, and x is the value of a Weibull random variable. The mean of the Weibull distribution is  $g + b\Gamma\{(a+1)/a\}\}$  and its variance is  $b^2 \left(\Gamma\{(a+2)/a\} - [\Gamma\{(a+1)/a\}]^2\right)$  where  $\Gamma()$  is the gamma function described in lngamma().

Domain <i>a</i> :	1e-323 to $8e+307$
Domain <i>b</i> :	1e-323 to 8e+307
Domain g:	-8e+307 to 8e+307
Domain x:	$-8e+307$ to $8e+307$ ; interesting domain is $x \ge g$
Range:	0 to 1

weibulltail(	a,b,x)		
Description:	the reverse cumulative Weibull distribution with shape $a$ and scale $b$		
	weibulltail( $a, b, x$ ) = weibulltail( $a, b, 0, x$ ), where $a$ is the shape, $b$ is the scale, and $x$ is the value of a Weibull random variable.		
Domain a:	1e-323 to 8e+307		
Domain <i>b</i> :	1e-323 to 8e+307		
Domain $x$ :	1e-323 to 8e+307		
Range:	0 to 1		

weibulltail(a, b, g, x)

Description: the reverse cumulative Weibull distribution with shape a, scale b, and location gThe reverse cumulative Weibull distribution is defined as

The reverse cumulative Weibull distribution is defined as

$$\exp\left\{-\left(\frac{x-g}{b}\right)^a\right\}$$

for  $x \ge g$  and 0 if x < g, where a is the shape, b is the scale, g is the location parameter, and x is the value of a generalized Weibull random variable.

1e-323 to 8e+307
1e-323 to 8e+307
-8e+307 to $8e+307$
$-8e+307$ to $8e+307$ ; interesting domain is $x \ge g$
0 to 1

invweibull( Description: Domain a: Domain b: Domain p: Range:	<pre>h,b,p) the inverse cumulative Weibull distribution with shape a and scale b: if weibull(a,b,x) = p, then invweibull(a,b,p) = x 1e-323 to 8e+307 1e-323 to 8e+307 0 to 1 1e-323 to 8e+307</pre>
invweibull(a	(a, b, q, p)
Description:	the inverse cumulative Weibull distribution with shape $a$ , scale $b$ , and location $g$ : if weibull $(a,b,g,x) = p$ , then invweibull $(a,b,g,p) = x$
Domain a:	1e-323 to 8e+307
Domain <i>b</i> :	1e-323 to 8e+307
Domain g:	-8e+307 to $8e+307$
Domain <i>p</i> :	0 to 1
Range:	g + c(epsdouble) to $8e+307$
invweibullta	-
Description:	the inverse reverse cumulative Weibull distribution with shape a and scale by if
1	the inverse reverse cumulative Weibull distribution with shape $a$ and scale $b$ : if weibulltail( $a, b, x$ ) = $p$ , then
-	weibulltail $(a,b,x) = p$ , then invweibulltail $(a,b,p) = x$
Domain <i>a</i> :	weibultail $(a, b, x) = p$ , then invweibultail $(a, b, p) = x$ 1e-323 to 8e+307
Domain <i>a</i> : Domain <i>b</i> :	weibulltail $(a, b, x) = p$ , then invweibulltail $(a, b, p) = x$ le-323 to 8e+307 le-323 to 8e+307
Domain <i>a</i> : Domain <i>b</i> : Domain <i>p</i> :	weibulltail( $a, b, x$ ) = $p$ , then invweibulltail( $a, b, p$ ) = $x$ le-323 to 8e+307 le-323 to 8e+307 0 to 1
Domain <i>a</i> : Domain <i>b</i> :	weibulltail $(a, b, x) = p$ , then invweibulltail $(a, b, p) = x$ le-323 to 8e+307 le-323 to 8e+307
Domain <i>a</i> : Domain <i>b</i> : Domain <i>p</i> : Range:	weibulltail( $a, b, x$ ) = $p$ , then invweibulltail( $a, b, p$ ) = $x$ le-323 to 8e+307 le-323 to 8e+307 0 to 1 le-323 to 8e+307
Domain a: Domain b: Domain p: Range: invweibullta	weibulltail $(a, b, x) = p$ , then invweibulltail $(a, b, p) = x$ le-323 to 8e+307 le-323 to 8e+307 0 to 1 le-323 to 8e+307 ail $(a, b, g, p)$
Domain <i>a</i> : Domain <i>b</i> : Domain <i>p</i> : Range:	weibulltail( $a, b, x$ ) = $p$ , then invweibulltail( $a, b, p$ ) = $x$ le-323 to 8e+307 le-323 to 8e+307 0 to 1 le-323 to 8e+307 ail( $a, b, g, p$ ) the inverse reverse cumulative Weibull distribution with shape $a$ , scale $b$ , and location g: if weibulltail( $a, b, g, x$ ) = $p$ , then
Domain a: Domain b: Domain p: Range: invweibullta Description:	weibulltail( $a, b, x$ ) = $p$ , then invweibulltail( $a, b, p$ ) = $x$ le-323 to 8e+307 le-323 to 8e+307 0 to 1 le-323 to 8e+307 ail( $a, b, g, p$ ) the inverse reverse cumulative Weibull distribution with shape $a$ , scale $b$ , and location g: if weibulltail( $a, b, g, x$ ) = $p$ , then invweibulltail( $a, b, g, p$ ) = $x$
Domain a: Domain b: Domain p: Range: invweibullta Description: Domain a:	weibulltail( $a, b, x$ ) = $p$ , then invweibulltail( $a, b, p$ ) = $x$ le-323 to 8e+307 le-323 to 8e+307 0 to 1 le-323 to 8e+307 ail( $a, b, g, p$ ) the inverse reverse cumulative Weibull distribution with shape $a$ , scale $b$ , and location g: if weibulltail( $a, b, g, x$ ) = $p$ , then invweibulltail( $a, b, g, p$ ) = $x$ le-323 to 8e+307
Domain a: Domain b: Domain p: Range: invweibullta Description: Domain a: Domain b:	weibulltail( $a, b, x$ ) = $p$ , then invweibulltail( $a, b, p$ ) = $x$ le-323 to 8e+307 le-323 to 8e+307 0 to 1 le-323 to 8e+307 ail( $a, b, g, p$ ) the inverse reverse cumulative Weibull distribution with shape $a$ , scale $b$ , and location g: if weibulltail( $a, b, g, x$ ) = $p$ , then invweibulltail( $a, b, g, p$ ) = $x$ le-323 to 8e+307 le-323 to 8e+307
Domain a: Domain b: Domain p: Range: invweibullta Description: Domain a: Domain b: Domain g:	weibulltail( $a, b, x$ ) = $p$ , then invweibulltail( $a, b, p$ ) = $x$ le-323 to 8e+307 le-323 to 8e+307 0 to 1 le-323 to 8e+307 ail( $a, b, g, p$ ) the inverse reverse cumulative Weibull distribution with shape $a$ , scale $b$ , and location g: if weibulltail( $a, b, g, x$ ) = $p$ , then invweibulltail( $a, b, g, p$ ) = $x$ le-323 to 8e+307
Domain a: Domain b: Domain p: Range: invweibullta Description: Domain a: Domain b:	weibulltail( $a, b, x$ ) = $p$ , then invweibulltail( $a, b, p$ ) = $x$ le-323 to 8e+307 le-323 to 8e+307 0 to 1 le-323 to 8e+307 ail( $a, b, g, p$ ) the inverse reverse cumulative Weibull distribution with shape $a$ , scale $b$ , and location g: if weibulltail( $a, b, g, x$ ) = $p$ , then invweibulltail( $a, b, g, p$ ) = $x$ le-323 to 8e+307 le-323 to 8e+307 -8e+307 to 8e+307

# Weibull (proportional hazards) distribution

$\label{eq:action} \begin{array}{llllllllllllllllllllllllllllllllllll$	weibullphden $(a, b, x)$ Description: the probability density function of the Weibull (proportional hazards) distribution with shape $a$ and scale $b$					
$\begin{array}{llllllllllllllllllllllllllllllllllll$						
Description:the probability density function of the Weibull (proportional hazards) distribution with shape $a$ , scale $b$ , and location $g$ The probability density function of the Weibull (proportional hazards) distribution is defined as $ba(x-g)^{a-1}\exp\{-b(x-g)^a\}$ for $x \ge g$ and 0 for $x < g$ , where $a$ is the shape, $b$ is the scale, $g$ is the location parameter, and $x$ is the value of a Weibull (proportional hazards) random variable.Domain $a$ : $1e-323$ to $8e+307$ Domain $g$ : $-8e+307$ to $8e+307$ Domain $x$ : $-8e+307$ to $8e+307$ Domain $x$ : $-8e+307$ to $8e+307$ Domain $x$ : $-8e+307$ to $8e+307$ Description:the cumulative Weibull (proportional hazards) distribution with shape $a$ and scale $b$ weibullph $(a, b, x)$ weibullph $(a, b, x) =$ weibullph $(a, b, 0, x)$ , where $a$ is the shape, $b$ is the scale, 	Domain <i>b</i> : Domain <i>x</i> :	1e-323 to 8e+307 1e-323 to 8e+307				
shape a, scale b, and location g The probability density function of the Weibull (proportional hazards) distribution is defined as $ba(x-g)^{a-1}\exp\{-b(x-g)^a\}$ for $x \ge g$ and 0 for $x < g$ , where a is the shape, b is the scale, g is the location parameter, and x is the value of a Weibull (proportional hazards) random variable. Domain a: 1e-323 to 8e+307 Domain b: 1e-323 to 8e+307 Domain g: -8e+307 to 8e+307 Domain x: -8e+307 to 8e+307; interesting domain is $x \ge g$ Range: 0 to 8e+307 weibullph(a,b,x) Description: the cumulative Weibull (proportional hazards) distribution with shape a and scale b weibullph(a,b,x) = weibullph(a, b, 0, x), where a is the shape, b is the scale, and x is the value of Weibull random variable. Domain a: 1e-323 to 8e+307	weibullphden	(a,b,g,x)				
defined as $ba(x-g)^{a-1}\exp\left\{-b(x-g)^a\right\}$ for $x \ge g$ and 0 for $x < g$ , where $a$ is the shape, $b$ is the scale, $g$ is the location parameter, and $x$ is the value of a Weibull (proportional hazards) random variable. Domain $a$ : 1e-323 to 8e+307 Domain $b$ : 1e-323 to 8e+307 Domain $g$ : -8e+307 to 8e+307 Domain $x$ : -8e+307 to 8e+307; interesting domain is $x \ge g$ Range: 0 to 8e+307 Weibullph $(a, b, x)$ Description: the cumulative Weibull (proportional hazards) distribution with shape $a$ and scale $b$ weibullph $(a, b, x) =$ weibullph $(a, b, 0, x)$ , where $a$ is the shape, $b$ is the scale, and $x$ is the value of Weibull random variable. Domain $a$ : 1e-323 to 8e+307	Description: the probability density function of the Weibull (proportional hazards) distribut					
$\begin{array}{llllllllllllllllllllllllllllllllllll$						
parameter, and x is the value of a Weibull (proportional hazards) random variable.Domain a: $1e-323$ to $8e+307$ Domain b: $1e-323$ to $8e+307$ Domain g: $-8e+307$ to $8e+307$ Domain x: $-8e+307$ to $8e+307$ ; interesting domain is $x \ge g$ Range:0 to $8e+307$ Weibullph( $a, b, x$ )Description:the cumulative Weibull (proportional hazards) distribution with shape a and scale bweibullph( $a, b, x$ ) = weibullph( $a, b, 0, x$ ), where a is the shape, b is the scale, and x is the value of Weibull random variable.Domain a: $1e-323$ to $8e+307$		$ba(x-g)^{a-1} {\rm exp}\left\{-b(x-g)^a\right\}$				
Domain $b$ : $1e-323$ to $8e+307$ Domain $g$ : $-8e+307$ to $8e+307$ Domain $x$ : $-8e+307$ to $8e+307$ ; interesting domain is $x \ge g$ Range: 0 to $8e+307$ weibullph $(a, b, x)$ Description: the cumulative Weibull (proportional hazards) distribution with shape $a$ and scale $b$ weibullph $(a, b, x) =$ weibullph $(a, b, 0, x)$ , where $a$ is the shape, $b$ is the scale, and $x$ is the value of Weibull random variable. Domain $a$ : $1e-323$ to $8e+307$						
Domain g: $-8e+307$ to $8e+307$ Domain x: $-8e+307$ to $8e+307$ ; interesting domain is $x \ge g$ Range:0 to $8e+307$ weibullph( $a, b, x$ )Description:the cumulative Weibull (proportional hazards) distribution with shape $a$ and scale $b$ weibullph( $a, b, x$ )weibullph( $a, b, x$ ) = weibullph( $a, b, 0, x$ ), where $a$ is the shape, $b$ is the scale, and $x$ is the value of Weibull random variable.Domain $a$ : $1e-323$ to $8e+307$						
Domain $x$ : $-8e+307$ to $8e+307$ ; interesting domain is $x \ge g$ Range:0 to $8e+307$ weibullph $(a, b, x)$ Description:the cumulative Weibull (proportional hazards) distribution with shape $a$ and scale $b$ weibullph $(a, b, x) =$ weibullph $(a, b, 0, x)$ , where $a$ is the shape, $b$ is the scale, and $x$ is the value of Weibull random variable.Domain $a$ :1e-323 to $8e+307$						
<pre>weibullph(a,b,x) Description: the cumulative Weibull (proportional hazards) distribution with shape a and scale b weibullph(a,b,x) = weibullph(a, b, 0, x), where a is the shape, b is the scale, and x is the value of Weibull random variable. Domain a: 1e-323 to 8e+307</pre>	Domain <i>x</i> :	$-8e+307$ to $8e+307$ ; interesting domain is $x \ge g$				
Description:the cumulative Weibull (proportional hazards) distribution with shape $a$ and scale $b$ weibullph $(a, b, x) =$ weibullph $(a, b, 0, x)$ , where $a$ is the shape, $b$ is the scale, and $x$ is the value of Weibull random variable.Domain $a$ :1e-323 to 8e+307	Range:	0 to 8e+307				
Description:the cumulative Weibull (proportional hazards) distribution with shape $a$ and scale $b$ weibullph $(a, b, x) =$ weibullph $(a, b, 0, x)$ , where $a$ is the shape, $b$ is the scale, and $x$ is the value of Weibull random variable.Domain $a$ :1e-323 to 8e+307	(a, b, a)					
and x is the value of Weibull random variable. Domain a: $1e-323$ to $8e+307$	-					
		• • •				
Domain b: $1e-323$ to $8e+30/$						
Domain x: 1e-323 to 8e+307						

Range: 0 to 1

weibullph(a, b, g, x)

Description: the cumulative Weibull (proportional hazards) distribution with shape a, scale b, and location g

The cumulative Weibull (proportional hazards) distribution is defined as

$$1 - \exp\left\{-b(x-g)^a\right\}$$

for  $x \ge g$  and 0 if x < g, where a is the shape, b is the scale, g is the location parameter, and x is the value of a Weibull (proportional hazards) random variable. The mean of the Weibull (proportional hazards) distribution is

$$g + b^{-\frac{1}{a}} \Gamma\{(a+1)/a)\}$$

and its variance is

$$b^{-\frac{2}{a}}\left(\Gamma\{(a+2)/a\}-[\Gamma\{(a+1)/a\}]^2\right)$$

where  $\Gamma()$  is the gamma function described in  $\ln \alpha(x)$ .

Domain <i>a</i> :	1e-323 to 8e+307
Domain b:	1e-323 to 8e+307
Domain g:	-8e+307 to 8e+307
Domain x:	$-8e+307$ to $8e+307$ ; interesting domain is $x \ge g$
Range:	0 to 1

weibullphtail(a, b, x)

Description: the reverse cumulative Weibull (proportional hazards) distribution with shape a and scale b

weibullphtail(a, b, x) = weibullphtail(a, b, 0, x), where a is the shape, b is the scale, and x is the value of a Weibull (proportional hazards) random variable.

Domain <i>a</i> :	1e-323 to 8e+307
Domain b:	1e-323 to 8e+307
Domain x:	1e-323 to 8e+307
Range:	0 to 1

weibullphtail(a, b, g, x)

Description: the reverse cumulative Weibull (proportional hazards) distribution with shape a, scale b, and location g

The reverse cumulative Weibull (proportional hazards) distribution is defined as

$$\exp\left\{-b(x-g)^a\right\}$$

for  $x \ge g$  and 0 of x < g, where a is the shape, b is the scale, g is the location parameter, and x is the value of a Weibull (proportional hazards) random variable.

Domain <i>a</i> :	1e-323 to 8e+307
Domain <i>b</i> :	1e-323 to 8e+307
Domain g:	-8e+307 to $8e+307$
Domain x:	$-8e+307$ to $8e+307$ ; interesting domain is $x \ge g$
Range:	0 to 1

invweibullph(a,b,p)

Description:the inverse cumulative Weibull (proportional hazards) distribution with shape a and<br/>scale b: if weibullph(a, b, x) = p, then invweibullph(a, b, p) = xDomain a:1e-323 to 8e+307Domain b:1e-323 to 8e+307Domain p:0 to 1Range:1e-323 to 8e+307

invweibullph(a, b, g, p)

Description:the inverse cumulative Weibull (proportional hazards) distribution with shape a, scale<br/>b, and location g: if weibullph(a, b, g, x) = p, then invweibullph(a, b, g, p) = xDomain a:1e-323 to 8e+307Domain b:1e-323 to 8e+307Domain g:-8e+307 to 8e+307Domain p:0 to 1Range:g + c (epsdouble) to 8e+307

invweibullphtail(a,b,p)

Description:	the inverse reverse cumulative Weibull (proportional hazards) distribution with shape				
	a and scale b: if weibullphtail( $a, b, x$ ) = p, then invweibullphtail( $a, b, p$ ) = x				
Domain <i>a</i> :	1e-323 to 8e+307				
Domain <i>b</i> :	1e-323 to 8e+307				
Domain <i>p</i> :	0 to 1				
Range:	1e-323 to 8e+307				

invweibullph	tail( <i>a</i> , <i>b</i> , <i>g</i> , <i>p</i> )			
Description:	the inverse reverse cumulative Weibull (proportional hazards) distribution with shape			
	a, scale b, and location g: if weibullphtail( $a, b, g, x$ ) = p, then			
	invweibullphtail(a,b,g,p) = x			
Domain <i>a</i> :	1e-323 to 8e+307			
Domain <i>b</i> :	1e-323 to 8e+307			
Domain g:	-8e+307 to $8e+307$			
Domain <i>p</i> :	0 to 1			
Range:	g + c(epsdouble) to $8e+307$			

### Wishart distribution

lnwishartden(df, V, X)

Description: the natural logarithm of the density of the Wishart distribution; missing if  $df \le n-1$ 

	df denotes the degrees of freedom, V is the scale matrix, and X is the Wishart random				
	matrix.				
Domain <i>df</i> :	1 to 1e+100 (may be nonintegral)				
Domain V:	$n \times n$ , positive-definite, symmetric matrices				
Domain X:	$n \times n$ , positive-definite, symmetric matrices				
Range:	-8e+307 to $8e+307$				

lniwishartden(df, V, X)

Description:	the natural logarithm of the density of the inverse Wishart distribution; missing if				
	$df \le n-1$				
	df denotes the degrees of freedom, V is the scale matrix, and X is the inverse Wishart				
	random matrix.				
Domain $df$ :	1 to 1e+100 (may be nonintegral)				
Domain V:	$n \times n$ , positive-definite, symmetric matrices				
Domain X:	$n \times n$ , positive-definite, symmetric matrices				
Range:	-8e+307 to $8e+307$				

John Wishart (1898–1956) was born in Montrose, Scotland. He obtained a degree in mathematics and physics from the University of Edinburgh. He learned mathematics from E. T. Whittaker, upon whose recommendation he became Karl Pearson's research assistant. During his apprenticeship, he worked on approximations to the incomplete beta function and published multiple papers on this topic. He is best known for deriving the generalized product moment distribution, which was consequently named the Wishart distribution. This distribution is a critical component in the calculation of covariance matrices and Bayesian statistics.

Wishart served in both world wars, fighting with the Black Watch regiment in the first and working for the Intelligence Corps in the second. Upon his return from World War II, he resumed his involvement with the Royal Statistical Society, becoming chairman of the Research Section in 1945. A few years later, he also served as Associate Editor for the journal *Biometrika*.

He taught courses in statistics and agriculture at Cambridge and became the Head of the Statistical Laboratory. He published multiple papers applying statistical methods to agricultural research and was involved with the United Nations Food and Agriculture Organization. He was in Mexico to establish an agricultural research center on behalf of this organization when he died.

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### Also see

- [FN] Functions by category
- [D] egen Extensions to generate
- [D] generate Create or change contents of variable
- [M-4] Statistical Statistical functions
- [U] 13.3 Functions

# String functions

	Contents	Functions	References	Also see		
Contents						
abbrev(s,n)	na	name $s$ , abbreviated to a length of $n$				
char(n)	th	the character corresponding to ASCII or extended ASCII code $n$ ; "" if $n$ is not in the domain				
collatorlocale( <i>loc</i>	, <i>type</i> ) th	the most closely related locale supported by ICU from $loc$ if $type$ is 1; the actual locale where the collation data comes from if $type$ is 2				
collatorversion(lo	<i>c</i> ) th	the version string of a collator based on locale <i>loc</i>				
$indexnot(s_1, s_2)$	th	the position in ASCII string $s_1$ of the first character of $s_1$ not found in ASCII string $s_2$ , or 0 if all characters of $s_1$ are found in $s_2$				
plural(n,s)	th	e plural of s if	$n \neq \pm 1$			
$plural(n, s_1, s_2)$	th	the plural of $s_1$ , as modified by or replaced with $s_2$ , if $n \neq \pm 1$				
real(s)	s	converted to n	umeric or missin	ng		
regexcapture(n)	su	bexpression <i>n</i>	from a previous	<pre>regerm() or regermatch() match</pre>		
regexcapturenamed	(grp) su	-		matching group named $grp$ in regular egexm() or regermatch() match		
regexm(s, re)	a			, which evaluates to 1 if regular ex- ASCII string <i>s</i> ; otherwise, 0		
regermatch( $s, re[, m]$ regerr( $s_1, re, s_2$ )	a	match of a reg pression <i>re</i> is places the first	s satisfied by the substring within	, which evaluates to 1 if regular ex- ASCII string s; otherwise, 0 ASCII string $s_1$ that matches $re$ with e resulting string		
$regerreplace(s_1, re$		mt[,std[,nl])places the first	alt]]]) substring within	ASCII string $s_1$ that matches $re$ with e resulting string		
$regexreplaceall(s_1$		places all subs		CII string $s_1$ that match $re$ with ASCII lting string		
<pre>regexs(n)</pre>	su	bexpression $n$ where $0 \le n$		<pre>regerm() or regermatch() match,</pre>		
soundex(s)	th	e soundex cod	e for a string, s			
$\texttt{soundex\_nara}(s)$	th	e US Census s	oundex code for	a string, s		
$\texttt{strcat}(s_1, s_2)$	th	ere is no stro to concatenat		instead the addition operator is used		
$strdup(s_1, n)$	th		up() function; i multiple copies	nstead the multiplication operator is s of strings		
string(n)	a	synonym for s	trofreal(n)			
string(n,s)	a	synonym for s	trofreal(n,s)	)		
<pre>stritrim(s)</pre>	s	<b>.</b> .	consecutive int ollapsed to one l	ernal blanks (ASCII space character blank		

<pre>strlen(s)</pre>	the number of characters in ASCII s or length in bytes
strlower(s)	lowercase ASCII characters in string $s$
<pre>strltrim(s)</pre>	s without leading blanks (ASCII space character char(32))
$\texttt{strmatch}(s_1, s_2)$	1 if $s_1$ matches the pattern $s_2$ ; otherwise, 0
<pre>strofreal(n)</pre>	n converted to a string
strofreal(n,s)	n converted to a string using the specified display format
$strpos(s_1, s_2)$	the position in $s_1$ at which $s_2$ is first found, 0 if $s_2$ does not occur, and 1 if $s_2$ is empty
<pre>strproper(s)</pre>	a string with the first ASCII letter and any other letters immediately following characters that are not letters capitalized; all other ASCII letters converted to lowercase
strreverse(s)	the reverse of ASCII string s
$strrpos(s_1, s_2)$	the position in $s_1$ at which $s_2$ is last found, 0 if $s_2$ does not occur, and 1 if $s_2$ is empty
<pre>strrtrim(s)</pre>	s without trailing blanks (ASCII space character char(32))
strtoname(s[,p])	s translated into a Stata 13 compatible name
<pre>strtrim(s)</pre>	<pre>s without leading and trailing blanks (ASCII space character char(32)); equivalent to strltrim(strrtrim(s))</pre>
<pre>strupper(s)</pre>	uppercase ASCII characters in string s
$subinstr(s_1, s_2, s_3, n)$	$s_1,$ where the first $n$ occurrences in $s_1$ of $s_2$ have been replaced with $s_3$
$subinword(s_1, s_2, s_3, n)$	$s_1$ , where the first <i>n</i> occurrences in $s_1$ of $s_2$ as a word have been replaced with $s_3$
$substr(s, n_1, n_2)$	the substring of $s$ , starting at $n_1$ , for a length of $n_2$
tobytes(s[,n])	escaped decimal or hex digit strings of up to 200 bytes of $s$
uchar(n)	the Unicode character corresponding to Unicode code point $n$ or an empty string if $n$ is beyond the Unicode code-point range
udstrlen(s)	the number of display columns needed to display the Unicode string s in the Stata Results window
$udsubstr(s, n_1, n_2)$	the Unicode substring of $s$ , starting at character $n_1$ , for $n_2$ display columns
uisdigit(s)	1 if the first Unicode character in <i>s</i> is a Unicode decimal digit; otherwise, 0
uisletter(s)	1 if the first Unicode character in $s$ is a Unicode letter; otherwise, 0
$\texttt{ustrcompare}(s_1, s_2[, loc])$	compares two Unicode strings
$ustrcompareex(s_1, s_2, loc, st, c)$	case, cslv, norm, num, alt, fr) compares two Unicode strings
ustrfix(s[,rep])	replaces each invalid UTF-8 sequence with a Unicode character
ustrfrom(s,enc,mode)	converts the string $s$ in encoding $enc$ to a UTF-8 encoded Unicode string
ustrinvalidcnt(s)	the number of invalid UTF-8 sequences in $s$
ustrleft(s,n)	the first $n$ Unicode characters of the Unicode string $s$
ustrlen(s)	the number of characters in the Unicode string $\boldsymbol{s}$
ustrlower(s[,loc])	lowercase all characters of Unicode string $s$ under the given locale $loc$

ustrltrim(s)	removes the leading Unicode whitespace characters and blanks from the Unicode string $s$
<pre>ustrnormalize(s,norm)</pre>	normalizes Unicode string $s$ to one of the five normalization forms specified by $norm$
$\texttt{ustrpos}(s_1, s_2[, n])$	the position in $s_1$ at which $s_2$ is first found; otherwise, 0
ustrregexm(s, re[, noc])	performs a match of a regular expression and evaluates to 1 if regular expression $re$ is satisfied by the Unicode string $s$ ; otherwise, 0
$ustrregexra(s_1, re, s_2[, noc])$	replaces all substrings within the Unicode string $s_1$ that match $re$ with $s_2$ and returns the resulting string
$ustrregexrf(s_1, re, s_2[, noc])$	replaces the first substring within the Unicode string $s_1$ that matches $re$ with $s_2$ and returns the resulting string
ustrregexs(n)	subexpression $n$ from a previous ustrregexm() match
ustrreverse(s)	the reverse of Unicode string s
ustrright(s,n)	the last $n$ Unicode characters of the Unicode string $s$
$ustrrpos(s_1,s_2[,n])$	the position in $s_1$ at which $s_2$ is last found; otherwise, 0
ustrrtrim(s)	remove trailing Unicode whitespace characters and blanks from the Unicode string $s$
ustrsortkey(s[,loc])	generates a null-terminated byte array that can be used by the sort command to produce the same order as ustrcompare()
<pre>ustrsortkeyex(s,loc,st,case)</pre>	<pre>,cslv,norm,num,alt,fr) generates a null-terminated byte array that can be used by the sort command to produce the same order as ustrcompare()</pre>
ustrtitle(s[,loc])	a string with the first characters of Unicode words titlecased and other characters lowercased
<pre>ustrto(s,enc,mode)</pre>	converts the Unicode string <i>s</i> in UTF-8 encoding to a string in encoding <i>enc</i>
ustrtohex(s[,n])	escaped hex digit string of s up to 200 Unicode characters
ustrtoname( $s[,p]$ )	string s translated into a Stata name
ustrtrim(s)	removes leading and trailing Unicode whitespace characters and blanks from the Unicode string $s$
ustrunescape(s)	the Unicode string corresponding to the escaped sequences of $s$
ustrupper(s[,loc])	uppercase all characters in string $s$ under the given locale $loc$
ustrword(s, n[, loc])	the $n$ th Unicode word in the Unicode string $s$
ustrwordcount(s[,loc])	the number of nonempty Unicode words in the Unicode string $s$
$usubinstr(s_1, s_2, s_3, n)$	replaces the first $n$ occurrences of the Unicode string $s_2$ with the Unicode string $s_3$ in $s_1$
$usubstr(s, n_1, n_2)$	the Unicode substring of $s$ , starting at $n_1$ , for a length of $n_2$
word(s,n)	the <i>n</i> th word in <i>s</i> ; <i>missing</i> ("") if <i>n</i> is missing

<pre>wordbreaklocale(loc,type)</pre>	the most closely related locale supported by ICU from loc if type is
	1, the actual locale where the word-boundary analysis data come
	from if $type$ is 2; or an empty string is returned for any other $type$
wordcount(s)	the number of words in s
wordcount(s)	from if $type$ is 2; or an empty string is returned for any other $t$

# **Functions**

In the display below, s indicates a string subexpression (a string literal, a string variable, or another string expression) and n indicates a numeric subexpression (a number, a numeric variable, or another numeric expression).

If your strings contain Unicode characters or you are writing programs that will be used by others who might use Unicode strings, read [U] **12.4.2 Handling Unicode strings**.

abbrev(s,n)	
Description:	name $s$ , abbreviated to a length of $n$
	Length is measured in the number of display columns, not in the number of charac- ters. For most users, the number of display columns equals the number of characters. For a detailed discussion of display columns, see [U] <b>12.4.2.2 Displaying Unicode</b> <b>characters</b> .
	If any of the characters of s are a period, ".", and $n < 8$ , then the value of n defaults to a value of 8. Otherwise, if $n < 5$ , then n defaults to a value of 5. If n is missing, abbrev() will return the entire string s. abbrev() is typically used with variable names and variable names with factor-variable or time-series operators (the period case).
	abbrev("displacement",8) is displa~t.
Domain s:	strings
Domain <i>n</i> :	integers 5 to 32
Range:	strings
char(n)	
Description:	the character corresponding to ASCII or extended ASCII code $n$ ; "" if $n$ is not in the domain
Domain n:	Note: ASCII codes are from 0 to 127; extended ASCII codes are from 128 to 255. Prior to Stata 14, the display of extended ASCII characters was encoding dependent. For example, char (128) on Microsoft Windows using Windows-1252 encoding displayed the Euro symbol, but on Linux using ISO-Latin-1 encoding, char (128) displayed an invalid character symbol. Beginning with Stata 14, Stata's display encoding is UTF-8 on all platforms. The char (128) function is an invalid UTF-8 sequence and thus will display a question mark. There are two Unicode functions corresponding to char(): uchar() and ustrunescape(). You can use uchar (8364) or ustrunescape ("\u20AC") to display a Euro sign on all platforms.
Range:	ASCII characters

uchar(n) Description:	the Unicode character corresponding to Unicode code point $n$ or an empty string if $n$ is beyond the Unicode code-point range
	Note that uchar() takes the decimal value of the Unicode code point. ustrunescape() takes an escaped hex digit string of the Unicode code point. For example, both uchar(8364) and ustrunescape("\u20ac") produce the Euro sign.
Domain <i>n</i> : Range:	integers $\geq 0$ Unicode characters

#### collatorlocale(loc,type)

Description:	the most closely related locale supported by ICU from $loc$ if $type$ is 1; the actual locale where the collation data comes from if $type$ is 2
	For any other type, loc is returned in a canonicalized form.
	$collatorlocale("en_us_texas", 0) = en_US_TEXAS$
	colletorlocalo("on us toras" 1) - on US

	$collatorlocale("en_us_texas", 1) = en_0s$
	<pre>collatorlocale("en_us_texas", 2) = root</pre>
Domain loc:	strings of locale name
Domain type:	integers
Range:	strings

#### collatorversion(*loc*)

Description: the version string of a collator based on locale *loc* 

The Unicode standard is constantly adding more characters and the sort key format may change as well. This can cause ustrsortkey() and ustrsortkeyex() to produce incompatible sort keys between different versions of International Components for Unicode. The version string can be used for versioning the sort keys to indicate when saved sort keys must be regenerated. strings

#### $indexnot(s_1, s_2)$

Range:

Description:	the position in ASCII string $s_1$ of the first character of $s_1$ not found in ASCII string $s_2$ , or 0 if all characters of $s_1$ are found in $s_2$
	indexnot() is intended for use only with plain ASCII strings. For Unicode charac- ters beyond the plain ASCII range, the position and character are given in bytes, not
Domain $s_1$ :	characters. ASCII strings (to be searched)
Domain $s_2$ :	ASCII strings (to search for)
Range:	$integers \ge 0$

```
plural(n,s)
  Description:
                  the plural of s if n \neq \pm 1
                  The plural is formed by adding "s" to s.
                  plural(1, "horse") = "horse"
                  plural(2, "horse") = "horses"
  Domain n:
                  real numbers
   Domain s:
                  strings
   Range:
                  strings
plural(n, s_1, s_2)
  Description:
                  the plural of s_1, as modified by or replaced with s_2, if n \neq \pm 1
                  If s_2 begins with the character "+", the plural is formed by adding the remainder of
                  s_2 to s_1. If s_2 begins with the character "-", the plural is formed by subtracting the
                  remainder of s_2 from s_1. If s_2 begins with neither "+" nor "-", then the plural is
                   formed by returning s_2.
                  plural(2, "glass", "+es") = "glasses"
                  plural(1, "mouse", "mice") = "mouse"
                  plural(2, "mouse", "mice") = "mice"
                  plural(2, "abcdefg", "-efg") = "abcd"
  Domain n:
                  real numbers
  Domain s_1:
                  strings
   Domain s_2:
                  strings
   Range:
                  strings
real(s)
  Description:
                  s converted to numeric or missing
                  Also see strofreal().
                  real("5.2")+1 = 6.2
                  real("hello") = .
   Domain s:
                  strings
                   -8e+307 to 8e+307 or missing
   Range:
regexcapture(n)
  Description:
                  subexpression n from a previous regerm() or regermatch() match
                  regexcapture(0) returns the entire string that satisfied the regular expression.
   Domain n:
                  integers
                  ASCII strings or missing
   Range:
regexcapturenamed(grp)
  Description:
                  subexpression corresponding to matching group named qrp in regular expression
                   from a previous regexm() or regexmatch() match
```

Domain grp: ASCII strings

Range: ASCII strings or missing

regexm(s,re) Description:	a match of a regular expression, which evaluates to 1 if regular expression $re$ is satisfied by the ASCII string $s$ ; otherwise, 0
	Regular expression syntax is based on Henry Spencer's NFA algorithm, and this is nearly identical to the POSIX.2 standard. $s$ and $re$ may not contain binary 0 (\0).
	regerm() is intended for use only with plain ASCII characters. For Unicode characters beyond the plain ASCII range, the match is based on bytes. For a character-based match, see ustregerm().
Domain <i>s</i> : Domain <i>re</i> : Range:	For more advanced regular expression matching, see regermatch(). ASCII strings regular expressions 0, 1, or <i>missing</i>

regexmatch(s,re[,noc[,std[,nlalt]]])

тс	0	
	Description:	a match of a regular expression, which evaluates to 1 if regular expression $re$ is satisfied by the ASCII string $s$ ; otherwise, 0
		regermatch() is intended for use only with plain ASCII characters. For Unicode characters beyond the plain ASCII range, the match is based on bytes. For a character-based match, see ustrregerm().
		If <i>noc</i> is specified and is not 0, a case-insensitive match is performed; otherwise, a case-sensitive match is performed.
		<i>std</i> specifies the regular expression standard: 1 for POSIX Extended Regular, 2 for POSIX Basic Regular, 3 for Emacs, 4 for AWK, 5 for grep, 6 for egrep, or any other number for Perl, the default.
		If $nlalt$ is specified and is 0, the newline character, char(10), is not treated like alternation operator $ $ ; otherwise, newline has the same effect as $ $ .
		s and $re$ may not contain binary 0 (\0).
	Domain s:	ASCII strings
	Domain re:	regular expression
	Domain noc:	integers
	Domain <i>std</i> :	integers
	Domain <i>nlalt</i> :	integers

Domain nlalt:integersRange:0, 1, or missing

 $regexr(s_1, re, s_2)$ 

Description: replaces the first substring within ASCII string  $s_1$  that matches re with ASCII string  $s_2$ and returns the resulting string

If  $s_1$  contains no substring that matches re, the unaltered  $s_1$  is returned.  $s_1$  and the result of regexr() may be at most 1,100,000 characters long.  $s_1$ , re, and  $s_2$  may not contain binary 0 (\0).

regexr() is intended for use only with plain ASCII characters. For Unicode characters beyond the plain ASCII range, the match is based on bytes, and the result is restricted to 1,100,000 bytes. For a character-based match, see ustrregexrf() or ustrregexra().

For more advanced regular expression replacement, see regexreplace() and regexreplaceall().

- Domain  $s_1$ : ASCII strings
- Domain *re*: regular expressions
- Domain  $s_2$ : ASCII strings
- Range: ASCII strings

#### $regexreplace(s_1, re, s_2[, noc[, fmt[, std[, nlalt]]]))$

Description:

replaces the first substring within ASCII string  $s_1$  that matches re with ASCII string  $s_2$ 

and returns the resulting string

If *noc* is specified and is not 0, a case-insensitive match is performed; otherwise, a case-sensitive match is performed.

fmt specifies the format string syntax supported in  $s_2$ : 1 for literal, where  $s_2$  is treated as a string literal (no special character substitution), 2 for sed, or any other number for Perl, the default.

*std* specifies the regular expression standard: 1 for POSIX Extended Regular, 2 for POSIX Basic Regular, 3 for Emacs, 4 for AWK, 5 for grep, 6 for egrep, or any other number for Perl, the default.

If nlalt is specified and is 0, the newline character, char(10), is not treated like alternation operator |; otherwise, newline has the same effect as |.

If  $s_1$  contains no substring that matches re, the unaltered  $s_1$  is returned.  $s_1, s_2$ , and re may not contain binary 0 (\0).

Domain  $s_1$ : ASCII strings

- Domain *re*: regular expression
- Domain  $s_2$ : ASCII strings
- Domain *noc*: integers
- Domain fmt: integers
- Domain *std*: integers
- Domain *nlalt*: integers
- Range: ASCII strings

regexreplaceal Description:	$(s_1, re, s_2[, noc[, fmt[, std[, nlalt]]]])$ replaces all substrings within ASCII string $s_1$ that match $re$ with ASCII string $s_2$ and returns the resulting string
	If $noc$ is specified and is not 0, a case-insensitive match is performed; otherwise, a case-sensitive match is performed.
	$fmt$ specifies the format string syntax supported in $s_2$ : 1 for literal, where $s_2$ is treated as a string literal (no special character substitution), 2 for sed, or any other number for Perl, the default.
	<i>std</i> specifies the regular expression standard: 1 for POSIX Extended Regular, 2 for POSIX Basic Regular, 3 for Emacs, 4 for AWK, 5 for grep, 6 for egrep, or any other number for Perl, the default.
	If $nlalt$ is specified and is 0, the newline character, char(10), is not treated like alternation operator  ; otherwise, newline has the same effect as  .
Domain $s_1$ :	If $s_1$ contains no substring that matches $re$ , the unaltered $s_1$ is returned. $s_1$ , $s_2$ , and $re$ may not contain binary 0 (\0). ASCII strings
Domain <i>re</i> :	regular expression
Domain $s_2$ : Domain <i>noc</i> :	ASCII strings integers
Domain $fmt$ :	integers
Domain <i>std</i> :	integers
Domain <i>nlalt</i> :	integers
Range:	ASCII strings

## regexs(n)

Description:	subexpression $n$ from a previous <code>regexm()</code> or <code>regexmatch()</code> match, where $0 \leq n < 10$
	Subexpression 0 is reserved for the entire string that satisfied the regular expression. The returned subexpression may be at most 1,100,000 characters (bytes) long.
Domain <i>n</i> : Range:	For more options to return matching substrings, see regexcapture() and regexcapturenamed(). 0 to 9 ASCII strings

ustrregexm(s, re[, noc])

Description: performs a match of a regular expression and evaluates to 1 if regular expression re is satisfied by the Unicode string s; otherwise, 0

> If noc is specified and not 0, a case-insensitive match is performed. The function may return a negative integer if an error occurs.

```
ustrregexm("12345", "([0-9]){5}") = 1
              ustrregexm("de TRÈS près", "rès") = 1
              ustrregexm("de TRÈS près", "Rès") = 0
              ustrregexm("de TRÈS près", "Rès", 1) = 1
              Unicode strings
Domain s:
              Unicode regular expressions
Domain re:
Domain noc:
              integers
              integers
```

### ustrregexrf( $s_1$ , re, $s_2$ [, noc])

Range:

Description:	replaces the first substring within the Unicode string $s_1$ that matches $re$ with $s_2$ and returns the resulting string
	If <i>noc</i> is specified and not 0, a case-insensitive match is performed. The function may return an empty string if an error occurs.
	ustrregexrf("très près", "rès", "X") = "tX près" ustrregexrf("TRÈS près", "Rès", "X") = "TRÈS près" ustrregexrf("TRÈS près", "Rès", "X", 1) = "TX près"
Domain $s_1$ :	Unicode strings
Domain $re$ :	Unicode regular expressions
Domain $s_2$ :	Unicode strings
Domain noc:	integers
Range:	Unicode strings

# $ustrregexra(s_1, re, s_2[, noc])$

Description:	replaces all substrings within the Unicode string $s_1$ that match $re$ with $s_2$ and returns the resulting string
	If <i>noc</i> is specified and not 0, a case-insensitive match is performed. The function may return an empty string if an error occurs.
	ustrregexra("très près", "rès", "X") = "tX pX" ustrregexra("TRÈS près", "Rès", "X") = "TRÈS près" ustrregexra("TRÈS près", "Rès", "X", 1) = "TX pX"
Domain $s_1$ :	Unicode strings
Domain re:	Unicode regular expressions
Domain $s_2$ :	Unicode strings
Domain noc:	integers
Range:	Unicode strings

ustrregexs(n) Description:	subexpression $n$ from a previous ustrregexm() match Subexpression 0 is reserved for the entire string that satisfied the regular expression. The function may return an empty string if $n$ is larger than the maximum count of subexpressions from the previous match or if an error occurs.	
Domain <i>n</i> : Range:	integers $\geq 0$ strings	
soundex(s)		
Description:	the soundex code for a string, s	
	The soundex code consists of a letter followed by three numbers: the letter is the first ASCII letter of the name and the numbers encode the remaining consonants. Similar sounding consonants are encoded by the same number. Unicode characters beyond the plain ASCII range are ignored.	
	<pre>soundex("Ashcraft") = "A226" soundex("Robert") = "R163" soundex("Rupert") = "R163"</pre>	
Domain s: Range:	strings strings	
<pre>soundex_nara(s)</pre>		
Description:	the US Census soundex code for a string, s	
	The soundex code consists of a letter followed by three numbers: the letter is the first ASCII letter of the name and the numbers encode the remaining consonants. Similar sounding consonants are encoded by the same number. Unicode characters beyond the plain ASCII range are ignored.	
	<pre>soundex_nara("Ashcraft") = "A261"</pre>	
Domain <i>s</i> : Range:	strings strings	
$strcat(s_1,s_2)$		
Description:	<pre>there is no strcat() function; instead the addition operator is used to concatenate strings "hello " + "world" = "hello world"</pre>	
	"a" + "b" = "ab"	
Domain $s_1$ : Domain $s_2$ :	"Café " + "de Flore" = "Café de Flore" strings strings	
Range:	strings	

strdup $(s_1, n)$ Description: Domain $s_1$ : Domain $n$ : Range:	there is no strdup() function; instead the multiplication operator is used to create multiple copies of strings "hello" * 3 = "hellohellohello" 3 * "hello" = "hellohellohello" 0 * "hello" = "" "hello" * 1 = "hello" "Здравствуйте " * 2 = "Здравствуйте Здравствуйте " strings nonnegative integers 0, 1, 2, strings
<pre>string(n) Description:</pre>	a synonym for strofreal(n)
string(n,s) Description:	a synonym for $strofreal(n,s)$
stritrim(s) Description:	s with multiple, consecutive internal blanks (ASCII space character char(32)) collapsed to one blank
Domain s: Range:	<pre>stritrim("hello there") = "hello there" strings strings with no multiple, consecutive internal blanks</pre>
<pre>strlen(s) Description:</pre>	the number of characters in ASCII s or length in bytes
	strlen() is intended for use only with plain ASCII characters and for use by pro- grammers who want to obtain the byte-length of a string. Note that any Unicode character beyond ASCII range (code point greater than 127) takes more than 1 byte in the UTF-8 encoding; for example, é takes 2 bytes.
	For the number of characters in a Unicode string, see ustrlen().
	<pre>strlen("ab") = 2 strlen("é") = 2</pre>
Domain s: Range:	strings integers $\geq 0$

ustrlen(s)	
Description:	the number of characters in the Unicode string $s$
	An invalid UTF-8 sequence is counted as one Unicode character. An invalid UTF-8 sequence may contain one byte or multiple bytes. Note that any Unicode character beyond the plain ASCII range (code point greater than 127) takes more than 1 byte in the UTF-8 encoding; for example, é takes 2 bytes.
	ustrlen("médiane") = 7 strlen("médiane") = 8
Domain <i>s</i> : Range:	Unicode strings integers $\geq 0$
udstrlen(s) Description:	the number of display columns needed to display the Unicode string $s$ in the Stata Results window
	A Unicode character in the CJK (Chinese, Japanese, and Korean) encoding usually requires two display columns; a Latin character usually requires one column. Any invalid UTF-8 sequence requires one column.
	udstrlen("中值") = 4 ustrlen("中值") = 2 strlen("中值") = 6
Domain <i>s</i> : Range:	Unicode strings integers $\geq 0$
<pre>strlower(s)</pre>	
Description:	lowercase ASCII characters in string $s$
	Unicode characters beyond the plain ASCII range are ignored.
Domain <i>s</i> : Range:	<pre>strlower("THIS") = "this" strlower("CAFÉ") = "cafÉ" strings strings with lowercased characters</pre>

ustrlower(s[,l])	
Description:	lowercase all characters of Unicode string s under the given locale $loc$
	If <i>loc</i> is not specified, the default locale is used. The same <i>s</i> but different <i>loc</i> may produce different results; for example, the lowercase letter of "I" is "i" in English but a dotless "i" in Turkish. The same Unicode character can be mapped to different Unicode characters based on its surrounding characters; for example, Greek capital letter sigma $\Sigma$ has two lowercases: $\varsigma$ , if it is the final character of a word, or $\sigma$ . The result can be longer or shorter than the input Unicode string in bytes.
	ustrlower("MÉDIANE","fr") = "médiane" ustrlower("ISTANBUL","tr") = "ıstanbul" ustrlower("ΟΔΥΣΣΕΎΣ") = "όδυσσεύς"
Domain s:	Unicode strings
Domain <i>loc</i> : Range:	locale name Unicode strings
8	6
<pre>strltrim(s)</pre>	
Description:	s without leading blanks (ASCII space character char(32))
_	<pre>strltrim(" this") = "this"</pre>
Domain s: Range:	strings strings without leading blanks
Range.	sumgs whilour reading blanks
ustrltrim(x)	
Description:	removes the leading Unicode whitespace characters and blanks from the Unicode string $\boldsymbol{s}$
	Note that, in addition to char(32), ASCII characters char(9), char(10), char(11), char(12), and char(13) are whitespace characters in Unicode standard.
	<pre>ustrltrim(" this") = "this" ustrltrim(char(9)+"this") = "this"</pre>
Domain s:	ustrltrim(ustrunescape("\u1680")+" this") = "this" Unicode strings
Range:	Unicode strings

$strmatch(s_1, s_2)$ Description:	1 if $s_1$ matches the pattern $s_2$ ; otherwise, 0
	strmatch("17.4", "1??4") returns 1. In $s_2$ , "?" means that one character goes here, and "*" means that zero or more bytes go here. Note that a Unicode character may contain multiple bytes; thus, using "*" with Unicode characters can infrequently result in matches that do not occur at a character boundary.
	Also see regerm(), regerr(), and regers().
Domain $s_1$ : Domain $s_2$ : Range:	<pre>strmatch("café", "caf?") = 1 strings strings integers 0 or 1</pre>
<pre>strofreal(n)</pre>	
Description:	n converted to a string
	Also see real().
	<pre>strofreal(4)+"F" = "4F" strofreal(1234567) = "1234567" strofreal(12345678) = "1.23e+07" strofreal(.) = "."</pre>
Domain <i>n</i> : Range:	-8e+307 to 8e+307 or missing strings
<pre>strofreal(n,s)</pre>	
Description:	n converted to a string using the specified display format
	Also see real().
Domain <i>n</i> :	<pre>strofreal(4,"%9.2f") = "4.00" strofreal(123456789,"%11.0g") = "123456789" strofreal(123456789,"%13.0gc") = "123,456,789" strofreal(0,"%td") = "01jan1960" strofreal(225,"%tq") = "2016q2" strofreal(225,"not a format") = "" -8e+307 to 8e+307 or missing</pre>
Domain <i>s</i> : Range:	strings containing % fmt numeric display format strings

```
Description:
                   the position in s_1 at which s_2 is first found, 0 if s_2 does not occur, and 1 if s_2 is empty
                   strpos() is intended for use only with plain ASCII characters and for use by program-
                   mers who want to obtain the byte-position of s_2. Note that any Unicode character
                   beyond ASCII range (code point greater than 127) takes more than 1 byte in the UTF-8
                   encoding; for example, é takes 2 bytes.
                   To find the character position of s_2 in a Unicode string, see ustrpos().
                   strpos("this","is") = 3
                   strpos("this","it") = 0
                   strpos("this","") = 1
                   strings (to be searched)
   Domain s_1:
   Domain s_2:
                   strings (to search for)
   Range:
                   integers \geq 0
ustrpos(s_1,s_2|,n|)
   Description:
                   the position in s_1 at which s_2 is first found; otherwise, 0
                   If n is specified and is greater than 0, the search starts at the nth Unicode charac-
                   ter of s_1. An invalid UTF-8 sequence in either s_1 or s_2 is replaced with a Unicode
                   replacement character \ufffd before the search is performed.
                   ustrpos("médiane", "édi") = 2
                   ustrpos("médiane", "édi", 3) = 0
                   ustrpos("médiane", "éci") = 0
                   Unicode strings (to be searched)
   Domain s_1:
                   Unicode strings (to search for)
   Domain s_2:
   Domain n:
                   integers
   Range:
                   integers
```

 $strpos(s_1, s_2)$ 

#### strproper(s)

Description: a string with the first ASCII letter and any other letters immediately following characters that are not letters capitalized; all other ASCII letters converted to lowercase

strproper() implements a form of titlecasing and is intended for use only with plain ASCII strings. Unicode characters beyond ASCII are treated as characters that are not letters. To titlecase strings with Unicode characters beyond the plain ASCII range or to implement language-sensitive rules for titlecasing, see ustritle().

```
strproper("mR. joHn a. sMitH") = "Mr. John A. Smith"
strproper("jack o'reilly") = "Jack O'Reilly"
strproper("2-cent's worth") = "2-Cent'S Worth"
strproper("vous êtes") = "Vous êTes"
strings
strings
```

#### ustrtitle(s[,loc])

Domain s:

Range:

Description: a string with the first characters of Unicode words titlecased and other characters lowercased

If *loc* is not specified, the default locale is used. Note that a Unicode word is different from a Stata word produced by function word(). The Stata word is a space-separated token. A Unicode word is a language unit based on either a set of word-boundary rules or dictionaries for some languages (Chinese, Japanese, and Thai). The titlecase is also locale dependent and context sensitive; for example, lowercase "ij" is considered a digraph in Dutch. Its titlecase is "IJ".

```
ustrtitle("vous êtes", "fr") = "Vous Êtes"
ustrtitle("mR. joHn a. sMitH") = "Mr. John A. Smith"
ustrtitle("ijmuiden", "en") = "Ijmuiden"
ustrtitle("ijmuiden", "nl") = "IJmuiden"
Unicode strings
Unicode strings
```

Range: Unicode strings

```
strreverse(s)
```

Domain s:

Domain *loc*:

Description: the reverse of ASCII string s

strreverse() is intended for use only with plain ASCII characters. For Unicode characters beyond ASCII range (code point greater than 127), the encoded bytes are reversed.

To reverse the characters of Unicode string, see ustrreverse().

strreverse("hello") = "olleh"

Domain s: ASCII strings

Range: ASCII reversed strings

ustrreverse(s) Description:	the reverse of Unicode string s
Description	The function does not take Unicode character equivalence into consideration. Hence, a Unicode character in a decomposed form will not be reversed as one unit. An invalid UTF-8 sequence is replaced with a Unicode replacement character \uffd.
Domain <i>s</i> : Range:	ustrreverse("médiane") = "enaidém" Unicode strings reversed Unicode strings
$strrpos(s_1, s_2)$ Description:	the position in $s_1$ at which $s_2$ is last found, 0 if $s_2$ does not occur, and 1 if $s_2$ is empty
	strrpos() is intended for use only with plain ASCII characters and for use by pro- grammers who want to obtain the last byte-position of $s_2$ . Note that any Unicode character beyond ASCII range (code point greater than 127) takes more than 1 byte in the UTF-8 encoding; for example, é takes 2 bytes.
	To find the last character position of $s_2$ in a Unicode string, see ustrpos().
Domain $s_1$ : Domain $s_2$ : Range:	<pre>strrpos("this","is") = 3 strrpos("this is","is") = 6 strrpos("this is","it") = 0 strrpos("this is","") = 1 strings (to be searched) strings (to search for) integers ≥ 0</pre>
ustrrpos( $s_1$ , $s_2$ [ Description:	(, $n$ ]) the position in $s_1$ at which $s_2$ is last found; otherwise, 0
	If n is specified and is greater than 0, only the part between the first Unicode character and the nth Unicode character of $s_1$ is searched. An invalid UTF-8 sequence in either $s_1$ or $s_2$ is replaced with a Unicode replacement character \ufffd before the search is performed.
	<pre>ustrrpos("enchanté", "n") = 6 ustrrpos("enchanté", "n", 5) = 2 ustrrpos("enchanté", "n", 6) = 6 ustrrpos("enchanté", "ne") = 0</pre>
Domain $s_1$ : Domain $s_2$ :	Unicode strings (to be searched) Unicode strings (to search for)
Domain <i>n</i> : Range:	integers integers
<pre>strrtrim(s)</pre>	
Description:	s without trailing blanks (ASCII space character char(32))
Domain s: Range:	strrtrim("this ") = "this" strings strings without trailing blanks

```
ustrrtrim(s)
  Description:
                  remove trailing Unicode whitespace characters and blanks from the Unicode string
                  s
                  Note that, in addition to char(32), ASCII characters char(9), char(10),
                  char(11), char(12), and char(13) are considered whitespace characters in the
                  Unicode standard.
                  ustrrtrim("this ") = "this"
                  ustrltrim("this"+char(10)) = "this"
                  ustrrtrim("this "+ustrunescape("\u2000")) = "this"
   Domain s:
                  Unicode strings
   Range:
                  Unicode strings
strtoname(s[,p])
                  s translated into a Stata 13 compatible name
  Description:
                  strtoname() results in a name that is truncated to 32 bytes. Each character in s that
                  is not allowed in a Stata name is converted to an underscore character, _. If the first
                  character in s is a numeric character and p is not 0, then the result is prefixed with an
                  underscore. Stata 14 names may be 32 characters; see [U] 11.3 Naming conventions.
                  strtoname("name") = "name"
                  strtoname("a name") = "a_name"
                  strtoname("5",1) = "_5"
                  strtoname("5:30",1) = "_5_30"
                  strtoname("5",0) = "5"
                  strtoname("5:30",0) = "5_30"
   Domain s:
                  strings
  Domain p:
                  integers 0 or 1
   Range:
                  strings
ustrtoname(s[,p])
  Description:
                  string s translated into a Stata name
                  ustrtoname() results in a name that is truncated to 32 characters. Each character
                  in s that is not allowed in a Stata name is converted to an underscore character, _. If
                  the first character in s is a numeric character and p is not 0, then the result is prefixed
                  with an underscore.
                  ustrtoname("name",1) = "name"
                  ustrtoname("the médiane") = "the_médiane"
                  ustrtoname("Omédiane") = "_Omédiane"
                  ustrtoname("Omédiane", 1) = "_Omédiane"
                  ustrtoname("Omédiane", 0) = "Omédiane"
   Domain s:
                  Unicode strings
   Domain p:
                  integers 0 or 1
                  Unicode strings
   Range:
```

strtrim(s)	
Description:	s without leading and trailing blanks (ASCII space character char(32)); equivalent to strltrim(strrtrim(s))
	<pre>strtrim(" this ") = "this"</pre>
Domain <i>s</i> : Range:	strings strings without leading or trailing blanks
ustrtrim(s)	
Description:	removes leading and trailing Unicode whitespace characters and blanks from the Unicode string $\boldsymbol{s}$
	Note that, in addition to char(32), ASCII characters char(9), char(10), char(11), char(12), and char(13) are considered whitespace characters in the Unicode standard.
	ustrtrim(" this ") = "this"
	$\texttt{ustrtrim}(\texttt{char}(11)\texttt{+"this ")\texttt{+}\texttt{char}(13) = \texttt{"this"}$
<b>D</b>	<pre>ustrtrim(" this "+ustrunescape("\u2000")) = "this"</pre>
Domain s: Range:	Unicode strings Unicode strings
Range.	Official strings
<pre>strupper(s)</pre>	
Description:	uppercase ASCII characters in string s
	Unicode characters beyond the plain ASCII range are ignored.
	<pre>strupper("this") = "THIS"</pre>
	<pre>strupper("café") = "CAFé"</pre>
Domain s:	strings
Range:	strings with uppercased characters
ustrupper(s[,la Description:	uppercase all characters in string s under the given locale $loc$
Description.	
	If <i>loc</i> is not specified, the default locale is used. The same <i>s</i> but a different <i>loc</i> may produce different results; for example, the uppercase letter of "i" is "I" in English, but "I" with a dot in Turkish. The result can be longer or shorter than the input string in bytes; for example, the uppercase form of the German letter $\beta$ (code point \u00df) is two capital letters "SS".
Domain <i>s</i> : Domain <i>loc</i> : Range:	<pre>ustrupper("médiane","fr") = "MÉDIANE" ustrupper("Rußland", "de") = "RUSSLAND" ustrupper("istanbul", "tr") = "ISTANBUL" Unicode strings locale name Unicode strings</pre>

subinstr( $s_1$ , $s_2$ , Description:	$s_3$ , n) $s_1$ , where the first $n$ occurrences in $s_1$ of $s_2$ have been replaced with $s_3$
	subinstr() is intended for use only with plain ASCII characters and for use by pro- grammers who want to perform byte-based substitution. Note that any Unicode char- acter beyond ASCII range (code point greater than 127) takes more than 1 byte in the UTF-8 encoding; for example, é takes 2 bytes.
	To perform character-based replacement in Unicode strings, see usubinstr().
	If $n$ is <i>missing</i> , all occurrences are replaced.
	Also see regerm(), regerr(), and regers().
Domain $s_1$ : Domain $s_2$ : Domain $s_3$ : Domain $n$ : Range:	<pre>subinstr("this is the day","is","X",1) = "thX is the day" subinstr("this is the hour","is","X",2) = "thX X the hour" subinstr("this is this","is","X",.) = "thX X thX" strings (to be substituted into) strings (to be substituted from) strings (to be substituted with) integers ≥ 0 or missing strings</pre>

#### usubinstr( $s_1$ , $s_2$ , $s_3$ ,n)

Description: replaces the first n occurrences of the Unicode string  $s_2$  with the Unicode string  $s_3$ in  $s_1$ 

If n is missing, all occurrences are replaced. An invalid UTF-8 sequence in  $s_1$ ,  $s_2$ , or  $s_3$  is replaced with a Unicode replacement character \uffd before replacement is performed.

```
usubinstr("de très près", "ès", "es", 1) = "de tres près"
```

```
\texttt{usubinstr}(\texttt{"de très pr'es","ès","X",2}) = \texttt{"de trX prX"}
```

Domain  $s_1$ : Unicode strings (to be substituted into)

Domain  $s_2$ : Unicode strings (to be substituted from)

Domain  $s_3$ : Unicode strings (to be substituted with)

Domain n: integers  $\geq 0$  or missing

Range: Unicode strings

```
subinword(s_1, s_2, s_3, n)
```

Description:  $s_1$ , where the first n occurrences in  $s_1$  of  $s_2$  as a word have been replaced with  $s_3$ 

A word is defined as a space-separated token. A token at the beginning or end of  $s_1$  is considered space-separated. This is different from a Unicode word, which is a language unit based on either a set of word-boundary rules or dictionaries for several languages (Chinese, Japanese, and Thai). If n is missing, all occurrences are replaced.

```
Also see regerm(), regerr(), and regers().
```

```
subinword("this is the day","is","X",1) = "this X the day"
subinword("this is the hour","is","X",.) = "this X the hour"
subinword("this is this","th","X",.) = "this is this"
strings (to be substituted for)
strings (to be substituted from)
strings (to be substituted with)
```

Domain  $s_3$ : strings (to be substituted wi

```
Domain n: integers \geq 0 or missing
```

Range: strings

```
substr(s, n_1, n_2)
```

Domain s:

Domain  $n_1$ :

Domain  $n_2$ : Range:

Domain  $s_1$ :

Domain  $s_2$ :

Description: the substring of s, starting at  $n_1$ , for a length of  $n_2$ 

substr() is intended for use only with plain ASCII characters and for use by programmers who want to extract a subset of bytes from a string. For those with plain ASCII text,  $n_1$  is the starting character, and  $n_2$  is the length of the string in characters. For programmers, substr() is technically a byte-based function. For plain ASCII characters, the two are equivalent but you can operate on byte values beyond that range. Note that any Unicode character beyond ASCII range (code point greater than 127) takes more than 1 byte in the UTF-8 encoding; for example, é takes 2 bytes.

To obtain substrings of Unicode strings, see usubstr().

If  $n_1 < 0$ ,  $n_1$  is interpreted as the distance from the end of the string; if  $n_2 = .$  (*missing*), the remaining portion of the string is returned.

```
\begin{array}{l} {\rm substr("abcdef",2,3)="bcd"}\\ {\rm substr("abcdef",-3,2)="de"}\\ {\rm substr("abcdef",2,.)="bcdef"}\\ {\rm substr("abcdef",-3,.)="def"}\\ {\rm substr("abcdef",2,0)=""}\\ {\rm substr("abcdef",15,2)=""}\\ {\rm substr("abcdef",15,2)=""}\\ {\rm strings}\\ {\rm integers}\geq 1 \mbox{ and } \leq -1\\ {\rm integers}\geq 1\\ {\rm strings}\\ \end{array}
```

usubstr( $s, n_1, n_2$ ) Description: the Unicode substring of $s$ , starting at $n_1$ , for a length of $n_2$		
Desemption	If $n_1 < 0, n_1$ is interpreted as the distance from the last character of the $s$ ; if $n_2 = .$	
	( <i>missing</i> ), the remaining portion of the Unicode string is returned.	
	usubstr("médiane",2,3) = "édi" usubstr("médiane",-3,2) = "an"	
	usubstr("médiane",2,.) = "édiane"	
Domain s:	Unicode strings	
Domain $n_1$ : Domain $n_2$ :	integers $\geq 1$ and $\leq -1$ integers $\geq 1$	
Range:	Unicode strings	
udsubstr( $s$ , $n_1$ , Description:	$n_2$ ) the Unicode substring of s, starting at character $n_1$ , for $n_2$ display columns	
	If $n_2 = .$ ( <i>missing</i> ), the remaining portion of the Unicode string is returned. If $n_2$ display columns from $n_1$ is in the middle of a Unicode character, the substring stops at the previous Unicode character.	
	udsubstr("médiane",2,3) = "édi" udsubstr("中值",1,1) = ""	
Domain s:	udsubstr("中值",1,2) = "中" Unicode strings	
Domain $n_1$ :	integers $\geq 1$	
Domain $n_2$ :	integers $\geq 1$	
Range:	Unicode strings	
tobytes(s[,n])		
Description:	escaped decimal or hex digit strings of up to 200 bytes of $s$	
	The escaped decimal digit string is in the form of $\DDD$ . The escaped hex digit string is in the form of $\xh$ . If $n$ is not specified or is 0, the decimal form is produced. Otherwise, the hex form is produced.	
	tobytes("abc") = "\d097\d098\d099"	
	tobytes("abc", 1) = "\x61\x62\x63" tobytes("café") = "\d099\d097\d102\d195\d169"	
Domain s:	Unicode strings	
Domain <i>n</i> :	integers	
Range:	strings	
uisdigit(s)		
Description:	1 if the first Unicode character in $s$ is a Unicode decimal digit; otherwise, 0	
	A Unicode decimal digit is a Unicode character with the character property Nd ac- cording to the Unicode standard. The function returns -1 if the string starts with an invalid UTF-8 sequence.	
Domain s: Range:	Unicode strings integers	
Range.	mugus	

uisletter(s)	
Description:	1 if the first Unicode character in $s$ is a Unicode letter; otherwise, 0
Domain s:	A Unicode letter is a Unicode character with the character property L according to the Unicode standard. The function returns -1 if the string starts with an invalid UTF-8 sequence.
	Unicode strings
Range:	integers
$ustrcompare(s_1$	$, s_2[, loc])$
Description:	compares two Unicode strings
	The function returns $-1$ , 1, or 0 if $s_1$ is less than, greater than, or equal to $s_2$ . The function may return a negative number other than $-1$ if an error happens. The comparison is locale dependent. For example, $z < \ddot{o}$ in Swedish but $\ddot{o} < z$ in German. If <i>loc</i> is not specified, the default locale is used. The comparison is diacritic and case sensitive. If you need different behavior, for example, case-insensitive comparison, you should use the extended comparison function ustrcompareex(). Unicode string comparison compares Unicode strings in a language-sensitive manner. On the other hand, the sort command compares strings in code-point (binary) order. For example, uppercase "Z" (code-point value 90) comes before lowercase "a" (code-point value 97) in code-point order but comes after "a" in any English dictionary.
Domain $s_1$ : Domain $s_2$ :	<pre>ustrcompare("z", "ö", "sv") = -1 ustrcompare("z", "ö", "de") = 1 Unicode strings Unicode strings</pre>

Domain  $s_2$ : Unicode strings

Domain *loc*: Unicode strings

```
Range: integers
```

```
\texttt{ustrcompareex}(s_1, s_2, loc, st, case, cslv, norm, num, alt, fr)
```

Description: compares two Unicode strings

The function returns -1, 1, or 0 if  $s_1$  is less than, greater than, or equal to  $s_2$ . The function may return a negative number other than -1 if an error occurs. The comparison is locale dependent. For example,  $z < \ddot{o}$  in Swedish but  $\ddot{o} < z$  in German. If *loc* is not specified, the default locale is used.

st controls the strength of the comparison. Possible values are 1 (primary), 2 (secondary), 3 (tertiary), 4 (quaternary), or 5 (identical). -1 means to use the default value for the locale. Any other numbers are treated as tertiary. The primary difference represents base letter differences; for example, letter "a" and letter "b" have primary differences. The secondary difference represents diacritical differences on the same base letter; for example, letters "a" and "ä" have secondary differences. The tertiary difference represents case differences of the same base letter; for example, letters "a" and "A" have tertiary differences. Quaternary strength is useful to distinguish between Katakana and Hiragana for the JIS 4061 collation standard. Identical strength is essentially the code-point order of the string, hence, is rarely useful. ustrcompareex("café","café","fr", 1, -1, -1, -1, -1, -1, -1, -1) = 0 ustrcompareex("café","cafe","fr", 2, -1, -1, -1, -1, -1, -1) = 1 ustrcompareex("Café","café","fr", 3, -1, -1, -1, -1, -1, -1) = 1 case controls the uppercase and lowercase letter order. Possible values are 0 (use order specified in tertiary strength), 1 (uppercase first), or 2 (lowercase first). -1 means to use the default value for the locale. Any other values are treated as 0.

```
ustrcompareex("Café","café","fr", -1, 1, -1, -1, -1, -1, -1) = -1
ustrcompareex("Café","café","fr", -1, 2, -1, -1, -1, -1, -1) = 1
```

cslv controls whether an extra case level between the secondary level and the tertiary level is generated. Possible values are 0 (off) or 1 (on). -1 means to use the default value for the locale. Any other values are treated as 0. Combining this setting to be "on" and the strength setting to be primary can achieve the effect of ignoring the diacritical differences but preserving the case differences. If the setting is "on", the result is also affected by the *case* setting.

```
ustrcompareex("café","Cafe","fr", 1, -1, 1, -1, -1, -1, -1) = -1
ustrcompareex("café","Cafe","fr", 1, 1, 1, -1, -1, -1, -1) = 1
```

*norm* controls whether the normalization check and normalizations are performed. Possible values are 0 (off) or 1 (on). -1 means to use the default value for the locale. Any other values are treated as 0. Most languages do not require normalization for comparison. Normalization is needed in languages that use multiple combining characters such as Arabic, ancient Greek, or Hebrew.

*num* controls how contiguous digit substrings are sorted. Possible values are 0 (off) or 1 (on). -1 means to use the default value for the locale. Any other values are treated as 0. If the setting is "on", substrings consisting of digits are sorted based on the numeric value. For example, "100" is after value "20" instead of before it. Note that the digit substring is limited to 254 digits, and plus/minus signs, decimals, or exponents are not supported.

```
ustrcompareex("100","20","en", -1, -1, -1, -1, 0, -1, -1) = -1
ustrcompareex("100","20","en", -1, -1, -1, -1, 1, -1, -1) = 1
```

*alt* controls how spaces and punctuation characters are handled. Possible values are 0 (use primary strength) or 1 (alternative handling). Any other values are treated as 0. If the setting is 1 (alternative handling), "onsite", "on-site", and "on site" are considered equals.

fr controls the direction of the secondary strength. Possible values are 0 (off) or 1 (on). -1 means to use the default value for the locale. All other values are treated as "off". If the setting is "on", the diacritical letters are sorted backward. Note that the setting is "on" by default only for Canadian French (locale fr\_CA).

	ustrcompareex("coté","côte","fr_CA",-1,-1,-1,-1,-1,0) = -1
	ustrcompareex("coté","côte","fr_CA",-1,-1,-1,-1,-1,-1,1) = 1
	ustrcompareex("coté","côte","fr_CA",-1,-1,-1,-1,-1,-1) = 1
	ustrcompareex("coté","côte","fr",-1,-1,-1,-1,-1,-1,-1) = 1
Domain $s_1$ :	Unicode strings
Domain $s_2$ :	Unicode strings
Domain <i>loc</i> :	Unicode strings
Domain st:	integers
Domain case:	integers
Domain <i>cslv</i> :	integers
Domain norm:	integers
Domain num:	integers
Domain alt:	integers
Domain $fr$ :	integers
Range:	integers

#### ustrfix(s[,rep])

Description: replaces each invalid UTF-8 sequence with a Unicode character

> In the one-argument case, the Unicode replacement character \ufffd is used. In the two-argument case, the first Unicode character of rep is used. If rep starts with an invalid UTF-8 sequence, then Unicode replacement character \ufffd is used. Note that an invalid UTF-8 sequence can contain one byte or multiple bytes.

```
ustrfix(char(200)) = ustrunescape("\uffd")
             ustrfix("ab"+char(200)+"cdé", "") = "abcdé"
             ustrfix("ab"+char(229)+char(174)+"cdé", "é") = "abécdé"
Domain s:
             Unicode strings
Domain rep:
             Unicode character
             Unicode strings
```

#### ustrfrom(*s*,*enc*,*mode*)

Range:

Description: converts the string s in encoding enc to a UTF-8 encoded Unicode string

> mode controls how invalid byte sequences in s are handled. The possible values are 1, which substitutes an invalid byte sequence with a Unicode replacement character \ufffd; 2, which skips any invalid byte sequences; 3, which stops at the first invalid byte sequence and returns an empty string; or 4, which replaces any byte in an invalid sequence with an escaped hex digit sequence %Xhh. Any other values are treated as 1. A good use of value 4 is to check what invalid bytes a Unicode string ust contains by examining the result of ustrfrom(ust, "utf-8", 4).

Also see ustrto().

Domain s: Domain enc: Domain mode: Range:	<pre>ustrfrom("caf"+char(233), "latin1", 1) = "café" ustrfrom("caf"+char(233), "utf-8", 1) =         "caf"+ustrunescape("\uffd") ustrfrom("caf"+char(233), "utf-8", 2) = "caf" ustrfrom("caf"+char(233), "utf-8", 3) = "" ustrfrom("caf"+char(233), "utf-8", 4) = "caf%XE9" strings in encoding enc Unicode strings integers Unicode strings</pre>
ustrinvalidcnt(	s)
Description:	the number of invalid UTF-8 sequences in s
	An invalid UTF-8 sequence may contain one byte or multiple bytes.
Domain <i>s</i> : Range:	<pre>ustrinvalidcnt("médiane") = 0 ustrinvalidcnt("médiane"+char(229)) = 1 ustrinvalidcnt("médiane"+char(229)+char(174)) = 1 ustrinvalidcnt("médiane"+char(174)+char(158)) = 2 Unicode strings integers</pre>
ustrleft(s,n)	
Description:	the first $n$ Unicode characters of the Unicode string $s$
	An invalid UTF-8 sequence is replaced with a Unicode replacement character \uffd
Domain s: Domain n: Range:	ustrleft("Экспериментальные",3) = "Экс" ustrleft("Экспериментальные",5) = "Экспе" Unicode strings integers Unicode strings

### ustrnormalize(s,norm)

Description:

normalizes Unicode string s to one of the five normalization forms specified by norm

The normalization forms are nfc, nfd, nfkc, nfkd, or nfkcc. The function returns an empty string for any other value of norm. Unicode normalization removes the Unicode string differences caused by Unicode character equivalence. nfc specifies Normalization Form C, which normalizes decomposed Unicode code points to a composited form. nfd specifies Normalization Form D, which normalizes composited Unicode code points to a decomposed form. nfc and nfd produce canonical equivalent form. nfkc and nfkd are similar to nfc and nfd but produce compatibility equivalent forms. nfkcc specifies nfkc with casefolding. This normalization and casefolding implement the Unicode Character Database.

In the Unicode standard, both "i" (\u0069 followed by a diaeresis \u0308) and the composite character \u00ef represent "i" with 2 dots as in "naïve". Hence, the code-point sequence \u0069\u0308 and the code point \u00ef are considered Unicode equivalent. According to the Unicode standard, they should be treated as the same single character in Unicode string operations, such as in display, comparison, and selection. However, Stata does not support multiple code-point characters; each code point is considered a separate Unicode character. Hence, \u0069\u0308 is displayed as two characters in the Results window. ustrnormalize() can be used with "nfc" to normalize \u0069\u0308 to the canonical equivalent composited code point \u00ef.

ustrnormalize(ustrunescape("\u0069\u0308"), "nfc") = "ï"

The decomposed form nfd can be used to removed diacritical marks from base letters. First, normalize the Unicode string to canonical decomposed form, and then call ustrto() with mode skip to skip all non-ASCII characters.

Also see ustrfrom().

```
ustrto(ustrnormalize("café", "nfd"), "ascii", 2) = "cafe"
```

Domain s: Unicode strings

Domain *norm*: Unicode strings

Range: Unicode strings

#### ustrright(s,n)

#### Description: the last n Unicode characters of the Unicode string s

An invalid UTF-8 sequence is replaced with a Unicode replacement character \uffd.

	ustrright("Экспериментальные",3) = "ные" ustrright("Экспериментальные",5) = "льные"
Domain s:	Unicode strings
Domain n:	integers
Range:	Unicode strings

#### ustrsortkey(s[,loc])

Description:	generates a null-terminated byte array that can be used by the sort command to produce the same order as ustrcompare()
	The function may return an empty array if an error occurs. The result is locale dependent. If <i>loc</i> is not specified, the default locale is used. The result is also diacritic and
	case sensitive. If you need different behavior, for example, case-insensitive results,
	you should use the extended function ustrsortkeyex(). See [U] 12.4.2.5 Sorting strings containing Unicode characters for details and examples.
Domain s:	Unicode strings
Domain <i>loc</i> :	Unicode strings
Range:	null-terminated byte array

```
ustrsortkeyex(s,loc,case,cslv,norm,num,alt,fr)
```

Description:

generates a null-terminated byte array that can be used by the sort command to produce the same order as ustrcompare()

The function may return an empty array if an error occurs. The result is locale dependent. If *loc* is not specified, the default locale is used. See [U] **12.4.2.5 Sorting strings containing Unicode characters** for details and examples.

st controls the strength of the comparison. Possible values are 1 (primary), 2 (secondary), 3 (tertiary), 4 (quaternary), or 5 (identical). -1 means to use the default value for the locale. Any other numbers are treated as tertiary. The primary difference represents base letter differences; for example, letter "a" and letter "b" have primary differences. The secondary difference represents diacritical differences on the same base letter; for example, letters "a" and "ä" have secondary differences. The tertiary difference represents case differences of the same base letters; for example, letters "a" and "A" have tertiary differences. Quaternary strength is useful to distinguish between Katakana and Hiragana for the JIS 4061 collation standard. Identical strength is essentially the code-point order of the string and, hence, is rarely useful.

*case* controls the uppercase and lowercase letter order. Possible values are 0 (use order specified in tertiary strength), 1 (uppercase first), or 2 (lowercase first). -1 means to use the default value for the locale. Any other values are treated as 0.

cslv controls if an extra case level between the secondary level and the tertiary level is generated. Possible values are 0 (off) or 1 (on). -1 means to use the default value for the locale. Any other values are treated as 0. Combining this setting to be "on" and the strength setting to be primary can achieve the effect of ignoring the diacritical differences but preserving the case differences. If the setting is "on", the result is also affected by the *case* setting.

*norm* controls whether the normalization check and normalizations are performed. Possible values are 0 (off) or 1 (on). -1 means to use the default value for the locale. Any other values are treated as 0. Most languages do not require normalization for comparison. Normalization is needed in languages that use multiple combining characters such as Arabic, ancient Greek, or Hebrew.

*num* controls how contiguous digit substrings are sorted. Possible values are 0 (off) or 1 (on). -1 means to use the default value for the locale. Any other values are treated as 0. If the setting is "on", substrings consisting of digits are sorted based on the numeric value. For example, "100" is after "20" instead of before it. Note that the digit substring is limited to 254 digits, and plus/minus signs, decimals, or exponents are not supported.

*alt* controls how spaces and punctuation characters are handled. Possible values are 0 (use primary strength) or 1 (alternative handling). Any other values are treated as 0. If the setting is 1 (alternative handling), "onsite", "on-site", and "on site" are considered equals.

fr controls the direction of the secondary strength. Possible values are 0 (off) or 1 (on). -1 means to use the default value for the locale. All other values are treated as "off". If the setting is "on", the diacritical letters are sorted backward. Note that the setting is "on" by default only for Canadian French (locale fr\_CA).

Domain s: Unicode strings Domain *loc*: Unicode strings Domain st: integers Domain *case*: integers Domain *cslv*: integers Domain norm: integers Domain *num*: integers Domain *alt*: integers Domain fr: integers Range: null-terminated byte array

#### ustrto(s,enc,mode)

Description: converts the Unicode string s in UTF-8 encoding to a string in encoding enc

See [D] **unicode encoding** for details on available encodings. Any invalid sequence in *s* is replaced with a Unicode replacement character \ufffd. *mode* controls how unsupported Unicode characters in the encoding *enc* are handled. The possible values are 1, which substitutes any unsupported characters with the *enc*'s substitution strings (the substitution character for both ascii and latin1 is char(26)); 2, which skips any unsupported characters; 3, which stops at the first unsupported character and returns an empty string; or 4, which replaces any unsupported character with an escaped hex digit sequence \uhhhh or \Uhhhhhhh. The hex digit sequence contains either 4 or 8 hex digits, depending if the Unicode character's code-point value is less than or greater than \uffff. Any other values are treated as 1.

```
ustrto("café", "ascii", 1) = "caf"+char(26)
ustrto("café", "ascii", 2) = "caf"
ustrto("café", "ascii", 3) = ""
ustrto("café", "ascii", 4) = "caf\u00E9"
```

ustrto() can be used to removed diacritical marks from base letters. First, normalize the Unicode string to NFD form using ustrnormalize(), and then call ustrto() with value 2 to skip all non-ASCII characters.

Also see ustrfrom().

	<pre>ustrto(ustrnormalize("café", "nfd"), "ascii", 2) = "cafe"</pre>
Domain s:	Unicode strings
Domain enc:	Unicode strings
Domain mode:	integers
Range:	strings in encoding enc

ustrtohex(s[,n])Description: escaped hex digit string of s up to 200 Unicode characters The escaped hex digit string is in the form of \uhhhh for code points less than \ufff or Uhhhhhhhh for code points greater than uffff. The function starts at the *n*th Unicode character of s if n is specified and larger than 0. Any invalid UTF-8 sequence is replaced with a Unicode replacement character \ufffd. Note that the null terminator char(0) is a valid Unicode character. Function ustrunescape() can be applied on the result to get back the original Unicode string s if s does not contain any invalid UTF-8 sequences. Also see ustrunescape(). ustrtohex("нулю") = "\u043d\u0443\u043b\u044e" ustrtohex("нулю", 2) = "\u0443\u043b\u044e" ustrtohex("i"+char(200)+char(0)+"s") ="\u0069\ufffd\u0000\u0073" Domain s: Unicode strings Domain n: integers > 1strings Range: ustrunescape(s)Description: the Unicode string corresponding to the escaped sequences of s The following escape sequences are recognized: 4 hex digit form \uhhh; 8 hex digit form \Uhhhhhhh; 1-2 hex digit form \xhh; and 1-3 octal digit form \ooo, where h is [0-9A-Fa-f] and o is [0-7]. The standard ANSI C escapes a, b, t.  $n, v, f, r, e, ", ', ?, \cdot$  are recognized as well. The function returns an empty string if an escape sequence is badly formed. Note that the 8 hex digit form \Uhhhhhhh begins with a capital letter "U". Also see ustrtohex(). ustrunescape("\u043d\u0443\u043b\u044e") = "нулю" Domain s: strings of escaped hex values Unicode strings Range: word(s,n)Description: the *n*th word in *s*; *missing* ("") if *n* is missing Positive numbers count words from the beginning of s, and negative numbers count words from the end of s. (1 is the first word in s, and -1 is the last word in s.) A word is a set of characters that start and terminate with spaces. This is different from a Unicode word, which is a language unit based on either a set of word-boundary rules or dictionaries for several languages (Chinese, Japanese, and Thai). Domain s: strings Domain n: integers Range: strings

ustrword( $s$ , $n$ ]	loc])
Description:	the nth Unicode word in the Unicode string s
	Positive $n$ counts Unicode words from the beginning of $s$ , and negative $n$ counts Unicode words from the end of $s$ . For examples, $n$ equal to 1 returns the first word in $s$ , and $n$ equal to $-1$ returns the last word in $s$ . If <i>loc</i> is not specified, the default locale is used. A Unicode word is different from a Stata word produced by the word() function. A Stata word is a space-separated token. A Unicode word is a language unit based on either a set of word-boundary rules or dictionaries for some languages (Chinese, Japanese, and Thai). The function returns <i>missing</i> ("") if $n$ is greater than <i>cnt</i> or less than <i>-cnt</i> , where <i>cnt</i> is the number of words $s$ contains. <i>cnt</i> can be obtained from ustrwordcount(). The function also returns <i>missing</i> ("") if an error occurs.
Domain <i>s</i> : Domain <i>loc</i> : Domain <i>n</i> : Range:	<pre>ustrword("Parlez-vous français", 1, "fr") = "Parlez" ustrword("Parlez-vous français", 2, "fr") = "-" ustrword("Parlez-vous français", -1, "fr") = "français" ustrword("Parlez-vous français", -2, "fr") = "vous" Unicode strings Unicode strings integers Unicode strings</pre>

### wordbreaklocale(loc,type)

Description:	the most closely related locale supported by ICU from $loc$ if $type$ is 1, the actual locale where the word-boundary analysis data come from if $type$ is 2; or an empty string is returned for any other $type$
Domain <i>loc</i> : Domain <i>type</i> :	<pre>wordbreaklocale("en_us_texas", 1) = en_US wordbreaklocale("en_us_texas", 2) = root strings of locale name integers</pre>
Range:	strings
wordcount(s)	
Description:	the number of words in s
Domain s:	A word is a set of characters that starts and terminates with spaces, starts with the beginning of the string, or terminates with the end of the string. This is different from a Unicode word, which is a language unit based on either a set of word-boundary rules or dictionaries for several languages (Chinese, Japanese, and Thai). strings
Range:	nonnegative integers 0, 1, 2,

ustrwordcount(s[,loc])
Description: the number of nonempty Unicode words in the Unicode string s
An empty Unicode word is a Unicode word consisting of only Unicode whitespace
characters. If loc is not specified, the default locale is used. A Unicode word is
different from a Stata word produced by the word() function. A Stata word is a spaceseparated token. A Unicode word is a language unit based on either a set of wordboundary rules or dictionaries for some languages (Chinese, Japanese, and Thai).
The function may return a negative number if an error occurs.
ustrwordcount("Parlez-vous français", "fr") = 4
Domain s: Unicode strings
Domain loc: Unicode strings

## References

Range:

Cox, N. J. 2004. Stata tip 6: Inserting awkward characters in the plot. Stata Journal 4: 95-96.

- -------. 2011. Stata tip 98: Counting substrings within strings. Stata Journal 11: 318-320.
- . 2022. Stata tip 148: Searching for words within strings. Stata Journal 22: 998–1003.
- Jeanty, P. W. 2013. Dealing with identifier variables in data management and analysis. Stata Journal 13: 699-718.
- Koplenig, A. 2018. Stata tip 129: Efficiently processing textual data with Stata's new Unicode features. *Stata Journal* 18: 287–289.
- Schwarz, C. 2019. Isemantica: A command for text similarity based on latent semantic analysis. Stata Journal 19: 129-142.

# Also see

- [FN] Functions by category
- [D] egen Extensions to generate
- [D] generate Create or change contents of variable
- [M-4] String String manipulation functions

integers

- [U] 12.4.2 Handling Unicode strings
- [U] 13.2.2 String operators
- [U] 13.3 Functions

# **Trigonometric functions**

	Contents	Functions	References	Also see	
Contents					
acos(x)	th	e radian value	of the arccosine	e of x	
acosh(x)	th	e inverse hype	erbolic cosine of	x	
asin(x)	th	e radian value	of the arcsine of	f x	
asinh(x)	th	e inverse hype	erbolic sine of $x$		
atan(x)	th	e radian value	of the arctanger	nt of $x$	
atan2(y, x)	the radian value of the arctangent of $y/x$ , where the signs of the parameters $y$ and $x$ are used to determine the quadrant of the answer				
$\operatorname{atanh}(x)$	the inverse hyperbolic tangent of $x$				
$\cos(x)$	the cosine of $x$ , where $x$ is in radians				
$\cosh(x)$	th	e hyperbolic c	cosine of $x$		
sin(x)	th	e sine of $x$ , w	here $x$ is in radia	ins	
$\sinh(x)$	th	e hyperbolic s	ine of $x$		
$\tan(x)$	th	e tangent of $x$	, where $x$ is in ra	adians	
tanh(x)	th	e hyperbolic t	angent of $x$		

# **Functions**

acos (x) Description: Domain: Range:	the radian value of the arccosine of $x$ -1 to 1 0 to $\pi$
acosh(x) Description:	the inverse hyperbolic cosine of x $acosh(x) = ln(x + \sqrt{x^2 - 1})$
Domain:	$acosn(x) = m(x + \sqrt{x^2 - 1})$ 1 to 8.9e+307
Range:	0 to 709.77
asin(x)	
Description:	the radian value of the arcsine of $x$
Domain:	-1 to 1
Range:	$-\pi/2$ to $\pi/2$
asinh(x)	
Description:	the inverse hyperbolic sine of x asinh(x) = $\ln(x + \sqrt{x^2 + 1})$
Domain:	-8.9e+307 to 8.9e+307
Range:	-709.77 to 709.77

```
atan(x)
Description:
                the radian value of the arctangent of x
Domain:
                -8e+307 to 8e+307
Range:
                -\pi/2 to \pi/2
atan2(y, x)
Description:
                the radian value of the arctangent of y/x, where the signs of the parameters y and x
                are used to determine the quadrant of the answer
Domain y:
                -8e+307 to 8e+307
Domain x:
                -8e+307 to 8e+307
Range:
                -\pi to \pi
atanh(x)
Description:
                the inverse hyperbolic tangent of x
                   \operatorname{atanh}(x) = \frac{1}{2} \{ \ln(1+x) - \ln(1-x) \}
                -1 to 1
Domain:
                -8e+307 to 8e+307
Range:
\cos(x)
Description:
                the cosine of x, where x is in radians
                -1e+18 to 1e+18
Domain:
                -1 to 1
Range:
\cosh(x)
Description:
                the hyperbolic cosine of x
                   \cosh(x) = \{\exp(x) + \exp(-x)\}/2
Domain:
                -709 to 709
                1 to 4.11e+307
Range:
sin(x)
Description:
                the sine of x, where x is in radians
                -1e+18 to 1e+18
Domain:
                -1 to 1
Range:
sinh(x)
Description:
                the hyperbolic sine of x
                   \sinh(x) = \{\exp(x) - \exp(-x)\}/2
                -709 to 709
Domain:
Range:
                -4.11e+307 to 4.11e+307
\tan(x)
Description:
                the tangent of x, where x is in radians
Domain:
                -1e+18 to 1e+18
Range:
                -1e+17 to 1e+17 or missing
tanh(x)
Description:
                the hyperbolic tangent of x
                   tanh(x) = \{ \exp(x) - \exp(-x) \} / \{ \exp(x) + \exp(-x) \}
                -8e+307 to 8e+307
Domain:
Range:
                -1 to 1 or missing
```

### Technical note

The trigonometric functions are defined in terms of *radians*. There are  $2\pi$  radians in a circle. If you prefer to think in terms of *degrees*, because there are also 360 degrees in a circle, you may convert degrees into radians by using the formula  $r = d\pi/180$ , where *d* represents degrees and *r* represents radians. Stata includes the built-in constant \_pi, equal to  $\pi$  to machine precision. Thus, to calculate the sine of theta, where theta is measured in degrees, you could type

sin(theta\*\_pi/180)

atan() similarly returns radians, not degrees. The arccotangent can be obtained as

acot(x) = pi/2 - atan(x)

### 

### References

Norton, E. C. 2022. The inverse hyperbolic sine transformation and retransformed marginal effects. Stata Journal 22: 702–712.

Oldham, K. B., J. C. Myland, and J. Spanier. 2009. An Atlas of Functions. 2nd ed. New York: Springer.

### Also see

- [FN] Functions by category
- [D] egen Extensions to generate
- [D] generate Create or change contents of variable
- [M-5] sin() Trigonometric and hyperbolic functions
- [U] 13.3 Functions

# Subject and author index

See the combined subject index and the combined author index in the Stata Index.